

ACRICULTURAL RESEARCH INSTITUTE
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# PHILOSOPHICAL TRANSACTIONS,

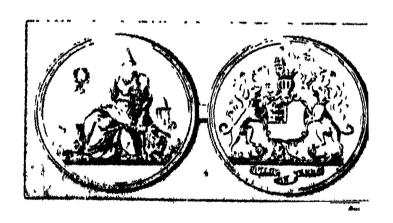
OF THE

# ROYAL SOCIETY

# LONDON.

VOL. LXXVI. For the Year 1786.

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LONDON, .

\*\* FOLD BY LOCKYER DAVIS, AND PETER ELMSLY, PRINTERS TO THE ROYAL SOCIETY: \*\*

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#### [ iii ]

## ADVERTISEMENT.

IIE Committee appointed by the Royal Society to direct the publication of the Philosophical Transactions, take this opportunity to acquaint the Public, that it fully appears, as well from the council-books and journals of the Society, as from repeated declarations which have been made in feveral former Transactions, that the printing of them was always, from time to time, the fingle act of the respective Secretaries, till the Forty-seventh Volume: the Society, as a Body, never interesting themselves any further in their publication, than by occasionally recommending the revival of them to some of their Secretaries, when, from the particular circumstances of their assairs, the Transactions had happened for any length of time to be intermitted. And this feems principally to have been done with a view to satisfy the Public, that their usual meetings were then continued for the improvement of knowledge, and benefit of mankind, the great ends of their first institution by the Royal Charters, and which they have ever fince steadily pursued.

But the Society being of late years greatly inlarged, and their communications more numerous, it was thought advisable, that a Committee of their members should be appointed to reconsider the papers read before them, and select out of them such, as they should judge most proper for publication in the suture Transactions; which was accordingly done upon the 26th of March 1752. And the grounds of their choice are, and will continue to be, the importance and singularity of the subjects, or the advantageous manner of treating them; without pretending to answer for the certainty of the facts, or propriety of the reasonings, contained in the several papers so published, which must still rest on the credit or judgment of their respective authors.

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It is likewise necessary on this occasion to remark, that it is an established rule of the Society, to which they will always adhere, never to give their opinion, as a Body, upon any subject, either of Nature or Art, that comes before them. And therefore the thanks, which are frequently proposed from the chair, to be given to the authors of such papers as are read at their accustomed meetings, or to the persons through whose hands they receive them, are to be considered in no other light than as a matter of civility, in return for the respect shewn to the Society by those communications. The like also is to be said with regard to the several projects, inventions, and curiosities of various kinds, which are often exhibited to the Society; the authors whereof, or those who exhibit them, frequently take the liberty to report, and even to certify in the public news-papers, that they have met with the highest applatse and approbation. And therefore it is hoped, that no regard will hereafter be paid to fuch reports, and public notices; which in fome instances have been too lightly credited, to the dishonour of the Society.



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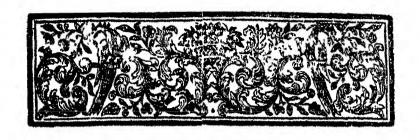
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THE President and Council of the Royal Society adjudged, for the Year 1785, the Medal on Sir Godfrey Copley's Donation, to Major-General William Roy, for his Meafurement of a Base on Hounslow-Heath.



### PHILOSOPHICAL

# TRANSACTIONS

I. Observations on the Graduation of Astronomical Instruments; with an Explanation of the Method invented by the late Mr. Henry Hindley, of York, Clock-maker, to divide Circles into any given Number of Parts. By Mr. John Smeaton, F.R.S.; communicated by Henry Cavendish, Esq. F.R.S. and S.A.

#### Read November 17, 1785.

PERHAPS no part of the science of Mechanics has been cultivated by the ingenious with more assiduity, or more deservedly so, than the art of dividing Circles for the purpose of Astronomy and Navigation. It is said, that TYCHO BRAHE VOL. LXXVI.

and Hevelius laboured this part of their influments with their own hands; and though public rewards have at length brought forth different methods of dividing from our best artists, which have been communicated to the Public; yet I trust it will be thought, that if any thing relative to this business remains yet behind, that may tend to surnish the ingenious artists, who are cultivating this field, with any new or curious idea upon the subject, it will be well worth communicating to this learned Society: since, if an hint, which is effentially different from any thing that (so far as I know) the Public is in possession of, be once started, and is pursued and worked upon by ingenious men, it is not possible to say, to what valuable purposes it may be converted.

This, perhaps, will better appear by taking a short review of the labours of others, from the time of Tycho BRAHE and Hevelius (who did not use telescopic sights) to the present time.

The very learned, ingenious, and inventive Dr. Hook, in his Animadversions on the Machina Calestis of Hevertus, published in the year 1674, has given us an elaborate description of a quadrant, whose divisions were formed, and afterwards read off, by means of an endless screw, working upon the outermost border of the limb of a quadrant; which, he says, does not at all depend upon the care and diligence of the instrument-maker in dividing, graving, or numbering the divisions, for the same screw makes it from end to end; yet he has given us no account of any particular care or caution that he used, in preventing the same screw from making larger or smaller paces, in consequence of unequal resistance, from a different hardness of the metal in different parts of the limb; nor any method of correcting or checking the same; nor of making a screw, the

angle of whose threads with the axis shall be equal in every part of the circumference; therefore the whole of this bufiness (in which accurate mechanists well know confifts the whole of the difficulty) he refers to the ingenious workman; and, in particular, to the then celebrated Mr. Tompton, whom, he fays, he employed to make his inflrument, and who had thereby feen and experienced the difficulties that do occur therein: but was any ingenious workman now to purfue the directions of Dr. Hook, fo far as his communication thereof extends, we may conclude, that he would make a very inaccurate piece of work, far inferior in performance to what the Doctor feems to expect from it \*. But yet, I believe, it was the first attempt to apply the endless screw and wheel, or arch, to the purpose of forming divitions for astronomical instruments; for, the Doctor fays himfelf, the perfection of this inftrument is the way of making the divisions; that it excels all the common ways of division: and in the table of contents it is intituled, An Explication of the new Way of dividing.

This method, however, of Dr. Hook's was not laid aside without a very sull and sufficient trial: for Mr. Flamsteed, in the *Prolegomena* of the third volume of *Historia Calestis*, informs us, that be contrived the sextant, wherewith his observations were chiefly made, from his entrance into the Royal Observatory in the year 1676 to the year 1689. This sextant was sirst made of wood, and afterwards of iron, with a brass limb of two inches broad, by Mr. Tompion, at the expence of Sir Jonas Moore; the radius thereof was 6 feet 91 inches; it was surnished with an endless screw upon its limb of 17

<sup>\*</sup> This was indeed verified in an attempt upon the same plan by the Duc DE CHAULNES, published in a Memolr of the Royal Academy of Sciences at Paris, for the year 1765.

B 2 threads

4 threads in an inch, and with telefcopic fights'. Or this instrument Mr. FLAMSTEED gives the figure at the latter end of his Prolegomena before-mentioned, fufficiently large to fee the general defign; the whole being mounted upon a fliong polar axis of iron, of three inches diameter.

Though, in the full description of this instrument, Mr. FLAMSTEED mentioned the Limb's being furnished with diagonal divisions, diffinguishing the arch to 10 seconds +; yet it is pretty clear, that it had not these originally upon it; but that the dependance was wholly upon the ferew divisions, when it came out of Mr. Tompion's hands. This one may reasonably infer from the observations themselves; for the first observation, set down as taken with this instrument, being upon the 29th of October, 1676, it was not till the 11th of September, 1677, that the column which contained the check angle by diagonal lines was filled up; and there was also a fpace of time, antecedent to that last mentioned, wherein no observations are recorded as taken with this instrument, in which time the diagonal divitions might be put on; and this will be put beyond a doubt, as he fays expressly, that finding, in the year 1677, that the threads of the ferew had worn the border of the limb, he divided the limb into degrees himfelf, and drew a fet of diagonal divisions ‡; and then comparing the two fets of divisions together, he fometimes found them to differ a whole minute; wherefore, for correction thereof, he constructed a new table for conversion of the revolutions and parts of the screw into degrees, minutes, and seconds; and

<sup>. \* &</sup>quot; - Qualem nemo, colo adhibens;-" Preface to Historia Coelest. printed in one vol. 1712.

Prolegomena Histor. Cœlest. vol. III. p. 104. 1 13d. p. 106. "Giadus in limbo destribui ac diagonales duxi."

which he applied in the observations taken in 1678.—However, notwithstanding this correction, in looking over the observations noted down as deduced each way, I frequently sind a difference of half a minute; not unfrequently 40"; but in an observation of the moon, of the 9th June, 1687, I find a difference of 55"\*, which upon a radius of 6 feet 9 inches amounts to more than the part of an inch.

In the year 1689, Mr. FLAMSTEED compleated his mural are at Greenwich; and, in the Prolegomena before-mentioned, he makes an ample acknowledgement of the particular affiftance, care, and industry of Mr. Abraham Sharp; whom, in the month of August, 1688, he brought into the observatory, as his amanuensis; and being, as Mr. Flamsteed tells us, not only a very skilful mathematician, but exceedingly expert in mechanical operations +, he was principally employed in the construction of the mural arc; which in the compass of sourcem months he finished, so greatly to the satisfaction of Mr Flamsteed, that he speaks of him in the highest terms of praise ‡.

This celebrated Instrument, of which he also gives the figure at the end of the *Prolegomena*, was of the radius of 6 feet 7½ inches; and, in like manner as the fextant, was furnished both

<sup>\*</sup> Vol. I. of Hift. Coleft. p. 343.

<sup>+ &</sup>quot; Qui mechanices perquam expertus, pariter ac mathefeos peritus." Frolegomena, vol. III. p. 108.

<sup>† \*\*</sup> SHARPEXUS fervus meus sidelissimus, ne omnibus quidem dotibus & facul
\*\* tatibus crat imbutus, que ipsum tam subtili & dissicili operi obeundo idoneum

\*\* redderent." Prolegom. ibid.

And on finishing the instrument, he says, "Gradus describuntur sive numerantur et exsculpantur, artificiosa manuali opera dicti domini Suarr, qui limbum

partitus est, diagonales duxit, totumque organum absolvit et persecit: adeo

se se exactius id peragere non potuisse, agnoverint." Prolegom. p. 212.

with ferew and diagonal divisions, all performed by the accurate hand of Mr. Sharp. But yet, whoever compares the different parts of the table for conversion of the revolutions and parts of the screw belonging to the mural arc into degrees minutes and seconds \*, with each other, at the same distance from the zenith on different sides; and with their halves, quarters, &c. will find as notable a disagreement of the screw-work from the hand-divisions, as had appeared before in the work of Mr. Tompion: and hence we may conclude, that the method of Dr. Hook, being executed by two such masterly hands as Tompion and Sharp, and found desective, is in reality not to be depended upon in nice matters.

From the account of Mr. FLAMSTEED it appears also, that Mr. Sharp obtained the zenith point of the instrument, or line of collimation, by observation of the zenith stars, with the face of the instrument on the east and on the west side of the wall +: and that having made the index stronger (to prevent flexure) than that of the sextant, and thereby heavier, he contrived, by means of pullies and balancing weights, to relieve the hand that was to move it from a great part of its gravity +.

I have been the more particular relating to Mr. SHARP, in the business of constructing this mural arc; not only because we may suppose it the first good and valid instrument of the kind, but because I look upon Mr. SHARP to have been the first person that cut accurate and delicate divisions upon astronomical instruments; of which, independent of Mr. FLAMSTEED'S testimony, there still remain considerable proofs: for, after leaving Mr. FLAMSTEED, and quitting the department above-mentioned 1,

<sup>\*</sup> Hist. Coelest. vol. II. Appendix. + Prolegom. p. 109.

The Mr. Sharp continued in first correspondence with Mr. Flamstern & long as he lived, as appeared by letters of Mr. Flamstern's found after Mr. Sharp's deaths many of which I have seen.

he retired into Yorkshire, to the village of Little Horton, near Bradford, where he ended his days about the year 1743; and where I have feen not only a large and very fine collection of mechanical tools (the principal ones being made with his own hands), but also a great variety of scales and instruments made therewith, both in wood and brafs, the divisions whereof were fo exquisite, as would not discredit the first artists of the present times: and I believe there is now remaining a quadrant, of four or five feet radius, framed of wood, but the limb covered with a brafs plate; the fubdivisions being done by diagonals, the lines of which are as finely cut as those upon the quadrants at Greenwich. The delicacy of Mr. SHARP's hand will indeed permanently appear from the copper plates in a quarto book, published in the year 1718, intituled, Geometry improved by A. Sharp, Philomath, whereof not only the geometrical lines upon the plates, but the whole of the engraving of letters and figures, were done by himself, as I was told by a person in the mathematical line, who very frequently attended Mr. SHARP in the latter part of his life. I therefore look upon Mr. Sharp as the first person that brought the affair of hand division to any degree of perfection.

Some time about the establishment of the mural arc at Greenwich, the celebrated Danish Astronomer Olaus Roemer began his domestic Observatory, which he sinished in the year 1715, as we are informed by his historian Peter Florrebow, in the third volume of his works, in the tract, intituled, Basis Astronomia, published in the year 1741. In this tract is the description of an instrument, Tab. III. which not only answered the purpose of the meridian arc; but, its telescope being mounted upon a long axis, became also in reality what we now call a Transit Instrument; and which surnished, so far

as I have been able to learn, the first idea thereof. One end of the axis of this instrument being the center of the meridian arc, and carrying its index, M. Roemer thereby avoided the errors arising from the plane of the mural arc not being accurately a vertical plane; and which Mr. Flamstern endeavoured to check, by observing the passage of known stars nearly in the same parallel of declination; that is, passing nearly over the same part of the plane of the arc; by which he was enabled to correct or check the errors of the arc in right ascension. But it is the peculiar method in which Roemer divided his instruments, that occasions him here to be introduced.

Though it is a very simple problem by which geometricians teach how to divide a given right line into any number of parts required; yet it is still a much more simple thing to set off upon a given right line, from a point given, any number of equal parts required, where the total length is not exactly limited; for this amounts to nothing more than assuming a convenient opening of the compasses, and beginning at the point given, to set off the opening of the compasses as many times in succession, as there are equal parts required; which process is as applicable to the arch of a circle as it is to a right line. Of this simple principle Roemer endeavoured to avail himself.

For this purpose M. Roemer took two stiff, but very fine-pointed, pieces of steel, and fixed them together, so as to avoid, as much as possible, every degree of spring that would necessarily attend long-legged compasses, or even those of the shortest and stiffest kind when the points are brought near together. The distance of the points that he chose was about the to or to of an inch. This, upon a radius of 21 or three feet, would be about 10 minutes. With this opening, beginning

at the point given, he fet off equal spaces in succession to the end of his arch, which was about 75°. Those were distinguished upon the limb of the instrument by very sine points, which were referred to by a grosser division, the whole being properly numbered. The subdivision of those arches of 10 minutes each was performed by a double microscope, carried upon the arm or radius of the instrument, the common socus being surnished with parallel threads of single silk, whereof eleven being disposed at ten equal intervals, comprehending together one ten-minute division, the distance of the nearest threads became a very visible space, answerable to one minute each, and therefore capable of a much surther subdivision by estimation.

The divitions of this inftrument were therefore, properly speaking, not degrees and minutes; but yet, if exactly equal, would serve the purpose as well, when their true value was found, which was done by comparison with larger instruments.

Now, if it be considered, that in going step by step of ten minutes each, through a space of 75 degrees, there will be a succession of 450 divisions, dependant upon each other; if it be also considered, that the least degree of extuberance in the surface of the metal, where each new point is set down, or the least hard particle (wherewith all the base metals seem to abound) will cause a deviation in the first impression of a tapes point, and thereby produce an inequality in the division; it is evident, that though this inequality may be very small, and even imperceptible between neighbouring divisions, yet among distant ones, it may and will arise to something considerable; which, in the mensuration of angles, will have the same ill tendency as in near ones. Now, as M. Roemer has given us no Vol. LXXVI.

means of checking the distant divisions, in respect of each other, it is very probable that no one has followed his steps, in cases where great accuracy was required, in a confiderable number of divitions. For in reality this method is likely to fall far short of Dr. Hook's; as Dr. Hook's divitions being cut in a fimilar successive manner, by the rotation of the sharp edge of the threads of a ferew against the exterior edge of the limb of the instrument, a very slight degree of pressure will bring a fine ferew of thirty threads in an inch (which he preferibes) to touch against an arch whose radius is four or five feet in more than one, two, three, or four threads at once; fo that the threads supporting one another, a small extuberance, or even a fmall hard particle in the metal, will be cut through or removed by the grinding or rather fawing motion of the ferew; and which, in regard to its contact, being in reality an edge, will be much more effectual (that is, more firm) in its retention than a mere simple point: and a repetition of the operation, from the support of the threads to each other, will tend to mend the first traces; whereas, in ROEMER's way, a repetition will make them worfe; for, whatever drove forward or backward the point on first entering, will, from the sloping of the point, be confirmed and increased in driving it deeper.

When Dr. HALLEY was chosen Astronomer Royal (Mr. FLAMSTEED's instruments being taken away by his executors), Mr. GRAHAM undertook to make a new mural quadrant, about the weat 1725; who, uniting all that appeared valuable in the different methods of his predecessors, executed it with a degree of contrivance, accuracy, and precision, before unknown: and the division thereof he performed with his own hand. The model of this quadrant, for strength, easy management, and the model of this predecessors with the most perfect. What

What I apprehend to be peculiar in it, was the application of the arch of 96°; not only as a check upon the arc of degrees and minutes, but as superior thereto, being derived from the more simple principle of continual bisection.

To make room for this, he has entirely rejected the subdivision by diagonals, and has adopted the method of the Vernier; but the fubdivition of the vernier divitions he, as I apprehend for the first time, measured by the turns of the detached adjusting forew, making it in fact a micrometer, by which the diffance of the fet of the instrument was to be measured from the perfect coincidence of one of the actual divisions of the limb with the next stroke of the vernier; by which means the obfervation could not only be read off with all the precision that the division of the instrument was capable of, but the two sets of divisions could be checked and compared with each other. Another thing that I apprehend to be peculiar in this instrument, was the more certain method of transferring and cutting the divisions, from the original divided points, by means of the beam-compass, than could possibly be done from a fiducial edge, as had doubtless been constantly the practice in cutting diagonals; for, placing the steady point of the beam-compais in the tangent line to that part of the arc where each division was to be cut, the opening of the compass being nearly the length of the tangent, the other point would cut the division in the direction of the radius nearly; and though in reality an arch of a circle, yet the small part of it in use would be so nearly a right line, as perfectly to answer the same end; all which advantages put together, it is probable, induced Mr. GRAHAM to reject the diagonals.

Soon after the completion of this quadrant, Mr. GRAHAM undertook to execute a senith fewer for the Rev. Dr. BRADLEY,

which was fixed up at Wanstead, in Essex, in the year 1727. The very simple construction that he adopted for this instrument (the plumb line itself being the index) did not admit of the use of a vernier: he therefore contented himself with dividing the arch of the limb of this instrument by primary points, as close as he thought necessary, that is, by divisions of five minutes each, and measuring the distance from the set of the instrument to the next point of division by a micrometer screw, in the construction of which screw he used uncommon care and delicacy. I have mentioned this instrument to introduce this observation; that I think it highly probable, had Mr. Graham constructed the great quadrant after the zenith sector had been fully tried, he would have rejected not only the diagonals but the verniers also, as containing a source of error within themselves which may be avoided by a well-made screw\*.

It seems also, that Mr. GRAHAM, at the time he constructed both these instruments, was not aware how much error
could arise from the unequal expansions of different metals by
heat or cold: for in both the radius, or frame of the instrument, was iron, while the limbs were of brass. They, however, remain in the Royal Observatory, perfect models, in all
other respects, of every thing that is likely to be attained in
their respective destinations, and monuments of the superlative abilities of that great mechanician Mr. Graham +.

<sup>\*</sup> This has been found consentaneous to the experience of my friend Mr. Aubra, who, on my suggestion, has long since laid aside the use of his vernier, measuring always by the micrometer screws the distance between the set of the instrument, and the coincidence of the first stroke of the vernier with the next primary division of the limb.

I have been informed, that Dr. MASKELTER has caused this objection to the finitest be rectified, since its removal to the Royal Observatory, by subdicteting an instead of that of brass, the points being made upon study of gold.

Mr. GRAHAM lived till the year 1751; and during his time there were few inflruments of confequence conftructed without his advice and opinion. They were for many years done by Mr. Sisson, to whom doubtless Mr. Graham would fully communicate his method of division; and from this school arose that very eminent and accurate artist Mr. Bird, whose delicate hand, joined with great care and affiduity, enabled him still further to promote this branch of division; and which being carried by him to a great pitch of perfection, the Commissioners of Longitude did themselves the credit, by an handfome reward, to induce him to publish to the world his particular method of dividing astronomical instruments; which being drawn up by himself, in the year 1767, this matter is fully fet forth to the public: I shall therefore only take this opportunity of observing, that there seems to be one article in which Mr. BIRD's method may be still improved.

I must here observe, that I apprehend no quadrant, that has ever undergone a severe examination, has been found to form a perfect arch of 90°; nor is it at all necessary it should: the perfect equality of the divisions throughout the whole is the first and primary consideration; as the proportion of error, when ascertained by proper observations, can be as easily and readily applied, when the whole error of the rectangle is sisteen seconds, as when it is but five.

In this view, from the radius taken, I would compute the chord of fixteen degrees only. If I had an excellent plain scale, I would use it; because I should expect the deviation from the right angle to be less than if taken from a scale of more moderate accuracy; but if not, the equality of the divisions would not be affected, though taken from any common diagonal scale. This chord, so prepared, I would lay off five times, in succession, from the

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the primary point of o given, which would compleat eight degrees; I would then bifect each of those arches of 16°, as prescribed by Mr. Bird, and laying off one of them beyond the 80th, would give the 88th degree: proceeding then by bifection, till I came to an arch of two degrees, laying that off from the 88th degree, would give the point of ninety degrees. Proceeding still by bifection, till I had reduced the degrees into quarters = fifteen minutes each, I would there ftop; as from experience I know, that when divisions are over close, the accuracy of them, even by bifection, cannot be so well attained as where they are moderately large. If a space of + of an inch. which is a quarter of a degree, upon an eight-feet radius, is thought too large an interval to draw the index over by the micrometer fcrew, this may be shortened by placing another line at the distance of one-third of a division on each side of the index line, in which case the screw will never have to move the index plate more than one-third of a division, or five minutes; and the perfect equality of those side lines from the index line may be obtained, and adjusted to five minutes precisely, by putting each of the fide lines upon a little plate, capable of adjustment to its true distance from the middle one, by an adjusting fcrew.

The above hint is not confined to the chord of fixteen degrees, which prohibits the subdivisions going lower than fifteen minutes: for if it be required to have divisions equivalent to five minutes upon the limb itself; then I would compute the chord of 21° 20′ only; and laying it off four times from the primary point, the last would mark out the division 85° 20′, pointed out by Mr. Brad; supplying the remainder to a quadrant, from the bisected divisions as they arise, and not by the application of the temputed chords.

In my Introduction to M. ROEMER's Method of Division, I have shown, that divisions laid off in succession, by the same opening of the compasses, either in a right line, or in the arch. of a circle, being in its idea geometrically true, and in itself the most simple of all processes, it has the fairest chance of being mechanically and practically exact, when cleared of the difturbing causes. The objection therefore to his method is, the great. number of repetitions, which depending upon each other in fuccession (requiring no less than 540 to a quadrant, when subdivided to ten minutes each), the finallest error in each, repeated 540 times, without any thing to check it by the way, may arise to a very fentible and large amount: but in the method I have hinted, this objection will not lie; for, in the first case, the affumed opening is laid off but five times; and in the latter cafe but four times; nor does this repetition arise out of the nature of the thing; for, if you like it better, you may, in the former case,, at once compute the chord of 64°; and in the latter that of 85° 20', and then proceed wholly by bifection; supplying what is wanted to make up the quadrant, from the bifected divisions, as they arise. Mr. BIRD prescribes this method himself, for the division of HADLEY's sextants and octants.

He, I suppose, was the first, who conceived the idea of laying off chords of arches, whose subdivisions should be come at by continual bisection; but why he mixed therewith divisions that were derived from a different origin (as prescribed in his method of dividing) I do not easily conceive. He says, that after he had proceeded by the bisections, from the arc of 85° 20′, the several points of 30°, 60°, 75°, and 90°, (all of which were laid down from the principle of the chord of 60° being equal to radius), sell in without sensible inequality; and so indeed they might; but yet it does not follow that they were equally true in these places

as if they had been (like the rest) laid down from the bisection from 85° 20', and therefore being the first made, whatever error was in them, would be communicated to all connected with them, or taking their departure from them. Every heterogeneous mixture should be avoided where equal divisions are required. It is not the fame thing (as every good artist will see) whether you twice take a measure from a scale as nearly the same as you can, and lay them off separately; or lay off two openings of the compasses, in succession, unaltered; for though the same opening, carefully taken off from the fame scale a second time, will doubtless fall into the points made by the first, without sensible error; yet as the sloping sides of the conical cavities made by the first point will conduct the points themselves to the conter, there may be an error which, though insensible to the sight, would have been avoided by the more simple process of laying off the opening twice, without ever altering the compasses.

The 96 arc was, I have no doubt, invented by Mr. GRA-HAM, from having perceived, in common with all preceding artists, how very much more easy a given line was to bisect, than to trifect, or quinquesect; and therefore the 96 arc which proceeded by bifections only (or by laying off the fame identical openings, which, as already shewn, is still more simple and unexceptionable) was wholly intended by him by way of checking the division of the arc of 90, which required trifections and quinquefections. But experience foon shewed the superior advantage of it so strongly, that the use of the 90 arc is now wholly fet aside, where accuracy is required; whereas the ingenuity of Mr. BIRD having shewn a way to produce the on arc by bisection, when this is really pursued quite through the piece, by rejecting all divisions derived from any other origin, the 90 arc will have nothing in it to prevent its being equally

equally unexceptionable with the 96 arc; and consequently if, instead of the 96 arc, another arc of 90 was laid down (which being upon a different radius, its divisions will stand totally unconnected with the former), then these two arcs would in reality be a check upon each other; for being of equal validity, the mean might be taken: and if (in lieu of vernier divisions) strokes at the distance of any odd number, as 7, 9, 11, or 13, are marked upon, and carried along with, the index plate; these will produce a check upon neighbouring divisions; and the angle may then be deduced from the medium of no less than four readings.

The last works that have been made known to the public in the line of graduation (so far as has come to my knowledge) are those of the very ingenious Mr. RAMSDEN, which were published, by order of the Board of Longitude, in the year 1777.

From his own information, I learn, that in the year 1760 he turned his thoughts towards making an engine for dividing mathematical instruments; and this he did in consequence of a reward offered by the Board of Longitude to Mr. BIRD, for publishing his method of graduating quadrants; for as, several years previous to that period, he had taken great pains to accomplish himself in the art of hand-dividing, in which line Mr. Bird had acquired his eminence, he conceived by this publication of Mr. BIRD's he should be reduced to the same standard of performance with the rest of the trade. He, therefore, partly to fave time, and that kind of weariness to an ingenious mind that ever must attent the endless repetition of the same thing from morning to night; partly still to preserve the pre-eminence he had then gained; and partly to procure dispatch in the great increase of demand for HADLEY's sextants and octante, incomsequence of the fuccelsful application of the mean's the the purpole 'Vol. LXXVI. D

purpose of ascertaining the longitude at sea (which instruments for this purpose required a degree of accuracy and certainty in the division, by no means necessary thereto when applied to the simple purpose of observing latitudes); I say, for these considerations, Mr. Ramsden determined to set about something in the instrumental way, that should be sufficient effectually to answer these purposes.

Accordingly, confidering the nature of the endless screw, he for this felf to work upon an engine whose divided wheel or plate was of thirty inches diameter; and though the performance of this first essay was inferior to his expectations and wishes, yet with it he was able to divide theodolites with a degree of precision far superior to any thing of the kind that had been exhibited to the public.

This engine I myfelf faw in the spring of the year 1768; and it appeared to me not only a very laudable attempt towards instrumental divisions, but a very good model for the construction of an engine of the most accurate kind for that purpose. And he furthermore, at the same time, shewed me the model or pattern for casting a wheel of a much larger size, which he proposed to make upon the same plan, and with considerable improvements. This being effected fome time in or about the year 1774, its accuracy was proved by making a fextant, afterwards subjected to the examination of Mr. BIRD; who in consequence approved the method, not only as fully fufficient for the divition of HADLEY's fextants and octants for any purpose whatfoever, but in fact for dividing any inftrument whose radius did not exceed that of the dividing wheel, which was forty-five inches in diameter: whereupon the Board of Longitude, ever ready to encourage all endeavours that tend to the certainty and perfection of any thing subservient to the purpose of finding the longitude at fea, very properly and usefully resolved to confer

an handsome reward on Mr. RAMEDEN, for delivering a full explanation of his method of making the said engine; which, in consequence, was published by order of the Board of Longitude in the year already mentioned, viz. 1777: the designs whereof are so full and explicit, that whoever could not understand that description, so as to enable him to make it, would be smfit to undertake it on other accounts.

From what I have faid upon the works of the different artiffs that I have mentioned, it would feem that the art of graduation was brought to that degree of perfection, that nothing material can now be added thereto: and I should have been apt to have thought so myself, if I had not happened, in the course of my life, to have had a communication made to me (under the seal of secrecy) which seems to promise yet further light and assistance in perfecting that important art; and every impediment to the discovery thereof being now removed, I shall in the remainder of this essay give the clearest description thereof that I am able, with such clucidations and improvements as seem to be naturally pointed out by the method itself.

In the autumn of the year 1741, I was first introduced to the acquaintance of that then eminent artist, Mr. Henry Hindley, of York, clockmaker;—he immediately entered with me into the greatest freedom of communication, which founded a friendship that lasted to his death, which did not happen till the year 1771, at the age of 70. On the first interview, he shewed me not only his general set of tools, but his engine, at that time furnished with a dividing plate, with a great variety of numbers for cutting the teeth of clock wheels, &c. and also, for more nice and curious purposes, furnished with a wheel of about thirteen inches diameter, very stout and strong, and cut into 360 teeth; so which was applied an endless screw, adapted thereto. The

threads of this ferew were not formed upon a cylindric furface, but upon a folid whose sides were terminated by arches of circles. The whole length contained sifteen threads; and as every thread (on the side next the wheel) pointed towards the center thereof, the whole sifteen were in contact together; and had been so ground with the wheel, that, to my great astonishment, I found the screw would turn round with the utmost freedom, interlocked with the teeth of the wheel, and would draw the wheel round without any shake or sticking, or the least sensation of inequality.

How long this engine might have been made before this first interview, I cannot now exactly ascertain: I believe not more than about a couple of years; but this I well remember, that he then shewed me an instrument intended for astronomical purposes, which must have been produced from the engine, and which of itself must have taken some time in making \*.

I in

. \* This inftrument was of the equatorial kind; the wheel parallel to the equator, the quadrant of latitude, and femi-circle of declination, being all furnished with screws containing sisteen threads each, framed and moved in the fame manner as that of the engine; the whole of which infirmment was already framed, and the telescope tube in its place, which was intended to be of the inverting refracting kind, and to be furnished with a micrometer. This, however, was not complexed till some years after; but, in the year 1748, I received it in London for fale. It staid with me two years, in which time I shewed it to all my mechanical and philosophical friends, amongst whom was Mr. Shoar, who afterwards published in the Philosophical Transactions, vol. XLVI. No 493. p. 241. un Account of a portable Observatory, but without claiming any particular menit from the contrivance. Mowever, the model of it differs from Handley's equatorial only in the following articles. He added an azimuth circle and compais at the He omitted the endless screws, placing verniers in their stead; and at the top, a reflecting telescope instead of a refractor. This infrument of HINDuntil thing afterwards returned to him unfold, I pointed out the principal deficienchis that I found therein; viz. that, in putting the inftrument into different politions,

I in reality thought myself much indebted to Mr. HINDLEY for this communication; but though he shewed me his engine, and told me, that the fcrew was cut by the rotation of the point of a tool, carried round upon a strong arm, at the diftance of the radius of the wheel from the center of motion, which arm was carried forward by the wheel itself, and the wheel was put forward by an endlers force, formed upon a cylinder to a proper fize of thread, cut by his chock lathe; though he shewed me also this chock lathe, and the method employed to make the threads of the screw equiangular with the axis, that is, to free the ferew from what workmen term drunkenness; and also showed me how, by the single screw of his lathe, he could cut, by means of wheel-work, fcrews of every necessary degree of fineness \* (and, by taking out a wheel, could cut a left-handed fcrew of the very fame degree of fineness); by which means he was enabled not only to adapt his plain fcrew to the fize of the teeth of his wheel, but also to prevent any drunkenness that otherwise the curved screw would. be subject to in consequence of being produced from the plain

tions, the springing of the materials was such as in some positions to amount to considerable errors. This remained with him in the same slate till the year of the first Transit of Ferms, viz. 1761; when it was sold to \_\_\_\_\_\_ Constable, Rsq. of Burton Constable, in Haldsrags. Mr. Issually, to remedy the evil above-mentioned, applied balances to the different movements. He soon afterwards completed one, de novo, upon this improved plan, for his Grace the late Duke of Norfolk. A method of balancing in much the same way, without the knowledge that it had been done before, has been fully explained, and laid before the Society, by our ingenious and wonthy brother Mr. Narane. Phil. Transvol. LXI. p. 108.

\* A machine for cutting the endless forew of Mr. Ramsden's engine, upon principles exactly similar, is fully and accurately set forth in his Description of his dividing Engine above-mentioned.

one; furthermore, that the screw and wheel, being ground together as an optic glass to its tool, produced that degree of smoothness in its motion that I observed; and, lastly, that the wheel was cut from the dividing plate: yet, how the dividing plate was produced, he for particular reasons reserved to himself.

Nor can he be blamed for the refervation of this one secret: as he had, even at the time of my early acquaintance with him, a kind of forelight that from the superior merit of HAD-LEY's quadrant, a demand for that, and other instruments for the purpose of navigation, was likely to increase; and that he might live to fee a public reward offered for a method of dividing them with greater accuracy and dispatch than had at that time appeared. Indeed, he had himself an idea, from the fatisfactory fuccess that had attended his operations in dividing, that a fcrew and wheel, produced from his engines of one foot diameter, would have as much truth as the eight-feet quadrant at Greenwich: and though he doubtless greatly overrated the accuracy of these miniature performances, yet it does not follow, as his methods were not confined to fo narrow a compass, but that, his scale of operation being proportionably enlarged, a degree of accuracy in the graduation of astronomical inftruments may be attained in proportion.

I must here beg leave to observe, that there appears to me to be a natural limitation to the accuracy of instruments, consisting of considerable portions of a circle, such as quadrants, &c. \*. I do not find that the finest stroke upon the limb of a quadrant, made by BIRD's own hand, if removed from its

<sup>\*</sup> The zenith sector consists but of few degrees, with little variation of its position in using it.

coincidence with its index, can be replaced with any degree of sertainty nearer than the 4000dth part of an inch, though aided by a magnifying glass \*.

A 4000dth part of an inch being then determined to be the minimum visibile by the strokes of an instrument, this will be less than one second of a degree upon a radius of four feet; and therefore, if the whole fet of divisions upon the limb could be preserved true to this aliquot part of an inch, the eight-feet quadrants of Greenwich might be expected to be true to half a fecond. How far they are from this, I do not exactly know; but I have reason to think they vary from it some seconds: nay, I believe it is generally allowed, that our largest quadrants, even when executed by the accurate hand of Mr. BIRD, do not exceed those of a less size, by the same hand, in proportion to their increase of radius: nor can it well be expected that they should; since, as the weight necessarily increases in a triplicate ratio of the radius, the great weight of the Greenwich quadrants in moving and fixing them (as they could not be divided in their place) may eafily derange the framing; or even the internal elasticity of the materials may give way, by a change of polition, to fo minute a quantity as a 4000dth part of an inch. It therefore appears to me, that fince the divisions of a quadrant of four-feet radius are more than fufficient, and even those of three feet admit of all the distinctness that in other respects is wanted, a three-feet quadrant, in point of

It will be to little purpose to attempt it with a greater power. Double microscopes can doubtless be formed to magnify objects, far less than a 4000dth part of an inch, to distinct surfaces; but then the advantage of such degrees of magnifying power is chiefly upon the organized bodies of nature. Let a dot, or the finest point that can be made by human art, be so viewed, and it will appear not round, but a very ragged irregular figure.

fize, is capable of all attainable exactness; and would be as much to be depended on as any of those now in being of eight feet. By adopting quadrants of this smaller fize, we shall of course get rid of ist the present weight; and consequently of much cumber, unhandiness, and derangement, that must arise from that weight, as well as the fear of totally discomposing them, if ever moved out of their place.

It now comes to be time to open a principle upon which there is a prospect of effecting such an improvement. I have shewn that a 40coth part of 'an inch is the ultimatum that we are to expect from fight, though aided by glasses, when observing the divisions of an instrument. But in the XLVIIIth, volume of the Philosophical Transactions for the year 1754, I have shewn the mechanism of a new pyrometer, and experiments made therewith; whereby it appears, that, upon the principle of contact, a 24,000th part of an inch is a very definite quantity. I remembered very well that I did not then go to the extent of what I might have afforted, being willing to keep within the bounds of credibility: but on occasion of the present subject. I have reexamined this inftrument, and find myself very well authorised to fay, that a 60,000th part of an inch, with fuch an instrument, is a more definite and certain quantity than a 4000th part of an inch is to the fight, conditioned as above specified. The certainty of contact is, therefore, fifteen times greater than that of vision, when applied to the divisions of an instrument; and if this principle of certainty in contact did not take place even much beyond the limit I have now affigned, we never should have seen those exquisite mirrors for reflecting telescopes, that have already been produced.

These reflections apply immediately to my present subject, as HINDLEY's method of division proceeds wholly by contact, and that

that of the firmest kind; there being scarcely need of magnifying glasses in any part of the operation.

In the year 1748 I came to fettle in London; and the first employment I met with was that of making philosophical instruments and apparatus. In this situation, my friend HINDLEY, from a principle the reverse of jealousy, fully communicated to me, by letter, his method of division; and though I was enjoined secrecy respecting others (for the reasons already mentioned), yet the communication was expressly made with an intention that I might apply it to my own purposes.

The following are extracts from two letters, which contain the whole of what related to this subject; and since I have many things to observe thereon, so that the paraphrase would be much greater than the text, I think it best not to interrupt the description with any commentary, as perhaps his own mode of expression will more briefly and happily convey the general idea of the work than any I can use instead of it.

#### My DEAR FRIEND,

York, 14 Nov. 1748.

AS to what you was mentioning about my brother's knowing how I divided my engine place, I will describe it as well as I can myself; but you will want a good many things to go through with it.

The manner is this: first chuse the largest number you want, and then chuse a long plate of thin brass; mine was about one inch in breadth, and eight feet in length, which I bent like an hoop for an hogshead, and soldered the ends together; and turned it of equal thickness, upon a block of smooth-grained wood, upon my great lathe in the air (that is, upon the end of the mandrel): one side of the hoop must be rather wider than Vol. LXXVI.

the other, that it may fit the better to the block, which will be a short piece of a cone of a large diameter: when the hoop was turned, I took it off, cut, and opened it straight again.



The next step was to have a piece of steel bended into the form as per margin \*; which had two small holes bored in it, of equal bigness, one to receive a small pin, and the other a drill of equal size. I ground the holes after they were hardened, to make them round and smooth. The chaps formed by this steel plate were as near together as just to let the long plate through. Being open at one end, the chaps so formed would spring a little, and would press the long plate close, by setting in the vise. Then I put the long

plate to a right angle to the length of the steel chaps, and bored one hole through the long plate, into which I put the small pin; then bored through the other hole; and by moving the steel chaps a hole forward, and putting in the pin in the last hole, I proceeded till I had divided the whole length of the plate.

The next thing was to make this into a circle again. After the plate was cut off at the end of the intended number, I then proceeded to join the ends, which I did thus: I bored two narrow short brass plates + as I did the long one, and put one on the inside, and the other on the outside of the hoop, whose ends were brought together; and put two or three turned screw pins, with flat heads and nuts to them, into each end, which held them together till I rivetted two little plates, one on each side of the narrow plate, on the outside of the hoop. Then I took out the screws, and turned my block down, till the hoop

The figure is confiderably less than the real tool should be.

<sup>†</sup> These I shall hereaster distinguish by the name of saddle-plates.

would fit close on; and by that means my right line was made into an equal divided circle of what number I pleased.

The engine plate was fixed on the face of the block, with a ffeel hole fixed before it, to bore through; and I had a point that would fall into the holes of the divided hoop; so by cutting shorter, and turning the block less, I got all the numbers on my plate.

I need not tell you, that you get as many prime numbers as you please; nor that the distance of the holes in the steel chaps must be proportioned to the length of the hoop.

You may ask my brother what he knows about my method of dividing; but need not tell him what I have said about it; for I think neither he nor John Smith know so much as I have told you, though I believe they got some knowledge of it in general terms \*.——I desire you to keep the method of dividing to yourself, and conclude with my best wishes,

and am, dear Sir, yours, &c.

HEN. HINDLEY.

Though the above letter was in itself very clear and explicit, as to the general traces of the method, yet some doubts occurring to me, a further explanation became necessary. A copy of my letter not being preserved, the purport of it may be inferred from the answer, which was as follows:

\* The persons here referred to were both bred with him. His brother, Mr. ROGER HINDLEY, who has many years followed the ingenious profession of a watch-cap-maker in London, was so much younger as to be an apprentice to him. Mr. JOHN SMITH, now dead, had some years past the honour to work in the instrument way, under the direction of the late Dr. Demaineray, for his present Majesty.

DEAR FRIEND,

York, 13 March, 1748-9.

I THINK in your last you feem to be apprehensive of some difficulties in drilling the hoop for dividing: First, that the center of the hole in the hoop might not be precifely in the center of the hole of the steel chaps, it was drilled in; but if I described fully to you the method I used, I can see no danger of error there: for my chaps were very thick, and the two corresponding holes were a little conical, and ground with a steel pin; first one pair, and then the other, alternately, till the pin would go the same depth into each. Then for drilling the hoop, I took any common drill that would pass through, and bore the hole. After that I took a five-fided broach, which opened the hole in the brafs betwixt the freel chaps, but would not touch the steel; so consequently the center of the holes in the brafs must be concentric with the holes in the chaps: and for alterations by air, heat, cold, &cc. I was not above two or three hours in drilling a row of holes, as far as I remember.

adly, For drilling, in a right line, I had a thin brass plate, fastened between the steel chaps, for the edge of the hoop to bear against, whilst I thrust it forward from hole to hole. What you propose of an iron frame with a lead outside, will be better than my wooden block; but considering the little time that past, betwixt transferring the divisions of the hoop to the divisions of my dividing plate, I did not suffer much that way. It was when I drilled the holes in my dividing plate that I used a frame for drilling, which had one part of it that had a steel hole, that in lying upon the plane of the dividing plate was fixed fast in its place for the point of the drill to pass through: then, at the length of the drill, there was another piece of the.

steel, with a hole in it, to receive the other end of the drill to keep it at right-angles to the plane of the plate. This piece was a spring, which bended at the end, where it was sastened to the frame of the lathe, at about eighteen inches from the end of the drill; so it pushed the drill through with any given force the drill would bear: and though that end of the drill moved in the arch of a circle, it was a very small part of it, being no more than equal to the thickness of the dividing plate.

My good wishes conclude me yours,

HEN. HINDLEY.

Whoever attentively considers the communication contained in the above letters will see, that more happy expedients could not have been devised to procure a set of divisions, where there should be the most exact equality among neighbours; and which, for the purposes of clock-making, is the principal thing to be wished for. But herein, as in M. Roemen's method, there were no means of checking the distant divisions, which run on to 360: now such a check, when the expansion of metals is considered, and particularly the difference of expansion between brass and steel, seems absolutely necessary for the purpose of divisions upon instruments, where the accurate mensuration of large angles is required, as much as the equality of neighbouring divisions.

With this view the invention of this ingenious person suggested to him the thought of making his curved screw to lay

fugurated, that the difference for expansion between the steel chaps and the difference for expansion between the steel chaps and the difference for expansion between the steel chaps and the difference hope for break also, with hard steel hope for separately the chaps for break also, with hard steel hope for feparately the chaps for break also, with hard steel hope for feparately the chaps for break also, with hard steel hope for feparately the chaps of break also, with hard steel hope for feparately the chaps of break also in the fermion of the chaps and the chaps of break also in the feparately the chaps of the chaps of

hold of fifteen teeth or degrees together: this, in effect, becomes a pair of compasses, 24 removes of which complete the whole circle, and produce 24 checks in the circumference: and whoever considers the very exquisite degree of truth that results from the grinding of surfaces in contact, as already noticed, must expect a very great degree of rectification of whatever errors might subsist in the wheel after its first cutting.

What degree of truth it might in reality be capable of upon its first production and adjustment, is not now to be ascertained, he never having used it for the graduation of any capital instrument. Those that he made with a view to an accurate measure of angles, he always made with a screw and wheel, or parts of circles cut by his engine into teeth, and ground together as before-mentioned; but I have reason to think, that its performance, if put to a strict test, was never capable of that accuracy that he himself supposed it to have.

The method itself, however, from its simplicity, and ease of execution, seems to me to be a soundation for every thing that can be expected in truth of graduation; and in consequence for reducing instruments to the least size that is capable of bringing out all that can be expected from the largest; when it shall, like manual division, have received those advantages that the joint labours of the most ingenious men can bestow upon it. That I may not appear to be without grounds for my expectations, I will beg leave to propose, what near factly years occasional contemplation has suggested to me on the subject; and as I can describe the process I would pursue, where different from Hindley's, in sewer words than I could make out a regular criticism upon his letters, I will immediately proceed to the description of it.

# Proposed Improvements of HINDLEY's Method.

I would recommend the number of parts into which the circle is to be reduced to be 1440; that is 4 times 360; which divisions will therefore be quarters of a degree; the distances of the holes in the chaps will therefore, to a three-feet radius, be 1570 of an inch nearly; that is, between the one-sixth and one-seventh of an inch distance center and center.

Having provided myself with a stout mandrel, or arbor, for a chock Lashe, properly framed, that would turn a circle of six seet diameter, I would prepare a chock, or platform, for the end of it, of that diameter, or a little more, composed of clean-grained mahogany plank, all cut out of the same log; which, when sinished, to be about 1½ inch thick, and formed in sectors of circles, suppose 16 to make the circle; the middle line of each sector lying in the direction of the grain of the wood, this will consequently every where point outward: the method of framing this kind of work is well known.

The way of getting a flip of brass to answer the circumference of this platform is suggested in Mr. Bird's Account of constructing Mural Quadrants. Let a parallelogram of brass of about three seet long, and of a competent substance (suppose half an inch ) to make it when finished about one-twentieth of an inch in thickness, be cast of the finest brass; and this to be rolled down will it becomes of sufficient length, for the hoop, and about one-fifth part, more. I would then cut off, from the whole length, somewhat better than one-first part, the whole being sufficiently reduced to a thinkness part. The whole being sufficiently reduced to a thinkness part.

get such a long strip of brass reduced to an equal breadth, than the method prescribed by HINDLEY; viz. by turning it upon the chock prepared; but I would not make it wider on one side than the other, like the hoop of a cask, as he describes, but exactly to sit the chock, when truly cylindric; for the internal elasticity of the brass, in so great a length, will be very sufficient for sitting it on tight enough, without any tapering. This I will now suppose done; and a pair of steel chaps, as described by HINDLEY, to be also prepared, and ready for grinding; which, by such a careful admeasurement as can easily be made, will give the length of the hoop sufficiently near, on its first preparation.

# Method of forming a Pair of Straps as a check to the Divisions.

The part first cut off must be again cut into two equal parts in length; which, for distinction sake, I will call the straps; and which are to serve as checks to every both and every 120th division of the circle.

be wrought to a right line in contiguity to each other; by this means the straight edge of each of the straps will be reduced to the same distance from the steel hole: the hard steel edges may be rectified by the grindstone, if necessary.

This being done, not only the holes in the chaps, but the holes in the two fleel plates, applied to each other, like the two fides of the chaps, must be respectively ground together; not with a taper pin, as prescribed by Hinding; but so as not only to be cylindrical, but that the same cylindrical pin shall equally sit them all, and leave them smooth and polished; which is a process no ways difficult to a curious artist, and of which therefore a minute description is unnecessary.

The chaps being then put upon one of the straps, with its straight edge uppermost, and a pin put through the holes on the left-hand, and through the steel hole in the strap under operation, the chaps must be set upright, so that the line joining the centers of the holes shall be parallel to the upper edge of the strap; the brass plate, mentioned by Hindley, between the chaps, as a guide for directing them always to that upright position, may be then adjusted and fixed to the inside of the chap next the operator \*.

The performance of the enfuing part of this work should be at a season when the temper of the air is not very variable; rather above the mean temper (suppose at 60°) than below it;

<sup>\*</sup> It, would be well, previous to the chilling of the ficel chaps, that another hole was drilled in the chaps, that should be somewhat above the upper edge of the straps, and in the middle betwixt side and side, to receive a steady pix therein, antecedent to drilling the main holes; for then a tempered steel pin, a little taxet, will, by driving it in as far as necessary, constantly answer this purpose strate to last, so as to regulate the holes in grinding, to be truly opposite; proper stoles should also be drilled for fixing the brass guide plate to one of the chaps.

but above all things the artist should be himself cool; that is, not in a state of sensible perspiration; and there should be a free circulation of air in the room. Things being thus conditioned in respect to temperature, he may begin to drill the holes in one of the straps; the pin being first put through the chaps and through the steel hole of the strap; and the next hole, being drilled through the brass with a common drill, that and every hole as it goes is to be finished with a taper broach, as prescribed by HINDLEY; and he may then prove or finish every hole by the application of a thorough broach, made fo full as to require a degree of pressure to force it through; and this broach being a little tempered, and the holes quite hard, there will be no fear of injuring the seel holes \*.

Calling the hole in the steel plates o, and observing the time of beginning, you may proceed to drill 60 holes as prefcribed by HINDLEY; and noting how long you have been about it, you may lay the work aside a length of time, equal to the time you took in drilling; that any addition of warmth it may have acquired in handling or working may be again lost in a great degree +. After this pause you may begin again, and go on to finish 60 holes more; that is, to the length of

The steel holes in the chaps need not to be above one-twentieth of an Inch in dismeter; and though it may be proper to make the fieel plate, of which they formed, one-tenth of an inch thick, in order to give the spring formed holistica them a convenient degree of stiffness, yet they may be reduced (by chamforing the outfides) to half that thickness.

As there is not much occasion for the artist to touch his work, the effects of that may also be very much avoided by wearing thick gloves; and the friction being but flight, and the work almost continually in the vise, the variation of description in the metals concerned cannot be fensible or confiderable,

120 holes from the beginning; you then proceed in the same manner with the other strap.

### Method of drilling the Hoop.

You are now prepared to commence the work upon the long or boop-plate; and you proceed therewith, in forming the first hole with the chaps, as before directed by HINDLEY, and this first hole you call o. You then place the straps one on each fide the hoop, with their gaged edges upward, and put the pin through the holes denominated 60 upon the straps, and through the first hole already made, and denominated o upon the hoop; then, bringing the gaged edges of the fleet plates to be even with the upper or working fide of the hoop, you pinch them together in the vife, and drill and broach the hole through the steel plates, which will make the hole, number 60, upon the hoop. This done, you put the pin through the left-hand hole of the chaps, and the hole marked o upon the hoop-plate first made, and proceed to drill with the chaps to 59 holes inclusive, which will fill up the whole space from o to the 60th division before obtained.

You now again have recourse to the straps, and placing them one on each side the hoop-plate, you put the pin through the 120th hole of the straps, and through the hole marked o upon the hoop-plate; and regulating the steel plates to the hoop-plate as before, you drill and form a hole with the steel plates, which will correspond with the 120th hole upon the hoop-plate; and afterwards filling up the 59 holes wanting by means of the chaps, you then have all completed to the 120th division, which is one-twelfth of the whole circle.

You

You then proceed, in like manner, with another fit of 120 holes; that is, placing the 60th hole of the flrap, to the 120th hole of the hoop-plate, and from it producing the 185th hole; you, in like manner as before, fill up this 60 with the chaps; and afterwards placing the 1 oth hole on the fliaps in the 1 20th hole on the hoop-plate, you will obtain the 240th hole. fo that filling up this last fet of 60 divitions, you have chsained 241 holes, including 240 spaces or divisions of the hoop; and repeating this process ten times more, you will, in like manner, obtain 1441 holes, comprchending 1440 spaces .. And this process being carried on in temperate weather, the mantier of working produces twelve fimilar operations, wherein the materials and tools concerned will not only be fubject to werd' little change of temperature, but that change, whatever it is, will be nearly fimilar in each let of 120 holes. we may therefore infer, that the greatest inequality, or indeed any that can be fenfible, must be at every 60 divisions, that is, between the 50th and 60th, and between the right and 120th, both which will be equally repeated 12 times, in the whole length which is to compose the circumstrence of a Circle. all which will thus be checked thereby 12 times in the circumference, and 12 times more at the intermediate distances; that is, with iz mafter checks, and 12 fubordinate ones, in the whole countd.

"It is proper like to observe, that in M. Rozman's method each fixer soldings could havely be trusted in an affair of great absolutely backetists of the objections blready made, arising stoke the points is but the furface of the brass; but hereits parts probability for exceedingly firm, and the

It will be proper, for realists hereafter to be mentioned, to continue the following to the more, making in the whole 140 r kelds.

operation carried on with fo much power, that any small mequality in the hardness of the brass, or irregularity of surface, cannot be supposed to affect the place of the center of the hole; nor will any small inequality that may be suspected from the wear of the steel holes sensibly affect the center of the hole, to which every thing is ultimately referred.

### Method of joining the Hoop.

A more happy thought than that of HINDLEY's, for joining the two ends of the hoop, could fearcely have been wished for, in regard to preserving the same equality of the space between the holes contiguous to the joint, as in the other parts: for though, geometrically speaking, the two faddle plates, in which the little cylindrical bolts are fixed, for bringing the terminating holes of the hoop plate to their due distance, being one applied within the hoop, and the other without, will belong to circles of different radii; yet this disterence being exceedingly small in such thin metal, and so great a radius, and one being as much too big for the hoop as the other is too little, when the bolts are put in, and the hoop in that part set nearly to a circle by a mould; the mean between them assumed by the hoop, from the elastic compressibility of the materials, will be the truth.

It must, however, be remarked, that in the use of the straps, the joining of the hoop should not be made at any part betwixt an 119th and an 120th division, as some inequality must be supposed there, unless the saddle plates were adapted thereto. The method the most easily practised, will be to continue the division upon the hoop, about twenty more than the completion of the number intended to form the circle, and to cut of sixthe overplus ones at the beginning.

The saddle plates I would recommend to contain ten holes each; so that if the divisions are carried on to twenty more than what will be contained in the circle, there will be a piece containing twenty to cut off; and this again being cut in the middle will afford ten holes to make each saddle plate; so that there will be a place for a bolt on each side the joint, and then putting a bolt through every other hole, there will be three bolts at an end.

The pieces destined for the saddle plates, thus obtained, being broader than can be admitted when put to this use, I would advise to divide the breadth of the plate into three equal parts; and with a cutting hook (which perhaps will be attended with the least violence in the separation) to separate the two outside pieces from the middle piece: by this means the two saddle plates (though double) will occupy one third only of the breadth of the hoop in the middle; and two of the pieces cut off being applied, one on each side of the saddle plate on the outside, will answer in like manner for the rivet plates.

The last operation to compleat the joining of the hoop is the putting on the rivet plates: to compleat this, I would advise a piece of brass, of three or four inches in length, to be filed so as to answer to the inside of the hoop, when reduced to a true circular form; and being three-eighths, or one-half an inch in thickness, to file the opposite side somewhat nearly concentric thereto; apply the middle of its convex arch to the inside of the hoop at the joint, and then bringing on the middle of one of the rivet plates to the joint of the hoop, confine the three together by a comple of narrow-chapped hand vises, leaving a space between them capable of receiving a couple of pins as rivets on each side the joint; the holes for the rivets are then to be their them together them together them together the holes for the rivets are then to be their them.

their entry, into which fmooth taper pins are to be driven; not with violence, but moderately, that no fensible stretching of the folid parts may take place thereby; then cutting off and fmoothing the heads, shift the vises so as to receive another couple of holes, and a third couple in the fame end of the hoop; and proceed progressively in the same manner, from the middle to the other end of the nivet plate; then gently separate the internal brass mould with a thin knife, or such like instrument: and cutting off, and very lightly rivetting the inner ends, proceed to fix the other rivet plate, in the same manner, on the other fide: by this means the hoop will be firmly joined in the very position given it by the faddle plates and mould. These plates may then be removed, the infide of the hoop cleared and fmoothed, if necessary; and the outside will have the middle part clear where the divisions lie, and that without sensible loss or gain in the juncture.

## Method of transferring the Divisions of the Hoop to a dividing Plate.

The hoop being thus refitted for the chock, that should be turned down to leave a shoulder on one side, that the hoop, now reduced to an equal breadth, may be forced against it; and the divisions, being equally distant from one of its edges, will be all found in a circle, as if turned upon it. It should be very carefully sitted to the chock, that it may go on with a sufficients degree of tightness, and without the necessity of much forcing; and it will be no inconvenience now, if it goes on upon a very slight degree of taper of the chock, as the internal spring of the materials will easily accommodate it to this shape will injury to its general truth; a slight degree of a green should be

be turned in the place where the divisions will come, that any conical pin, that is to serve as an index, let drop into the divisions or holes, may not, by reaching through this thin plate, abut upon the wood, rather than upon the sides of the holes: and thus this hoop is made into a which of 1440 equal divisions, moveable round upon its own axis, whereon it was formed.

Against the time that this is compleated, there must be prepaied a flat circular plate or wheel of brafs, the rim of which should be of about 31 inches breadth, and about two-tenths of an inch in thickness when finished, to make a dividing plate; the external diameter of this is to be such, that when laid flat upon the furface of the mahogany platform, its extreme edge will exceed the diameter of the hoop by about half an inch all round. There must also be prepared brass arms (suppose eight in number) of an equal substance with the outer rim, and all connected with a circular plate in the middle; and, the whole of this work being framed beforehand, is to be let on flat upon the mahogany platform; whose face is supposed to be turned truly . flat, and fufficiently affixed with forews: in this fituation, the outward edge is to be turned, and the outward face of the rim turned flat. The center plate, which may be about twelve inches diameter, is also to be turned as flat as possible, and a center hole, of about half an inch diameter, to be very carefully turned Thoroug.

A piece of clean, threight grained, well leafoned mahogany, of about two feet long, three inches thick, and five or fix inches broad, is then to be well affixed to found part of the general frame of the lathe, which much now have its polition altered, so that the firm will become horizontal; and therefore the frame bould be

be originally made with this view \*. The piece of mahogany is to be affixed fo that one of its larger faces shall be in a parallel plane to the face of the platform, and fo low as to clear the under side of the platform in its rotation; and so far distant from the center, that an index may be fixed upon this upper face of the piece of wood, so as conveniently to drop into the holes of the hoop; while the common cutter frame of a clockmaker's engine shall be firmly attached upon the same sace of the wood, and so fixed as to cut the edge of the dividing plate into teeth, answerable to the several divisions of the hoop. The teeth need only to be cut with a common cutter, making a parallel notch: and here it will be proper to observe, that not only both the index and cutter are to be founded on the fame piece or base of wood; but that the nearer they are together, the more free they will be from the effects of all variations of expansions by variations of temperature +.

The equalifing the Teeth of the dividing Plate by grinding.

The object of transferring the divisions of the hoop to the teeth of the dividing plate, is still farther to equalife the teeth by grinding; especially those that, falling within the compass of

\* After changing the position of the lathe, the collar of its mandrel should be removed, and the neck made to move within three planes, so as to preserve an exact center, in the manner of an equal altitude instrument.

† It is proper to observe, that as it may be impracticable to get the rim of the dividing plate cast of the proper size, in one entire piece, it will be very practicable, if cast of a less size (suppose half), but of a sufficient thickness, to roll to down; and by having the outward edge originally thicker than the inner, which proportion of the radii, it may be so managed by the rollers as to be of an about thickness when brought to its proper size. But the arms and contact this mould be of the same metal, rolled in the same degree.

each set of 120 divisions, may be supposed, if any, to be mended thereby; but as it may be incommodious to construct a curved screw, of such a length and size, in HINDLEY's method, as would be sufficient for the purpose, I would propose to use two screws of brass, cut from a cylinder in the way set forth by Mr. Ramsden, each of which, with a very little grinding upon this large circumference, would lay hold of ten or twelve teeth together. I would place the two screws, that is, their middles, to be ninety divisions asunder; of consequence, when one of the screws is between the 59th and the 60th, or between the 19th and 120th division of each set, the other will be in the middle of the space divided by the chaps only \*.

The threads of these screws I would advise to be cut a little taper, so that as they grind in, they may fill the notches of the teeth; which also, by this means, will acquire a little tapering towards their extremities; and by cutting the notches parallel, as I have mentioned, the true ground part will always be certain of being at the extremity.

When the screws have been used in grinding till they are found to have the effect of a perfectly equal and easy rotation all round, and all the teeth reduced to a sensible taper, and regular bearing, I would then totally remove the screws from the square block of wood, upon whose upper face I suppose them to have been mounted; in like manner as I suppose the index and cutting frame to have been removed, to make room for the mounting of

<sup>&</sup>quot;The best way of giving an equal motion to those two screws, seems to be by a detached axis, carrying tare common flat wheels, one acting upon a like flat wheel, upon the axis of one forew, and the other, in the same manner, upon the other; and applying the pulley flat considerating the power to the middle of the detached axis between the two wheels, the spring or twist will be equal both the first of that in turning the contrary was many, they will still be an equal total.

the screws. I now consider the teeth of the dividing plate, so somed, as having all the equality that the present known state of human art has pointed out; and the whole convertible upon the axis or mandrel upon which it has been originally formed, and the central hole of the plate concentric therewith: I therefore consider the ground faces of the teeth of the plate as the actual divisions. It now remains to shew how they are to be transferred, to form the divisions of an instrument.

Preparation of the dividing Plate for graduating Instruments.

If a finall cylinder of hard steel is duly polished, and made of a fize so as just to chock in betwixt the extremities of the teeth. then the center of that cylinder will be a fixed point, in respect to the circumference of the wheel: if another cylinder is applied in like manner, at the distance of a number of divisions (suppole it a prime number, to as to cross all former divisions, wiz. 17 or 19), then the middle of the line joining the centers of the two cylinders will remain in the direction of the fame radius, though one of them should force in a minute quantity further than the other; and if a point is assumed in the direction of a tangent to a circle at this middle-point, then though both the cylinders should drop in a minute quantity further at one time than another, yet the middle-point would remain at the fame distance from the point in the tangent; provided that point was removed to a compotent distance, that is, to five or fix inches. On this principle I would conferud an index, the tun cylinders Thing fixed in a sparme, convertible about the middle point, and re-he contered in the oad of the lever, reprofesting the comment; then state sever being semin convertible about the period the tungers the middle point would always language inflance from Q 2 \* ; \*

Mr. SMEATON'S Observations on the

44 from the point in the tangent, and there hold it steadily fast; the tangent point being placed upon the fixed block beforementioned.

Use of the dividing Plate in the Graduation of Instruments.

Our dividing plate is now ready for the reception of an instrument; suppose it a quadrant, whose radius, however, must not exceed the radius of the dividing plate: It is to be laid upon the face of the dividing plate, and a weight, or weights, equivalent to that of the quadrant, is placed on the opposite side, to balance it. It must also be supposed, that the quadrant is made with a view to be divided by this engine, and consequently, that the central cylinder is so well adapted, and nicely fitted to the center hole of the quadrant, that the center cylinder can be removed, in order for the limb to be divided, and again replaced, without fenfibly altering its center. This being the case, let a piece of metal be turned, to apply to the quadrant, perfectly like its center cylinder at the upper end, and turned nicely to fit the central hole in the dividing plate, at the lower end; then, the quadrant being fixed with proper fastening fcrews, I would cut the divisions with a beam compass; and, if a fixed point is assumed, viz. the center of the tangent point for the index: then the beam compais being always opened to the computed length of the tangent of the circle of divisions, it be sufficiently near for cutting the divisions, square to the circular arches between which they are placed.

It will also be proper (to prevent unequal expansions) that the beam of the compais should be formed of a piece of cleangrained white fir; and that the length between the points he is lefed in a tube of tin or brais; without touching the beam, except at the terminations, which will in a great measure protect it from both alteration of moisture, and of heat from the body of the artist, during the operation.

It will be likewise proper to have a lever, or some equivalent contrivance, to bring the dividing plate forward; that after lifting the little cylinders out of the divisions, and resting them upon the tops of the teeth, they may be brought gently forward with an equal drag, and ultimately snap in between the teeth, by the strength of the spring commanding the index; by this means the drag of the friction of the whole will be constantly the same way.

#### Conclusion.

Now, if, as it has been shewn, a quadrant of any radius may be read off to the 4000dth part of an inch, then this quantity upon a radius of three feet will not be so much as 13 second; and as the whole of the process is carried on by contact, in which a greater error than that of a 60,000dth part of an inch cannot be admitted in any single operation. I should affuredly expect a three-feet quadrant, so divided, to be true in its divisions, and read off to at most two seconds.

But, efter all, in an instrument like this, I should expect the greatest source of error to be in the want of perfect coincidence of the center of the divisions with the actual center upon which the index revolves; and therefore, that if, instead of a quadrant of three-feet radius, a "complete circle of five feet diameter was divided, and its divisions read off from the two opposite points (taking the mean), then the errors of the center will be whally excited. For this reason, in the clearly of opinion, that the fagure proposition of this AMS-DEN.

DEN, to use circles instead of quadrants, or other portions of circles, will bid much the fairest for perfection in actual practice; and that his ingenious method of making them both stiff and light, by the use of hollow conical tubes by way of spokes, in the manner of a common wheel, will enable him to mount them of five feet diameter, upon hollow axes, in the nature of a transit. By this means we shall have all the good properties of both the quadrant and transit united in one instrument; and observations both of right ascension and declination, through the very same telescope, as long since attempted by M. Roemer; and to a degree of perfection and certainty, in point of declination, hitherto unattainable by the largest instruments that have yet been made.

N. B. In matters of very nice determination, small circumstances often come to be of consequence; and it is in this view that I mention what follows. It was a practice of HINDLEY'S of many years standing, and since followed by myself and others, wherever he made any use of the vernier, to key the vernier plate in the same plane, or cylindrical surface continued, whereon the principal divisions are cut. It is of equal utility, though the vernier be rejected, to key the index stroke in the plane of the divisions. In this way the divisions being by convenience upon the external border of the limb \*, reposets of divisions are thosely rendered incommedicus; but those

It has been objected, that laying the divisions upon the extreme edge of the limb of the infrusement subjects it to injury: but, to obviate this, in an HADLER'S quadrant made for me, by my direction, by the late Mr. MORGAN, in the year 1756, wherein the verhier is taid even with the divisions, more are protected by a projection of the felial part of the limb, beyond the verhier; a Raise being dank laying edge of the limb, to obser the vernier.

that wish two sets, as a check, will in a great measure aid themselves, by reading from two different parts of the same set of divisions; which is very easily provided for, by putting an additional stroke upon the index plate, at the distance of 9, 11, or any prime number of divisions to 19, 23, or more; and reading off from that stroke also; as before recommended for great quadrants, where the vernier is proposed to be rejected \*: so that they will thereby be mutually checked by divisions that had no correspondence in their original formation.

\* I would not have it thought, from my proposal of rejecting the vernier, that I have any quarrel with it; I think it a very simple and ingenious contrivance, where it is properly applicable; that is, where the strokes of the vernier, or their estimated halves, are sufficient for all the precision required or expected from the instrument, as in Hadley's quadrants, theodolites, &c.: but where still more minute divisions are required than can easily be had by estimation from the vernier; to do this by a screw, as a supplement to the vernier, appears to me in the light of bringing a more accurate tool to supply the desciences of one less accurate; when the former might, with more propriety, supply the place of the latter altogether.



11. A Series of Observations on, and a Discovery of, the Period of the Variation of the Light of the Star marked δ by Bayer, near the Head of Cepheus. In a Letter from John Goodricke, Esq. to Nevil Maskelyne, D. D. F. R. S. and Astronomer Royal.

#### Read November 24, 1785.

SIR,

York, June 28, 1785.

THE improvements which of late years have been introduced into astronomy, should be attributed not only to the diligence and accuracy wherewith astronomers prosecute their observations and discoveries, but in part also to your exertions, and especially to that kind encouragement which you have, on many occasions, afforded those who make this science their chief study; and I am happy to have this opportunity of acknowledging myself one of those who are much indebted to you in this respect. Under these impressions I thought I could not do better than to address to you the following account of a periodical variation in the star & Cephei, which I lately discovered. This account will, I presume, be a considerable addition to the sew discoveries that have but very lately been made respecting the same subject. They may probably lead to some better knowledge of the fixed stars, especially of their constitution and the cause of their remarkable changes.

My first observation was Oct. 19, 1784; and as I wished to establish the several points of the variation with as great accuracy as the nature of the subject will admit of, I have delayed sending this account till now; but as observations made through fo long an interval of time must be very numerous, and would only fwell this paper to an unnecessary length, I have in the following scries formed a sclection, chiefly of those that were made under the most favourable circumstances; and I must add, that none of those that are omitted contradict the results. From this feries I have fettled, that the flar has a periodical variation of 5 d. 8 h. 37'1, during which time it undergoes the following changes:

- 1. It is at its greatest brightness about one day and thirteen hours.
- 2. Its diminution is performed in about one day and eighteen hours.
- 3. It is at its greatest obscuration about one day and twelve hours.
  - 4. It increases in about thirteen hours.

When it is in the first point it appears as a star of between the fourth and third magnitude; but its relative brightness does not feem always to be quite the same, being sometimes between Z and . Cephei, and fometimes only equal to, or fomething less than, . Cophei, or between & Cephei and 7 Lacertæ. In the third point it appears as a star of between the fourth and fifth magnitude, if not nearer the fifth; and its relative brightness is as follows: nearly equal to s and & Cephei, and considerably less than 7 Lacertæ.

The relative brightness and magnitude of those stars to which the variable one was compared, is as follows: \( \zeta \) Cephei, the brightest, is between the third and fourth magnitude; , Cephei, the the next brightest, is between the fourth and third; 7 Lacertæ is less than ι Cephei, and of about the fourth magnitude; ε Cephei is between the fourth and lifth magnitude; and ξ Cephei, which is a little 1 is than ι, is between the fifth and fourth.

### A Series of Observations on the Variation of the Light of the Star & Cephei.

1784, Oct. 19, at 81 h. I thought it was rather less than  $\zeta$  Cephei.

Oct. 20, at 81 h. it was rather less than  $\zeta$ , and about equal to Cephei.

Oct. 22, at 91 h. less than 1, and larger than 2 Cephei; but the air was not very favourable.

Oct. 23, at 61 h. and 11 h. less than 7 Lacertæ, and a little brighter than s Cephei.

Oct. 24, at 61 h. less than  $\zeta$  Cephei, somewhat less than  $\ell$  Cephei, and something brighter than 7 Lacertæ; strong moonlight, and air rather hazy.

At 8½ h. to 11 h. a little less than  $\zeta$  and  $\iota$ . Cephei, and brighter than 7 Lacertæ; zir clear and frosty; the moon was very low at 11 h.

Oct. 25, at 6 h. 8 h. and 11 h. nearly the same; air pretty clear, and moon bright.

Oct. 26, at 9th. and 11 h. rather less than 7 Lacertze; strong moon-light, but air very clear.

Oct. 27, 64 h. and 104 h. less than 7 Lacertze, and brighter than a Cephei; ditto.

Oct. 28, at 9½ h. and 12 h. just the same, if not less; moon-light, but the air was remarkably clear.

Oct. 31, at 8 h. nearly equal to, if not less than, 7 Laceruz.

Nov. 1, at 112 h. somewhat less than 7 Lacertæ; air clear.

Nov. 3, at 12½ h. equal to, if not a little less than, 7 Lacertæ; but the weather was not very favourable: it seemed to have increased since my sirst observation, which was at 5½ h.

Nov. 5, at 13 h. brighter than 7 Lacertæ, and less than  $\zeta$  Cephei; flying clouds, but air pretty clear.

Nov. 6, at 9 h. and 12 h. rather less than 7 Lacertæ.

Nov. 7, at 7½ h. I thought it still rather less than 7 Lacertæ, but at 10½ h. and 11 h. it was evidently less than it; air clear.

Nov. 10, at 11 h. and 12 h. something less than & Cephei, and brighter than 7 Lacertæ; clear sky.

Nov. 11, at 7 h. to 12 h. a little brighter than 7 Lacertæ.

Nov. 12, at 7 h. and 8 h. about equal to 7 Lacertæ. From 91 h. to 12½ h. it was something less than 7 Lacertæ, and brighter than a Cephci.

Nov. 13, at 6½ h. to 11 h. only a little brighter than & Cephei, though sometimes it appeared equal to it.

Nov. 14, at 71 h. brighter than a Cephei, and, I believe, equal to 7 Lacertæ. There was a haziness about 7 Lacertæ.

Nov. 15, at 12 h. less than & Cephei, and brighter than 7 Lacertæ; fine aurora borealis, but the air was very clear.

At 181 h. ditto; but the air was not very clear.

Nov. 16, at 6½ h. and 10 h. just the same, if not decreased at 10 h.

Nov. 17, at 61 h. to 102 h. a little less than 7 Lacertæ, and brighter than a Cephei; air clear.

Nov. 18, at 9 h. to 12 h. and 19 h. little brighter than s and E Cephei.

Nov.

Nov. 19, at 6 h. to 10 h. just the same, being but a very little brighter than s and & Cephei; air clear.

At 18 h. it was increased, being now brighter than s and E Cephei.

Nov. 20, 7 h. to 11 h. considerably brighter than 7 Lacertæ, something less than ζ Cephei; air extremely clear at 11 h.

Nov. 21, at 6 h. exactly the fame.

Nov. 22, at 91 h. about equal to 7 Lacertæ; moon-light.

Nov. 25, at 7 h. and 8 h. less than 7 Lacortæ, and brighter than e and & Cophei; air clear.

At 91 h. and 91 h. a little brighter than 7 Lacertæ.

At 10½ h. and 12 h. brighter than 7 Lacertæ, and about between 5 Cephei and 7 Lacertæ, but rather nearer 7 Lacertæ; air clear and moon-light.

Nov. 26, at 9 h. exactly as last night.

Nov. 29, at 7½ and 8 h. less than 7 Lacertæ, and something brighter than  $\varepsilon$  and  $\xi$  Cephei.

Nov. 30, at 8 h. as last night; air clear.

At 101 h. between 7 Lacertæ and & Cephei, but nearer s.

At 10½ h. 11 h. and 12 h. ditto, but nearer 7 Lacertæ; air clear. I have no doubt of its increase since 8½ h. Mr. E. Pigott found it rather less than  $\zeta$  Cephei at 18½ h. See his Observations.

Dec. 1, 11 h. fomething less than & Cephei, and brighter than 7 Lacertæ.

Dec. 3, 121 h. less than 7 Lacertæ, and brighter than a Cephei.

Dec. 4, 5½ h. to 12 h. little brighter than s and & Cephei.

Dec. 7, 10 h. and 11 h. between & Cephei and 7 Lacertæ.

Dec. 8, at 101 h. between 7 Lacertæ and s Cephei.

Dec. 9, 11½ h. ditto, but nearer s Cephei; about equal to § Cephei.

Dec. 11, 6 h. fomething less than 7 Lacertæ; brighter than 2 Cephei.

At 71 h. fomething brighter than 7 Lacertæ.

At 81 h. brighter than 7 Lacertæ.

At 9 h. and 11 h. between & Cephei and 7 Lacertæ, but nearer 7 Lacertæ.

Dec. 12, at 6 h. fomothing less than  $\zeta$  Cephei.

Dec. 13, at 91 h. brighter than 7 Lacertæ; considerably less than  $\zeta$  Cephei.

Dec. 14, at 81 h. nearly equal to, if not less than, 7 Lacertæ.

Dec. 17, at 5! h. and 7! h. equal to, if not less than, ι Cephei, and between ζ Cephei and 7 Lacertæ, but nearer ζ.

Dec. 18, at 9 h. less than 2 Cephei, and between ζ Cephei and 7 Lacertæ, but nearer 7 Lacertæ.

Dec. 19, at 19 h. less than 7 Lacertæ; considerably brighter than s and & Cephci.

Dec. 20, at 6 h. and 7 h. about equal to E Cephei, and a little brighter than & Cephei.

Dec. 21, at 8 h. and 18 h. nearly equal to & Cephei.

Dec. 22, at 8½ h. considerably brighter than 7 Lacertæ, less than  $\zeta$ , and a little less than  $\iota$  Cephei; strong moon-light.

Dec. 25, at 51 h. between 7 Lacertæ and & Cephei.

Dec. 28, at 8 h. &c. between & Cephei and 7 Lacertæ, and equal to, if not less than, 1 Cephei.

Having, in the beginning of this paper, mentioned my intention of omitting feveral observations, in order to be as short as possible, I have thought it best, with the exception of one only, to leave out all that were made in January, February,

and March, because they were much interrupted by the then unfavourable state of the weather.

1785, Feb. 8, at 9 h. equal to 7 Lacertæ; confiderably less than . Cephei.

At 10 h. rather brighter than 7 Lacertæ.

At 11 h. brighter than 7 Lacortæ; a little less than . Cephei.

April 1, at 11 h. about equal to s and & Cephei; weather not favourable.

April 2, at 12½ h. ditto.

April 3, at 8 h. a little less than . Cephei, less than & Cephei, and brighter than 7 Lacertæ.

April 4, at 12 h. ditto; if any thing, it is less than it was last night.

April 7, at 10 h. about equal to s and & Cephei; but the weather was not very favourable.

April 8, at 7½ h. considerably less than . Cephei, brighter than  $\varepsilon$  and  $\xi$  Cephei; but the air was not very clear.

At 10 h. it was increased.

At 11 h. only a little less than , Cephei.

At 12,h. equal to, if not a little brighter than 4, and less than 7 Cophei; considerably brighter than 7 Lacertæ.

April 12, at 12 h. a little less than s, and nearly equal to & Cephei.

April 13. at 9h. just the same.

At 11 h. seemed rather increased, being equal to s, and a little brighter than & Cephei.

April 16, at 11 1 h. nearly equal to e and & Cephei.

April 17, at 9 h. and 11 h. rather a little less than e, and a little brighter than & Cephei.

April 19, at 11½ h. about equal to Cephei, if not a little brighter than it; less than  $\zeta$  Cephei, and considerably brighter than 7 Lacertæ.

April 24, at 10 h. a little brighter than 7 Lacertæ; considerably less than . Cephei.

At 12 h. scarce at all altered, but if any thing it is a little increased; air very clear, and observation good.

April 25, at 10 h. and 11 h. little less than . Cephei, and considerably brighter than 7 Lacertæ.

April 26, at 10 h. and 11 h. less than 7 Lacertæ, something brighter than 2, and brighter than 2 Cephei.

May 4, at 9 h. and 12 h. a little less than s and & Cephei.

May 7, at 12 h. less than . Cephei, and a little brighter than 7 Lacertæ.

May 9, at 11 h. a little less than & Cephei.

May 10, at 12 h. between 7 Lacertæ and & Cephei, but fomething nearer s.

May 11, at 10 h. and 12 h. brighter than 1 Cephei, less than E Cephei, and much brighter than 7 Lacertæ.

May 14, at 11½ h. much less than 7 Lacertæ, equal to, if not a little brighter than, s Cephei, and brighter than & Cephei.

May 15, at 91 h. less than e, and about equal to & Cephei.

May 19, at 9½ h. and 11 h. equal to, if not a little brighter than, s Cephei, and brighter than & Cephei.

May 20, at 9½ h. 11 h. and 12 h. a little less than s, and nearly equal to E Cephei.

May 21, at 12 h. equal to, if not a little less than, ι Caphei; less than ζ Caphei, and considerably brighter than 7 Lacortæ.

May 22, at 10 h. and 11 h. a little brighter than . Cephei, the rest as last night.

May 23, at 11 h. and 111 h. nearly equal to 7 Lacerton, and less than 1 Cephei.

May

May 25, at 10 h. and 12 h. a little less than s, and about equal to & Cephei.

May 27, at 10 h. between \( \zeta\) and \( \text{Cephei, and confiderably} \)

brighter than 7 Lacertæ.

May 28, at 12 h. between 1 Cophei and 7 Lacerta.

June 1, at 91 h. I thought it less than Cephei; air not clear, and twilight pretty strong.

At 101h. and 12h. between \( \zeta\) and \( \zeta\) Cephei, but rather nearer \( \mu\).

June 2, at 12 h. exactly the fame.

June 6, at 12 h. ditto; the weather was not very favourable, but the observation seemed good.

June 10, at 11 1 h. a little less than & Cephei.

June 12, at 11 h. between & and & Cephei.

June 21, at 10 h. nearly equal to, if not a very little brighter than, & Cophei; twilight.

At 11 1 h. a little less than e, and about equal to & Cephei.

June 23, at 11½ h. between \$\zeta\$ and a Cephei, and brighter than 7 Lacertæ.

June 24, at 11 h. ditto; only a short view.

June 25, at 11½ h. a little, but certainly, brighter than a Cephei, brighter than & Cephei, and confiderably less than 7 Lacertze.

June 26, at 11 h. a little less than a Cephei, and equal to, if not a little brighter than, & Cephei.

In the above collection I find only two or three mistakes of any consequence, viz. the dates of the observations of April 7, and 8, are marked in my journal for April 8, and 9; but I have corrected them, being convinced they are erroneous: and the observation of May 10, I think, disagrees rather too much from what it ought to be by computation.

Tho

The following observations were made by my friend Mr. E. PIGOTT; who, at my request, was so kind as to observe the star as often as possible, though then in an ill state of health. They are, I presume, sufficient to corroborate the variation of the star as above stated, although in one or two places there may be found some little differences between our observations.

#### MR. PIGOTT'S OBSERVATIONS.

1784, Oct. 25, at 12 h. rather brighter than 7 Lacertæ; much brighter than & Cephei, and much less than  $\zeta$  Cephei; nearly between  $\zeta$  Cephei and 7 Lacertæ.

Oct. 26, at 12 h. seemed the same as yesterday.

Nov. 1, at 12 h. brighter than 2 Cephei; seemed rather less than 7 Lacertæ.

Nov. 13, at 8½ h. rather, but very little, brighter than & Cephei; less than 7 Lacertæ.

Nov. 15, at 12 h. seemed rather brighter than 7 Lacertæ, and less than ζ Cephei.

Nov. 17, at 8 h. less than 7 Lacertæ; rather brighter than & Cephei.

Nov. 18, at 12 h. equal to s Cephei, though sometimes it seemed less; less than 7 Lacertæ.

Nov. 19, at 12h. seemed equal to & Cephei.

Nov. 20, at 11 h. rather less than ζ Cephei; brighter than 7 Lacertæ.

Nov. 25, at 11½ h. if not equal rather brighter than 7 Lacertæ; much brighter than 8 Cephei.

Nov. 29, at 8 h. equal to a Cephei.

Nov. 30, at 111 h. brighter than Cephei; less than 7 Lacertæ.

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At

At 18½ h. much increased; rather less than ζ Cephei.

Dec. 4, at 6½ h. sometimes thought it less, and at other times brighter, than & Cophoi.

Dec. 11, at 52 h. less than 7 Lacertæ; rather brighter than & Cephei.

At 11 h. rather brighter than 7 Lacertæ; not at its full brightness.

Dec. 21, at 7 h. if any difference less than & Cephei.

At 184 h. a little brighter than & Cephei.

Dec. 22, at 8 h. less than ζ Cephei; a little brighter than 7 Lacertæ.

Dec. 28, at 5<sup>2</sup> h. nearly equal to Cephei; had only a short view of them.

1785, April 26, at 11½ h. less than  $\zeta$ , rather less than  $\iota$  Cephei, brighter than  $\iota$  Cephei, and if any difference rather brighter than 7 Lacertæ.

May 4, at 9½ h. much less than ζ Cephei, less than ι Cephei, and than 7 Lacertæ, and rather brighter than ε Cephei.

May 7, at 11 h. rather less than . Cephei, and brighter than . Cephei.

May 9, at 114 h. rather brighter than a Cephei, and much less than a Cephei, and 7 Lacortæ.

May 11, at 10½ h. rather less than ζ, and rather brighter than ι Cephei; much brighter than 7 Lacertæ.

May 19, at 10 h. equal to a Cephei, but if any difference rather brighter; little hazy and moon-light. The same at 12 h. but the weather was not hazy then.

May 20, at 111 h. and 121 h. rather brighter than a Cephei, and much less than 7 Lacertæ; moon-light strong at 111 h.

May 21, at 121 h. equal to 7 Lacertæ; less than . Cephoi.

May 22, at 12 h. equal to, if not brighter than, 7 Lacertæ; think it brighter than. Cephei.

May 23, at 113 h. feemed fometimes equal to, though generally less than, Cephei and 7 Lacertæ.

Having now delivered the observations, from whence I have deduced the preceding conclusions, nothing more relative to this subject remains to be mentioned, except the determination of the period; in the doing of which I must follow nearly the fame methods as have been used in some preceding papers. It is very evident, from a rough calculation, where only fingle periods or very fhort intervals are used, that it is about five days and eight hours. In order to determine this period with greater exactness, I have, in the following table, collated some of the most precise phases. The first five are times when & Cephei was observed to be equal to 7 Lacertæ during the course of its increase of brightness, which proceeds rapidly. The five next are similar times, with this only difference, that as it was not then actually observed to be equal to 7 Lacertæ, a proper allowance from the nearest observations was made on supposition that the changes are fimilar in every period. The ten last are affumed times between its least and greatest brightness, which determinations can hardly err more than a few hours, as the whole increase is completed in thirteen hours; but even were it so, the periods deduced from them would still be exact, because the intervals are very long.

1784 and	178	۲.							١	
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April 8,	8	}			- 3			J		J
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April 8,	8	5						,		
Nov. 30,	16	}	dit	tto	27		ditto	5	8	351 -
April 24,	8	ſ	-	.,,	1			J	•	44"
Oct. 23,	21	J	di	tto	39		ditto	5	8	411+
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May 21,	0	S						~		<i>J</i>
Nov. 19,	22	}	di	tto	25		ditto	5	8	40}
April 2,	23	5			<b>.</b> .				_	
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Hence	the 1	per	iod is, o	n a m	ean,		•	5	8	371+

A few curfory remarks shall conclude this Paper. What I have before mentioned, that the greatest brightness of & Cephei does not feem to be always quite the fame, is not peculiar to this star, but is also to be observed in the other variable ones. I have remarked in a late Paper, that the greatest brightness of & Lyræ is subject to considerable alterations, and thought then that it might be owing to some fallacy of observation; but now I have

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I have reason to alter, in some measure, my opinion on this head. Even Algol does not seem to be always obscured in the same degree, being perceived to be sometimes a little brighter than e Persei, and sometimes less than it \*. These seeming irregularities, however, do not appear to affect the period; for if we compare the same precise phases together, it will be sound still regular. This may, I suppose, be accounted for, by a rotation of the star on its axis, having fixed spots that vary only in their size.

I need not say, that the situation of  $\delta$  Cephei, on account of its great northern declination is such, that its changes may be observed with great advantage in these latitudes, it being always sufficiently clevated above the horizon. To this circumstance are also owing its various changes of position, which, I find, affect the comparative brightness of the stars a little; but, as these differences are very trifling, I shall take no further notice of them.

If you think this account worthy of notice, I beg you will be so kind as to communicate it to the Royal Society.

I remain, with great regard, &c.

### JOHN GOODRICKE.

\* This will appear from an attentive examination of the observations of that star's diminution in my two late Papers, which were printed in the LXXIIId and LXXIVth volumes of the Philosophical Transactions. I did not take much notice of it then, because I thought the difference was too small to be relied on; but the observations I have made since seem to consirm that it does really diminish a little unequally. M. MECHAIN, in a letter to Mr. E. PIGOTT, mentions the same fast.

III. Magnetical Experiments and Observations.

By Mr. Tiberius Cavallo, F. R. S.

(The Lecture founded by the late HENRY BAKER, Efq. F.R.S.)

# Read November 24, 1785.

HE object of this lecture is to shew the properties of some metallic substances with respect to magnetism; and the experiments herein related scem to ascertain some new and remarkable facts.

The magnetic properties have been generally thought to belong only to iron, or to those substances which contained that metal; comprehending under the general name of iron not only the metal commonly fo called, but likewife its more perfect and more imperfect states, viz. steel, iron ores, amongst which is confidered the magnet, and the calces of iron, excepting only these which are very much dephlogisticated, for they possess no magnetic property whatsoever. Some other metallic fubstances, and especially platina, brass, and nickel, on which the magnet has some action, were thought to be magnetic so far as they contained some portion of iron, the presence of which may be manifested by chemical methods in many cases, but not always; because the quantity of iron may be so excesfively small in proportion to the weight of the other metal in which it is concealed, as not to be discoverable by chemical analysis, and yet it may be sufficient to affect the magnetic needle. needle. The following experiment will shew, that an exceedingly small quantity of iron will render a body sensibly magnetic.

Having chosen a piece of Turkey-stone, which weighed about an ounce, I examined it by a very fensible magnetic needle, and found that it had not the least degree of magnetism, the needle not being moved from its usual direction by the vicinity of any part of the furface of the stone; I then weighed a piece of steel with a pair of scales that turned with the twentieth part of a grain, and afterwards drew one end of it over the furface of the stone in various directions. done, the piece of steel was weighed again, and was found to have loft fo small a part of its weight as not to be difcernible by that pair of scales; yet the Turkey-stone, which had acquired only that fmall quantity of steel, affected the magnetic needle very fenfibly. Chemistry seems not to afford any means by which so small a quantity of iron may be decisively detected in a body that weighs one ounce. Hence it follows, that though no iron is to be discovered in a body by chemical methods, yet it should not be concluded, that the said body, if it affect the magnetic needle, does not own its magnetism to some fmall quantity of iron concealed in its fubstance.

Nickel is a metallic fubstance which has been suspected to be capable of acquiring some degree of magnetism independent of iron; and this suspicion has been sounded upon observing, that nickel retained its magnetism after having been repeatedly purified. There are, however, persons who have denied the magnetism of purified nickel; and I have seen some pieces of it which did not in the least affect the magnetic needle. It is probable, that those pieces were not pure nickel, and perhaps

fome cobalt was contained in them; but I fee no reason why the nickel, when alloyed with a little cobalt, should show no magnetism, if that property does really belong essentially to it.

The greatest number of my experiments are relative to the properties of brass; and they seem to prove, that this compound metal, which is often magnetic, does not owe its magnetism to iron, but to some particular configuration of its component particles, occasioned by the usual method of hardening it, which is by hammering.

In some specimens of brass, and especially in that which has often passed from the work-shop to the surnace, and from the latter to the former, there are sometimes pieces of iron sensible not only to the magnet, or the chemical analysis, but even to the sight, which render the brass strongly magnetic. But the brass generally used in my experiments was such as, when quite tost, it had no sensible degree of magnetism.

Before we begin with the narration of those experiments, it will be proper to describe the magnetic needle I generally used, which is suspended in a particular manner; and which may be useful to persons who are fond of making magnetic experiments, not only for its sensibility, but likewise for the simplicity of its construction.

Experience having shewn, that large magnetic needles are not proper for experiments wherein a very small degree of magnetism must be ascertained, and the free motion of the usual small needles being proportionally more obstructed by the nature of their suspension, even when surnished with agate caps, I endeavoured to contrive a fort of suspension which might answer the purpose better than the needles suspended in the usual manner; and, after several attempts, at last I constructed a chain

of horse-hair, consisting of five or six links, to which the needle was fuspended. Each link is about three-quarters of an inch in diameter; and the extremities of each piece of hair, which is formed in a ring, are joined by a knot, and secured by a little fealing-way. The link on one end of this chain is fuspended to a pin in a proper frame, or any support that may be at hand; and to the link of the other extremity which lies lowermost, a piece of fine silver wire is hooked. This wire is about an inch and a half long, and its lower extremity is fastened round a small and cylindrical piece of cosk, through which a common fewing needle, made magnetic, is thrust horizontally. Thus the magnetic needle is suspended by a hair-chain, the links of which, on account of the smoothness and lightness of the hair, move very freely in each other, and allow the needle more than a whole revolution round its centre, with fo small a degree of friction as may be considered next to nothing. By comparing this needle with others of the best fort in use, I find the former to be much more sensible; for when bodies which have an exceedingly fmall magnetic power are tried, this needle will be frequently attracted by them when the others are not fenfibly affected.

In order to try farther the delicacy of such suspension, I placed a piece of looking-glass under the needle, and nearly horizontal, so that the image of the needle was seen in it. Now, as a fine line had been previously marked on the glass, things were so disposed as that the image of the needle might coincide with the line marked on the glass, the eye being placed in a proper point of view; afterwards, by shaking the needle either very gently or very quickly. I repeatedly indeavoured to place it out of the magnetic meridian; but every Vol. LXXVI.

endeavour proved ineffectual, for the needle constantly settled in the same direction, without any sensible variation.

With a needle thus suspended a variation compass might be very eafily confiructed, and it would perhaps be more accurate than those commonly in use. For this purpose the needle ought to be about three inches long, and the piece of lookingglass ought to be fixed upon the index of an HADLEY's sextant, which must be placed horizontally under the needle, with its edge or fiducial line in the meridian of the place, in order to observe the daily variation of the needle. I have made only a rough model of fuch a variation compass, and it seemed to answer very well. This construction appears to have the following advantages over the common fort: 1ft, the needle being cylindrical, and without a hole in the middle, would be less subject to have more than two poles. 2dly, The needle being slender, its poles would stand more exactly in its axis, which with the common flat needles is feldom the cafe. 3dly, It will appear, by a little confideration, that in this conftruction there is no need of the needle's center of motion keeping always in the fame invariable point, which renders the construction both very easy and very accurate: and, lastly, as the sextant may be placed at a confiderable distance below the needle, and the rest of the frame may be made of any fize, there would be no necessity of placing any brass or other metal so near the needle as might affect it in case this metal had any magnetism, which generally happens with brass.

In order to examine the magnetism of divers substances, besides the above described needle, I used to put a small magnetic needle upon water, and then bring the substance to be examined near it, or place the substance itself upon water, **Sometimes** 

fometimes resting it upon pieces of cork, and then bring a powerful magnet near it.

# Examination of the Magnetical Properties of Brass.

A few years ago, being intent on making some magnetic experiments, in which brafs was concerned, I used to examine first whether the pieces of brass had any magnetism or not, and rejected those pieces which had an evident degree of that power. In the course of those experiments I remember to have observed, that those pieces of brass which had been hammered were generally magnetic, and much more fo than others; in confequence of which I made no use of hammered brass in those experiments. But lately, having ordered a theodolite at a philosophical instrument shop, I particularly enjoined the workmen to try the brass, both soft and hammered, before they worked it, and to make no use of that which had any magnetism. They found, that hammered brass, even such as before the hammering had no magnetifin, could afterwards disturb the magnetic needle very sensibly. These observations induced me to make the following experiments.

# EXPERIMENT I.

An oblong piece of brass, weighing somewhat less than half an ounce, being examined by presenting every part of its furface to the suspended needle, shewed no sign of magnetism whatever. It was then hammered for about two minutes; the confequence of which was, that it became magnetic fo far as to attract either end of the needle from about a quarter of an inch. This same piece of brass being now put into the fire so as K 2

to become red-hot, by which means it was fostened, and when cold being presented to the suspended needle, its magnetism was found to be entirely gone. Hammering made it again magnetic. Softening by fire took the magnetism away a tecond time; and thus the magnetism was repeatedly given it by hammering, and was destroyed by softening; sometimes showing to have acquired a sensible degree of that power, even after two or three strokes of the hammer.

#### EXPERIMENT II.

The refult of the first experiment would naturally induce one to suspect, that the hammer and anvil might have imparted some small quantity of steel to the brass, which rendered it magnetic; and that this magnetism was destroyed in softening the brass, insomuch as the sire calcined the small quantity of steel that had adhered to it. In consequence of which consideration, I took other pieces of brass besides that used before, and hammered them between card-paper, changing the pieces of paper as often as was necessary, since they were easily broken by the hammer; but the pieces of brass became constantly magnetic by the hammering, and their magnetism was destroyed by fire.

In this experiment I generally gave to the brass not above thirty strokes with the hammer.

#### EXPERIMENT III.

Still suspecting that the hammer and the anvil might have imparted some small quantity of iron to the brass, because the pieces of card-paper sometimes were broken by the first or second fecond stroke, in which case either the hammer or the anvil touched the brass; I hardened a piece of brass by beating it between two large flints, viz. using one for the hammer, and the other for the anvil. The piece of brass became magnetic, though in this case it seemed to have acquired not so much power as when it had been hardened with the hammer; but it must be observed, that the slints being rough and irregular, the piece of brass could not be hardened by them so easily, or so equally, as by the other method.

The flints, being examined both before and after the experiment, were found to have not the least degree of magnetism.

#### EXPERIMENT IV.

A piece of brass, which by hammering had been rendered fo strongly magnetic as to attract either pole of the needle from about a quarter of an inch, was put into a crucible, together with a confiderable quantity of charcoal dust, which surrounded it every where. The crucible was covered with clay, and being put into the fire, was kept red-hot for about ten minutes. After cooling, the piece of brafs was taken out of the crucible, and being examined, was found to have entirely loft its magnetism. The object of this experiment was to ascertain whether the lofs of magnetism, in a piece of brass that was fostened, was owing to the calcination of the ferrugineous particles, which, notwithstanding the preceding experiments, might still be suspected to be imparted to it; because in this way of foftening the brafs, the ferrugineous particles being furrounded with charcoal dust, could not have been calcined; hence the brass ought not to have lost its magnetifu, which was not the refult of the experiment. EXPE-

# EXPERIMENT V.

One of those pieces of brass which had been used for the foregoing experiments, and which had been deprived of magnetism by fire, was hammered between two large and pretty thick pieces of copper, which were not in the least magnetic; and, after a few strokes of the hammer, it became sensibly magnetic.

#### EXPERIMENT VI.

In order to examine the difference of this property in brass of various kinds, I have tried a great many pieces of English as well as foreign brass; some of which was very old, and so sine and uniform, that an eminent watch-maker of my acquaintance used it for the very best fort of watch work. But I find, that they mostly have the property of becoming magnetic by hammering, and of losing that power when softened. There are, however, some pieces which acquire no magnetism by the hammering, though they are rendered equally hard by it as those which acquire the magnetism. By attentively examining them, I have not yet been able to distinguish, without a trial, which pieces are capable of acquiring magnetism, and which not; the colour, apparent texture, and degree of dustility seeming to afford no sure indication. In short, what I have observed relating to the magnetic properties of brass is:

1st, That most brass becomes magnetic by hammering, and loses the magnetism by annealing or softening in the sire.

adly, That the acquired magnetism is not owing to particles of iron or steel imparted to the brass by the tools employed.

3dly, Those pieces of brass which have that property, retain it without any diminution after a great number of repeated trials, viz. after having been repeatedly hardened and softened. But I have not found any means to give that property to such brass as had it not naturally.

4thly, A large piece of brass has generally a magnetic power fomewhat stronger than a smaller piece; and the flat surface of the piece draws the needle more forcibly than the edge or corner of it.

5thly, If only one end of a large piece of brass be hammered, then that end alone will disturb the magnetic needle, and not the rest.

6thly, The magnetic power which brass acquires by hammering has a certain limit, beyond which it cannot be increased by farther hammering. This limit is various in pieces of brass of different thickness, and likewise of different quality.

7thly, Though there are some pieces of brass which have not the property of being rendered magnetic by hammering; yet all the pieces of magnetic brass, that I have tried, lose their magnetism by being made red-hot, excepting indeed when some piece of iron is concealed in them, which sometimes occurs; but in this case, the piece of brass, after having been made red-hot and cooled, will attract the needle more forcibly with one part of its surface than with the rest of it; and hence, by turning the piece of brass about, and presenting every part of it successively to the suspended magnetic needle, one may easily discover in what part of it the iron is lodged.

From those observations it follows, that when brass is to be used for the construction of instruments wherein a magnetic needle is concerned, as dipping needles, variation compasses, see, the brass should be either lest quite soft, or it should be

chosen of such a fort as will not be made magnetic by hammering, which fort however does not occur very easily.

# Examination of the Magnetic Properties of some other Metallic Substances.

The refult of the experiments on brass induced me to examine other metallic substances, and especially its components, viz. copper and zinc: though the result of the experiments has not been very remarkable, excepting with platina, which metal has properties in great measure analogous to those of brass.

Having examined various pieces of copper, by means of the suspended magnetic needle, and having never found them magnetical, except only sometimes in such places which had been siled, and where some particles of steel might have been lest by the sile, I next proceeded to hammer some pieces of it, not only in the usual way, but likewise between slints: the result, however, was very dubious; for though, in general, they had no effect whatever on the needle, yet sometimes I thought the needle was really attracted by some pieces of hammered copper; but then this attractive power was so exceedingly small as not to be depended upon.

Zinc, either not hammered, or hammered as far as could be done without breaking it, shewed no signs of magnetism whatever, when presented to the magnetic needle. A mixture of rither and tin neither had any action upon the needle.

A piece of a broken reflector of a telescope, which consisted of rin and copper; a mixture of tin, zinc, and a little copper; a piece of filver, both fost and hammered; a piece of pure gold, both fost and hammered; a mixture of gold and filver, both hard and soft; and another mixture of a great deal of filver.

filver, a little copper, and a less quantity of gold, either before or after hammering, had not the least action on the magnetic needle.

Platina was the metal I last examined, and the experiments made with it seem to deserve particular attention.

#### EXPERIMENT I.

A large piece of platina, which, after being precipitated from its folution in aqua regia, had been fused, or rather concreted together, being presented to the suspended magnetic needle, shewed not the least sign of magnetism. It was then hammered; but after the third or fourth stroke of the hammer it broke into many pieces, several of which being tried, shewed no magnetism, nor could any of the finest particles be attracted by the magnet presented very nearly over them. The broken surface of this piece of platina was full of cavities, some of which were large, and others just discernible; and altogether the metal seemed to have undergone an impersect suspense.

### EXPERIMENT IL

The grains of native platina were examined next, by putting a magnet just over them; but the magnet attracted not above ten or twenty particles out of about half an ounce of platina: and those which were attracted had either little or no shining metallic appearance like the rest, and were exceedingly small.

## EXPERIMENT III.

Having picked out feveral of the largest grains of plasits, I presented the magnet to them; but they were not in the least attracted by it. One of those grains was then hammered; by which means, after about eight or ten strokes, it was spread into a plate, about a tenth of an inch in diameter, and nearly circular; afterwards the magnet being prefented to it, the former attracted it from the distance of about one-twentieth of an inch. The other grains being all hammered one after the other, were rendered by it so far magnetic as to be attracted by the magnet, and to difturb the fuspended needle when they were presented to it. But there were some amongst them which acquired no magnetism at all, though they had been purposely hammered much longer than the others.

As far as I could observe, those pieces which would not acquire any magnetisin by hammering, had not a very shining appearance before the hammering, though afterwards they could not be distinguished from the others by their appearance; and they feemed not to spread under the hammer to cafily as the others.

In general three or four strokes are sufficient to render a grain of platina evidently magnetic, but about ten strokes give it the full power it is susceptible of.

#### EXPERIMENT IV.

Those grains of platina, which in the preceding experiments had been rendered magnetic by hammering, being put upon a charcoal, were made red-hot by means of a blow-pipe; and afterwards being presented to the magnet, and likewise to the fuspended needle, they shewed not the least fign of magnetism. Heat, therefore, deprives them as well as brass of the magpetifm acquired by hammering. A fecond hammering renmered them magnetic, though not so quickly, nor to so great a degree, 3

degree, as it had done the first time. However, it must be obferved, that the pieces of platina having been rendered flat and thin by the first hammering, could not be so easily struck, nor spread much more, by the second.

If it is true, as those experiments feem to prove beyond a doubt, that magnetism may exist, or may belong to other fubstances, independent of iron, it must follow, that the attraction of a few particles of an unknown substance by the magnet is not a fure fign of the presence of iron. Hence those fubstances, which hitherto have been considered as containing ferrugineous particles, for no other reason but because the magnet attracted a small quantity of them, must be considered as dubious; and the conclusion of the existence of iron should not be admitted, except when those particles, which have been separated by the magnet, appear to be iron by some other trial; for though it is true, that iron is always attracted by the magnet, yet it does not hence follow, that whatever is attracted by the magnet must be iron.

# POSTSCRIPT.

THE existence of magnetism, or of the power of attracting and being attracted by the magnetic needle, in bodies, without the interference of iron or any ferrugineous matter, being a proposition not only new and singular, but seemingly of importance in philosophy, the experiments which tend to confirm it should be never deemed superfluous, nor any possible objection be left unanswered: hence, since the writing of the tregoing paper, I have endeavoured to raise objections, and contrive means of explaining them; but every confideration feemed to confirm the proposition advanced. The principal of those objections was, that the brafs which becomes magnetic by hammering and loses that power by softening, might contain a fmall quantity of iron, to which that magnetic power was owing; and that this iron or martial earth, differfed through the fubstance of the brass, might become phlogisticated by the action of hammering; infomuch as the brais being forced into a smaller space might perhaps give some of its phlogiston to the martial earth, and thus render it magnetic; and, on the contrary, the action of the fire in foftening might remove that phlogiston from the martial earth, and give it to the brass; hence the former, remaining quite dephlogisticated, would no longer shew any signs of magnetism. The consideration that iron may be dephlogisticated or calcined more easily than brass gave an apparent weight to the fuppolition; but the following experiments feem to expel every doubt.

## EXPERIMENT I.

Having chosen a piece of brass which would acquire no magnetism by hammering, I placed it upon the anvil, together with a considerable quantity of crocus martis, which crocus had no action on the magnetic needle; then began hammering the brass, and turning it frequently, in order to let part of the crocus adhere to it; and, in fact, the crocus had in several places been fastened so well into the brass, that hard wiping with a woollen cloth would not rub it off. The brass appeared red in those places; but, after having been hammered for a long time, it acquired no magnetism whatever. The hardening, therefore,

fore, could not render the iron calx so far phlogisticated as to affect the magnetic needle.

#### EXPERIMENT II.

In order to diversify the preceding experiment, I diilled a hole, about one-eighth of an inch long, and little more than one-fiftieth of an inch in diameter, into a piece of brass that was not rendered magnetic by hammering, and filled it with crocus martis; then I hammered the piece of brass, thus inclosing the calx of iron, and afterwards presented it to the meedle; but there was not the least sign of attraction: the martial earth, therefore, had not acquired any phlogiston from the brass by the action of hammering.

#### EXPERIMENT III.

The piece of brass mentioned in the preceding experiment, viz. with a little calx of iron in it, was put into the fire, and was made quite red-hot, in which state it remained for about three minutes. Then, after cooling, it was presented to the magnetic needle, and this was attracted by the brass only in that place wherein the calx of iron was contained. The action, therefore, of the fire had rendered the martial earth so far phlogisticated as to attract the magnetic needle; hence, if the magnetism of brass was owing to any ferrugineous matter contained in it, a piece of brass ought to become magnetic when softened, which is contrary to the experiments mentioned in this paper.

## EXPERIMENT IV.

A hole, similar to that mentioned in the second experiment, was drilled into a piece of brass that would not become magnetic by hammering, and into it was put some black calx of iron, which was so far phlogisticated as to be attractable by the magnet, and the hole was closed by a few strokes of the hammer. In consequence of which the piece of brass, when presented to the suspended magnetic needle, would attract it only about that place where the magnetic calx was contained. This attraction was very weak. Then the piece of brass, thus prepared, was put into the fire, and was kept for about six minutes, in a heat very little short of that necessary to melt brass, and after cooling I presented it to the needle, expecting that the fire might have dephlogisticated that calx of iron so far as not to let it act any longer upon the needle; but the attraction appeared to be of the same degree it was before the heating.

It feems, therefore, to be demonstrated, as far as the subject will admit of demonstration, that the magnetism acquired by brass, when hammered, is not owing to iron contained in it; and, consequently, that magnetism, or the power of heing attracted by, and attracting, the magnet, may exist independent of iron.

# TO DR. BLAGDEN, SEC. R. S.

SIR,

Windsor, January 9, 1786.

I HAVE made the experiment which you recommended me to try, relating to the magnetism of brass; viz. I mixed, by means of the blow-pipe, a small quantity of iron, with about four times its weight of such brass as would not become magnetic by hammering. The whole globule weighed about two grains, and it attracted the magnetic needle very powerfully. I then melted this globule of brass and iron with about sifty grains of the same fort of brass as had been used before. After cooling, the whole lump of brass appeared to have very little power upon the magnetic needle, every part of its surface attracting one end of the suspended needle, so as to let it just adhere to it when the air was not at all disturbed. But this weak and hardly perceivable degree of magnetism was not increased by hammering, nor annihilated by softening.

In the course of my experiments on the magnetism of brass, I have twice observed the following remarkable circumstance. A piece of brass, which had the property of becoming magnetic by hammering, and of losing the magnetism by softening, having been lest in the fire till it was partially melted, I found, upon trial, that it had lost the property of becoming magnetic by hammering; but having been afterwards fairly melted in a crucible, it thereby acquired the property it had originally, viz. that of becoming magnetic by hammering.

I have

I have likewise often observed, that a long continuance in a fire so strong as to be little short of melting hot, generally diminishes, and sometimes quite destroys, the property of becoming magnetic in brass. At the same time, the texture of the metal is considerably altered, becoming what some workmen call rotten. From this it appears, that the property of becoming magnetic in brass by hammering, is rather owing to some particular configuration of its parts, than to the admixture of any iron; which is confirmed still farther by observing, that Dutch plate-brass (which is made not by melting the copper, but by keeping it in a strong degree of heat whilst surrounded by lapis calaminaris) also possesses that property; at least all the pieces of it, which I have tried, have that property.

I am, &c.

T. CAVALLO.



IV. On Infinite Series. By Edward Waring, M. D. F. R. S. Lucasian Professor of Mathematics at Cambridge.

# Read December 15, 1785.

- I. In the Paper, which the Royal Society did me the honour to print, on Summation of Series, is given a method of finding the fum of a feries, whose general term  $(\frac{P}{Q})$  (where  $\frac{P}{Q}$  is a fraction reduced to its lowest terms) is a determinate algebraical function of the quantity (z) the distance from the first term of the series, which always terminates when the sum of the series can be expressed in finite terms.
- 2. The terms of every infinite feries must necessarily be given by a function of z, or by quantities which can be reduced to a function of z.
- 3. Let  $Q = A \times A' \times A'^2 \times ...A''' \times B \times B' \times B'' \times ...B'''' \times C$   $C' \times C'^2 \times ...C'' \times \&c.$  where A',  $A'^2$ ,  $A'^3$ ...A''', are fuccessive values of A; that is, result from A by writing in it for z respectively z + 1, z + 2, z + 3, ...z + n; and B',  $B' \cdot '^2$ ,  $B' \cdot '^3$ , B'''', result from B, by writing in it for z respectively z + 1, z + 2, z + 3, ...z + m; but B is not a successive value of A; &c. Let the numerator  $P = E \cdot E' \cdot E'^2 \cdot E^{1b-1} \cdot F \cdot F' \cdot F'^2 \cdot ...F^{1-k-1} \times L$ ; E',  $E^{12} \cdot ...E^{1b-1}$ ; F',  $F^{1-k-1}$ , &c. denoting successive values of the quantities E, F, &c. respectively; and L, admitting of no divisor of the formula  $K \times K'$ , where K' is a successive V of  $L \times XV$ .

ceffive value of K: let  $L=A\times B\times C\times \&c.\times E^{th}\times F^{tk}\times \&c.\times p'\times q'\times r'\times \&c.-A^{tn}\times B^{tm}\times C^{tr}\times \&c.\times E\times F\times \&c.\times p\times q\times r\times \&c.$  where p', q', r', &c. are irrational quantities and fuccessive values of p, q, r, &c. The factors A B, C, &c.  $E^{th}$ ,  $E^{th}$ , &c. being given, the factors p, q', t', &c. into which they are multiplied in the quantity L will casily be deduced by deducting the preceding irrational factors contained in A, B, C, &c.  $E^{th}$ ,  $E^{th}$ , &c. from the correspondent irrational factors contained in L; and in the same manner, from the factors A'', B''', &c. E, F, &c. can be deduced the irrational factors of the preceding p, q, r, &c.

Assume for the sum of the series sought the quantity  $\frac{E \times E' \times E'' ... E^{th-1} \times F \times F'... F^{tk-1} \times \&c.}{A ... A' ... A^{ts} ... A^{tn-1} \times B \times B' \times B^{t-2} ... B^{tm-1} \times C \times C' ... C^{t-r-1} \times \&c.}$ 

- 4. This feries will terminate if the fum fought can be expressed by a finite determinate function of z; if not, it will proceed in infinitum, and may be expressed either by a feries ascending or descending according to the dimensions of z.
- 5. If any factor, A or B, or C, &c. have no fuccessive one in the denominator; or if the greatest dimensions of z in the denominator be greater than its greatest dimensions in the numerator by 1, then the sum of the series is not a finite algebraical function of z.

- 6. If in the denominator are deficient some intermediate successive factors, multiply both the numerator and denominator by those desicient sactors, and they are supplied: for example, let  $A \times A''' \times A'''' \times \&c$ . be sactors of the denominator, in which are desicient the sactors A', A'', A'''', &c. multiply both numerator and denominator by the content  $A' \times A'' \times A'''' \times \&c$ . and they are restored.
- - 8. If the greatest index of the content H is contained in one factor only, then the sum of the series cannot be expressed in finite terms of the quantity z.
  - 9. The same may be applied to the contents of the several successive values of the quantities B, C, &c. in the denominator: for example, let the general term be  $\frac{1}{1\cdot 2\cdot 3\cdot 2-2\times z}$ ; multiply it into z-1 to compleat the deficient term, and it results M 2

 $\frac{z-1}{1\cdot 2\cdot 3\cdot z}$ ; affume, by the preceding method for the fum of the feries the quantity  $\frac{1}{1\cdot 2\cdot 3\cdot z-1}$ , of which the fuccessive term is  $\frac{1}{1\cdot 2\cdot 3\cdot z}$ , and their difference  $\frac{1}{1\cdot 2\cdot z-1} - \frac{1}{1\cdot 2\cdot z}$  =  $\frac{1}{1\cdot 2\cdot z-2\times z}$  the given term.

- 2. Let the term be  $Ne^z$  and e less than  $\tau$ , which is the term of a geometrical series; then will the sum of the infinite series be  $\frac{N}{1-e} \times e^z$ , beginning from the term whose distance from the first is z; for the difference between the two successive sums  $= \frac{N}{1-e} (e^z e^{z+1}) = Ne^z$  the given term.
- 3. Let the general term be  $\frac{(z+n+1-e^n\times z+1)a}{z+1\cdot z+n+1}\times e^{z+1}$ ; affume for the fum of the feries the fubsequent quantity  $(z+1\cdot z+2\cdot z+3\cdot z+n)^{-1}\times e^z\times (\alpha+\beta z+\gamma z^2\cdot z^{n-1})$  and by the preceding method the co-efficients  $\alpha$ ,  $\beta$ ,  $\gamma$ , &c. may be found: the fum is known to be  $=\frac{a}{z+1}\times e^{z+1}+\frac{a}{z+2}\times e^{z+2}+\frac{a}{z+3}\times e^{z+3}$  $\cdot \cdot \cdot \frac{a}{z+n}e^{z+n}$ , which can easily be reduced to the preceding formula.

If the general term be  $\frac{T'-T}{T\times T'}$  or  $\frac{PQ'-QP'}{QQ'}$ ; where T and T', P and P', Q and Q', are successive terms; then will the sums of the series be  $\frac{I}{T}$  or  $\frac{P}{Q}$  properly corrected.

10. If the function expressing the general term contain in the denominator a factor or factors, which have no successive one; reduce the factor or factors into an infinite series proceeding according to the dimensions of z, and thence, by the method before given, find the sum of the series. The same method

may be purfued, when the denominator of a fluxion, which is a function of x multiplied into  $\dot{x}$  contains the simple power only of a factor or factors; reduce the factor or factors into an infinite series, proceeding according to the dimensions of x, and by the known methods find the fluent of the fluxion.

- 11. The fluent of the fluxion or fum of the series may be deduced also from the subsequent propositions, from which may be investigated many series, whose sums are known.
- 1. Let  $p\dot{P} = Q\dot{q}$ ,  $q\dot{Q} = R\dot{r}$ ,  $r\dot{R} = S\dot{s}$ ,  $s\dot{S} = T\dot{i}$ , &c.; then  $\int P\dot{p} = P\dot{p} Q\dot{q} + R\dot{r} S\dot{s} + T\dot{t} \&c$ . if only the feries converges.
- 2. Let pP' + p'P' = Qq', qQ' + q'Q' + = Rr', rR' + r'R' = Ss', sS' + s'S' = Tt', &c. where P', p', Q', q', &c. denote the increments of the quantities P, p, Q, q, &c. respectively, then will the integral of the increment (Pp') = Pp Qq + Rr Ss + &c. if only the series converges.

Ex. 1. 
$$\int x^{-n}\dot{x} = \int_{\frac{x^{n+m}}{x^{n+m}}}^{x^{m}\dot{x}} = \frac{1}{x^{n-1}} \left( \frac{1}{m+1} + \frac{n+m}{r'+1} A + \frac{n+r'}{s+1} B + \frac{n+s'}{t'+1} C + \frac{n+t'}{T+1} D + &c. \right) = \frac{1}{1-nx^{n-1}};$$
 whence  $\frac{1}{1-n} = \frac{1}{m+1} + \frac{n+m}{r'+1} \times \frac{1}{m+1}$   $\frac{n+r'}{s'+1} \times \frac{n+m}{r'+1} \times \frac{1}{m+1} + &c.$  In this example  $\dot{p} = x^{m}\dot{x}$ ,  $P = x^{-n-m}$ ,  $\dot{q} = x^{r}\dot{x}$ ,  $Q = x^{-n-r'}$ ,  $\dot{r} = x^{s}\dot{x}$ , &c.

Ex. 2.  $\int_{-\frac{x^{m}\dot{x}}{x^{n+r}}}^{x^{m}\dot{x}} = \int x^{m-n-r}\dot{x} = \frac{1}{m-n-r+1} x^{m-n-r+1} = x^{m-n-r+1} \left( \frac{1}{m+1} + \frac{1}{m+1} \times \frac{n+r}{m+2} + \frac{1}{m+1} \cdot \frac{n+r}{m+2} \cdot \frac{n+r+1}{m+3} + &c. \right);$  whence  $\frac{1}{m-n-r+1} = \frac{1}{m+1} + \frac{n+r}{m+2} A + \frac{n+r+1}{m+3} B + &c.$  In both these examples the letters A, B, C, &c., denote the preceding terms.

Ex. 3. 
$$\int_{\frac{x^{m}x}{1+x}}^{x^{m}x} = \frac{x^{m+1}}{1+x} \left( \frac{1}{m+1} + \frac{1}{m+1, m+2} \times \frac{x}{1+x} + \frac{2}{m+1, m+2, m+3} \times \frac{x^{2}}{(1+x)^{2}} + \frac{2 \cdot 3}{m+1 \cdot m+2 \cdot m+3 \cdot m+4} \cdot \frac{x^{3}}{(1+x)^{3}} + &c. \right)$$
Ex.

Ex. 4. 
$$\int_{(a+bx^{n}+c\lambda^{2n})^{b}} \frac{1}{m+1} \frac{a'x^{m+1}}{(a+bx^{n}+c\lambda^{2n})^{b}} + \frac{a'x^{m+1}}{m+1} \cdot (a+bx^{n}+cx^{2n})^{b+1}} \times \left(\frac{nbbx^{m-1}}{m+n+1} + \frac{2nbcx^{2n-1}}{m+2n+1}\right) + \&c.$$
12. Let the general term of an infinite feries be 
$$\frac{A}{m+n+1} = \frac{A}{m+2n+1} + \frac{2nbcx^{2n-1}}{m+2n+1} + \frac{A}{m+2n+1} + \frac{A}{m+2n$$

 $\frac{1}{\times \delta - \gamma \cdot \delta - \gamma + 1 \cdot \cdot \cdot \delta - \gamma + 1 \times \&c.}$  - &c. = 0, &c. = 0; or, to explain it otherwise, assume the quantities  $\alpha$ ,  $\alpha + 1$ ,  $\alpha + 2$ ,  $\alpha + 3$ , ...  $\alpha+n$ ;  $\beta$ ,  $\beta+1$ ,  $\beta+2$ ,  $\beta+m$ ;  $\gamma$ ,  $\gamma+1$ ,  $\gamma+2$ ,  $\gamma+r$ ;  $\delta$ ,  $\delta+1$ ,  $\delta+2$ ,  $\delta+3$ ; &c. Subtract one  $\alpha$  from all the remaining quantities  $\alpha+1$ ,  $\alpha+2$ ,  $\alpha+n$ ;  $\beta$ ,  $\beta+1$ ,  $\beta+m$ ;  $\gamma, \gamma+1, \ldots \gamma+r$ ;  $\delta, \delta+1, \ldots \delta+s$ ; &c. and multiply all the differences resulting 1, 2, 3, .. n;  $\beta - \alpha$ ,  $\beta - \alpha + 1$ , ..  $\beta - \alpha + m$ ;  $\gamma-\alpha$ ,  $\gamma-\alpha+1$ ,  $\gamma-\alpha+2$ ,  $\gamma-\alpha+r$ ;  $\delta-\alpha$ ,  $\delta-\alpha+1$ , ...  $\delta - \alpha + s$ , &c. into each other, and call the content  $p^{\alpha}$ . In the fame manner fubtract a + 1 from all the remaining quantities a,  $\alpha+2$ ,  $\alpha+3$ ,  $\alpha+n$ ;  $\beta$ ,  $\beta+1$ ,  $\beta+m$ ;  $\gamma$ ,  $\gamma+1$ ,  $\beta+r$ ;  $\delta$ ,  $\delta+1$ ,... $\delta+s$ ; &c.; and let the remainders -1, 1, 2, 3, ...n-1;  $\beta-\alpha-1$ ,  $\beta-\alpha$ ,  $\beta-\alpha+1$ ,  $\beta-\alpha+m-1$ ;  $\gamma-\alpha-1$ ,  $\gamma-\alpha$ ,  $\gamma-\alpha+1,\ldots\gamma-\alpha+r-1;\delta-\alpha-1,\delta-\alpha,\delta-\alpha+1,\ldots\delta-\alpha+s-1,$ &c. be multiplied together, and their content be called pa+x. In the same manner subtract  $\alpha+2$ ,  $\alpha+3$ ,  $\alpha+n$  respectively from all the remaining quantities, and let the differences refulting fulting be multiplied together, and their respective contents be called  $p^{n+2}$ ,  $p^{n+3}$ ,  $p^{n+4}$ , ...  $p^{n+n}$ ; then, if the sum of the series can be found, will  $\frac{1}{p\alpha} + \frac{1}{p\alpha+1} + \frac{1}{p\alpha+2} + \frac{1}{p\alpha+3} \cdot \cdot \cdot \cdot \frac{1}{p\alpha+n} = 0$ .

In the same manner subtract  $\beta$ ,  $\beta+1$ ,  $\beta+2$ ,  $\beta+m$  respectively from all the remaining quantities, and multiply their respective remainders into each other, and call their contents respectively  $p^{\beta}$ ,  $p^{\beta+1}$ ,  $p^{\beta+2}$ ,  $p^{\beta+m}$ , then will  $\frac{1}{p\beta} + \frac{1}{p\beta+1} + \frac{1}$ 

$$\frac{1}{p\beta+2}\cdot\cdot\frac{1}{p\beta+m}=0.$$

Subtract  $\gamma$ ,  $\gamma + 1$ ,  $\gamma + 2$ ,  $\gamma + r$  respectively from all the remaining quantities, and multiply their respective remainders into each other, and call their contents respectively  $p^{\gamma}$ ,  $p^{\gamma+r}$ ,  $p^{\gamma+r}$ ; then will  $\frac{1}{p_{\gamma}} + \frac{1}{p_{\gamma+1}} + \frac{1}{p_{\gamma+2}} \cdot \frac{1}{p_{\gamma+r}} = 0$ .

Subtract  $\delta$ ,  $\delta + 1$ ,  $\delta + 2$ , ...  $\delta + s$  from all the remaining quantities, and multiply their respective remainders into each other, and call their contents respectively  $p^{\delta}$ ,  $p^{\delta+1}$ ,  $p^{\delta+2}$ ,  $p^{\delta+1}$ ; then will  $\frac{1}{p^{\delta}} + \frac{1}{p^{\delta}+1} + \frac{1}{p^{\delta}+2} + \frac{1}{p^{\delta}+s} = 0$ ; and so on; and, vice versa, if the sum of the above-mentioned fractions be respectively = 0; then the sum of the series, whose general term is the given one, can be found; otherwise not.

13. If the fum of the feries, whose general term is  $z+\alpha \cdot z+\alpha+1 \cdot z+\alpha+n \times z+\beta \cdot z+\beta+1 \cdot z+\beta+m \times z+\gamma \cdot z+\gamma+1 \cdot x+\gamma+r \times z+\beta+r \times z+\beta+r \times z+\gamma+r \times z+\gamma+r$ 

14. Let

14. Let  $A \times \overline{z+\beta} \cdot \overline{z+\gamma} \cdot \overline{z+\delta} \times \overline{z+\varepsilon} \times \&c. + B \times \overline{z+\alpha} \times \overline{z+\gamma} \cdot \overline{z+\delta} \cdot \overline{z+\varepsilon} \cdot \&c. + C \times \overline{z+\alpha} \cdot \overline{z+\beta} \times \overline{z+\delta} \cdot \overline{z+\varepsilon} \cdot \&c. + D \times \overline{z+\alpha} \cdot \overline{z+\beta} \cdot \overline{z+\gamma} \cdot \overline{z+\delta} \cdot \overline{z+$ 

15. Let the general term of a feries be  $\frac{1}{H} \times e^x$ , where e is less than 1; the sum of the series can be expressed in finite terms, when the above-mentioned quantities  $\frac{1}{px} + \frac{\frac{1}{e}}{px+1} + \frac{\frac{1}{e^x}}{px+2}$ 

$$+\frac{\frac{1}{e^{3}}}{p\alpha+3}\cdot\cdot+\frac{\frac{1}{e^{n}}}{p\alpha+n}=0, \frac{1}{p\beta}+\frac{\frac{1}{e}}{p\beta+1}+\frac{\frac{1}{e^{2}}}{p\beta+2}+\frac{\frac{1}{e^{3}}}{p\beta+3}\cdot\cdot\cdot+\frac{\frac{1}{e^{n}}}{p\beta+m}=0,$$

$$\frac{1}{p\gamma}+\frac{\frac{1}{e}}{p\gamma+1}+\frac{\frac{1}{e^{2}}}{p\gamma+2}\cdot\cdot\cdot\frac{\frac{1}{e^{n}}}{p\gamma+r}=0, \frac{1}{p\delta}+\frac{\frac{1}{e}}{p\delta+1}+\frac{\frac{1}{e^{n}}}{p\delta+2}+\frac{\frac{1}{e^{3}}}{p\delta+2}\cdot\cdot\cdot$$

 $\frac{e}{n^2+s}=0$ , &c.=0. This never happens unless e=1.

16. If the general term be any rational function of z into the exponential  $e^z$ , viz.  $\frac{az^l + bz^{l-1} + cz^{l-2} + &c}{z + a + b \times z + a + k \times &c} \times z + a + b \times z + a + k \times c$ 

where b, b', b'', &c. k, k', &c. l, m, m', &c. n, n', &c. &c. &c. denote whole numbers, and neither n, where n is a constant n, and n is a constant n, where n is a constant n is a constant n, where n is a constant n is a constant n, where n is a constant n, where n is a constant n is a const

 $\alpha - \beta$ , nor  $\alpha - \gamma$ , nor  $\beta - \gamma$ , &c. are whole numbers: let m be the greatest of the indices m, m', m'', &c.; n the greatest of the indices n, n', n'', &c.; r the greatest of the indices r, r', r'', &c.; then, from the sums of the series given, whose general

terms are 
$$\frac{e^{z}}{(z+\alpha)^m}$$
,  $\frac{e^{z}}{(z+\alpha)^{m-1}}$ ,  $\frac{e^{z}}{(z+\alpha)^{m-2}}$ ,  $\frac{e^{z}}{(z+\alpha)^{m-2}}$ ,  $\frac{e^{z}}{(z+\alpha)^{n}}$ ,  $\frac{e^{z}}{(z+\alpha)^{n}}$ ,  $\frac{e^{z}}{(z+\alpha)^{n}}$ ,  $\frac{e^{z}}{(z+\gamma)^{n}}$ ,  $\frac{e^{z}}{(z+\gamma)^{n}}$ ,  $\frac{e^{z}}{(z+\gamma)^{n-1}}$ ,  $\frac{e^{z}}{(z+\gamma)^{n}}$ , &c. can be deduced the funt of the above feries, whose general term is given above; multiply each of these terms into unknown coefficients  $e'$ ,  $f$ ,  $g$ ,  $h$ , &c. then reduce them to a common denominator, which is the same as the denominator of the given general term, and add them together, and make the correspondent terms of the numerator  $\frac{e^{z}}{(z+\gamma)^{n}}$ ,  $\frac{e^{z}}{(z+\gamma)^{n-1}}$ , &c. of the given general term; and from the equations resulting can be deduced the co-efficients  $e'$ ,  $f$ ,  $g$ ,  $h$ , &c. and thence from the given sums the sum of the series required.

Approximations to the fums of the ferreses may be deduced from the methods given in the Meditationes Analytica. The sum of some sew cases have been given from the periphery of the circle: for example, when  $\alpha$  and m are whole numbers, and e=1; or; more particularly, when m=2 and  $e=\frac{1}{2}$ , and some other particular cases, which may be with nearly the same facility calculated from approximations; the cases given indeed are so sew, unless when e=1, that they can very rarely be applied:

17. If the dimensions of z in the numerator be equal or greater than its dimensions in the denominator; that is, l be equal or greater than m+m'+m''+&c.+n+n'+n''+&c.+r+r'+r''

4 &c. &c. reduce the fractions to a mixed number, so that the dimensions of z in the numerator of the fraction be less than its dimensions in the denominator, and the integral part be  $Ae^{\alpha} + Bze^{\alpha} + Cz^{2}e^{\alpha} + Dz^{3}e^{\alpha} + \dots + Hz^{1m}e^{\alpha}$ : the fum of the infinite feries whose term is  $Ae^z + Bze^z + Cz^2e^z + Dz^3e^z + Ez^4e^z + \dots$  $+ \mathbf{H} \mathbf{z}^{\mathbf{w}} e^{\mathbf{z}} = \frac{\mathbf{A}e}{1-e} + \mathbf{B} \left( \frac{\mathbf{I}}{(1-e)^2} - \frac{\mathbf{I}}{1-e} \right) + \mathbf{C} \left( \frac{\mathbf{I} \cdot \mathbf{2}}{(1-e)^2}, -\frac{\mathbf{I}}{(1-e)^2} \right) + \mathbf{D}e$  $\left(\frac{1\cdot 2\cdot 3}{(1-\epsilon)^4} - \frac{1+2\times 1\cdot 2}{(1-\epsilon)^3} + \frac{1}{(1-\epsilon)^2}\right) + \text{E}e\left(\frac{1\cdot 2\cdot 3\cdot 4}{(1-\epsilon)^5} - &c\right)$ : the fum of a feries (whose general term is  $z^m c^z$ ) =  $\frac{1 \cdot 2 \cdot 3 \cdot 4 \cdot m}{(1-\epsilon)^{m+1}} e^{-\frac{1}{2}}$  $\frac{{}^{1}S^{m-1}}{(1-\epsilon)^{m}} \times 2 \cdot 3 \cdot m - 1c + \frac{{}^{1}S^{m-1} \times {}^{1}S^{m-2} - {}^{2}S^{m-1}}{(1-\epsilon)^{m-1}} \times 1 \cdot 2 \cdot 3 \cdot \overline{m-2} \cdot \epsilon$  $\cdots + \frac{L}{(1-\epsilon)^{m-b}} \times 1 \cdot 2 \cdot 3 \cdot (m-b-1) \cdot (\pm \frac{1}{(1-\epsilon)^2})$ , where Lis equal to the fum of all quantities of the following fort,  $=S^{m-1}\times^{\beta}S^{m-\alpha-1}\times^{\gamma}S^{m-\alpha-\beta-1}\times^{\beta}S^{n-\alpha-\beta-\gamma-1}S^{n-\alpha-\beta-\gamma-1}\times^{\beta}S^{n-\alpha-\beta-\gamma-1}\times^{\beta}S^{n-\alpha-\beta-\gamma-1}\times^{\beta}S^{n-\alpha-\beta-\gamma-1}\times^{\beta}S^{n-\alpha-\beta$ where  $\alpha$ ,  $\beta$ ,  $\gamma$ ,  $\delta$ , &c. are whole affirmative numbers; (in the preceding notation by Sis defigned the fum of the contents of every  $\pi$  of the following numbers 1, 2, 3, 4, 5, ... e); and  $\alpha + \beta + \gamma + \delta + \varepsilon + &c. = b + 1$ ; the above-mentioned pro $duct *S^{m-1} \times {}^{\beta}S^{m-\alpha-1} \times &c.$  is to be taken affirmative or negative, according as the number of letters α, β, γ, δ, &c. is even or uneven.

The fum of the feries  $z^m \times e^z$  may also be found by affurning for it  $(az^m + bz^{m-1} + cz^{m-2} + dz^{m-3} \dots k)e^z$ ; then, finding its fuccessive term  $(a \times z + 1 e + bz + 1 e + cz + 1 e + &c.) e^z$ , and taking the difference between it and the affurned quantity, there results  $(a \times e - 1 z^m + mae + be - 1 z^{m-1} + &c.)e^z$ ; by equating it to the given term  $z^m e^z$  are deduced the subfequent equations  $a \times e - 1 = 1$ , mae + be - i = 0, &c. whence N = 1 + ac

$$a = \frac{1}{e-1}, b = \frac{1}{e} - ma, &c.$$

If e=1, then affume  $az^{m+1}+bz^m+&c$ . for the fum fought, which rule was first taught by M. J. Bernoulli.

If the term be  $z^m f^{bz}$ ; for  $f^b$  substitute e, and there results  $z^m e^z$  the same as before.

18. Let  $P = A + Bx^n + Cx^{2n} + Dx^{3n} + &c.$  then will the fum of the feries  $\frac{A}{\alpha \cdot \beta \cdot \gamma \cdot \delta \cdot &c.} + \frac{Bx^n}{\alpha + n \cdot \beta + n \cdot \gamma + n \cdot &c.} + \frac{Bx^n}{\alpha + n \cdot \beta + n \cdot \gamma + n \cdot &c.}$ 

$$\frac{Cx^{2n}}{\alpha+2n\cdot\beta+2n\cdot\gamma+2n\cdot\&c.} + \&c. = \frac{1}{\alpha\beta\gamma\delta,\&c.} \times P - \frac{1}{\alpha} \cdot \frac{1}{\beta-\alpha} \cdot \frac{1}{\gamma-\alpha}.$$

$$\frac{1}{\delta-\alpha} \cdot \times \&c. x^{-\alpha} \int x^{\alpha} \dot{p} - \frac{1}{\beta} \cdot \frac{1}{\alpha-\beta} \cdot \frac{1}{\gamma-\beta} \cdot \frac{1}{\delta-\beta} \cdot \&c. x^{-\beta} \int x^{\beta} \dot{p} - \frac{1}{\gamma} \cdot \frac{1}{\alpha-\gamma} \cdot \frac{1}{\beta-\gamma} \cdot \&c. \times x^{-\gamma} \int x^{\gamma} \dot{p} - \&c.$$

This may be proved from the subsequent arithmetical proposition  $\frac{1}{\alpha} \cdot \frac{1}{\beta - \alpha} \cdot \frac{1}{\gamma - \alpha} \cdot \frac{1}{\delta - \alpha} \cdot &c. + \frac{1}{\beta} \cdot \frac{1}{\alpha - \beta} \cdot \frac{1}{\gamma - \beta} \cdot \frac{1}{\delta - \beta} \cdot &c. + \frac{1}{\gamma} \cdot \frac{1}{\alpha - \gamma} \cdot \frac{1}{\beta - \gamma} \cdot \frac{1}{\delta - \gamma} \cdot &c. + \frac{1}{\beta} \cdot \frac{1}{\alpha - \beta} \cdot \frac{1}{\beta - \gamma} \cdot \frac{1}{\gamma - \delta} \cdot &c. =$ 

α.β.γ.δ.&c.

19. Let the general term of the above-mentioned feries  $A + Bx^{2n} + Cx^{2n} + &c$ . be  $Hx^{2n}$ ; then from the fums of the feries p, and the fluents of the fluxions  $x^{n}p$ ,  $x^{n}p$ ,  $x^{n}p$ ,  $x^{n}p$ , &c. being given there follows the fum of a feries, whose general term is  $\frac{ax^{2n} + bx^{2n-1} + cx^{2n-2} + &c}{x + nx \cdot \beta + nx \cdot \delta + nx \cdot &c} \times Hx^{2n}$ , where l denotes a whole number.

If  $H = m \cdot \frac{m-1}{2} \cdot \frac{m-2}{3} \cdot \cdot \cdot \frac{m-z}{z+1}$ , or  $= m \cdot \frac{m-1}{2} \cdot \frac{m-2}{3} \cdot \cdot \cdot \frac{m-1}{2}$ , where l is a whole number, and m,  $\alpha'$ ,  $\beta'$ ,  $\gamma'$ , &c. are either whole numbers or fractions whose denominator is 2, and  $\alpha = \alpha' n$ ,  $\beta = \beta' n$ , &c. the sum of the above-mentioned series can be found by finite terms, circular arcs and logarithms.

If  $H = \frac{1}{1 \cdot 2 \cdot 3 \cdot . \cdot z}$  or  $= \frac{1}{1 \cdot 2 \cdot 3 \cdot . \cdot lz}$ , and  $l, \alpha, \beta, \gamma$ , &c. whole numbers and n = 1; then can the fum of any feries of the above-mentioned formula be found in finite algebraical functions of x, and the circular arcs and logarithms of them.

## PART IL

arly known in the æra of science; for when men could not find the exact value of a quantity, they were induced to find near approximations by trials, and from thence, by proportion, an approximation still nearer: which method is commonly denominated the Rule of False.

This was often found to deviate confiderably from the exact value; and the same operation was repeated, which frequently produced a nearer approximate value, and so on.

This method of approximations, the most general yet known, has been used in resolving problems by several of the most eminent mathematicians in different ages, and in this particularly by M. Euler.

2. The following observation, I believe, was first published: in the *Meditationes*, in the year 1770, viz. that the convergency of the approximate values, found by the rule of false and method of infinite series, generally depended on this, viz.

how.

how much nearer the approximate assumed is to one value of the quantity fought possible or impossible than to any other, and not to the quantity itself: hence, when two or more (n) values of the quantity fought are nearly equal, it is necessary to recur to more difficult rules, viz. to three or more trials; as, for example, let two roots be nearly equal, and write a,  $a + \pi$ , and  $a + \varrho$ , for the unknown quantity in the given equation made =0, and let the quantities refulting be A, B, and C, then will more near approximations to the two roots nearly equal of the given equation be a + the two roots(x) of the quadratic  $\left(\frac{A}{\pi \rho} + \frac{B}{\pi (\pi - \rho)} + \frac{C}{\rho (\rho - \pi)}\right) x^2 - \left(A \times \frac{\pi + \rho}{\pi \rho} + B \times \frac{\rho}{\pi \cdot (\pi - \rho)} + \frac{C}{\rho \cdot (\pi - \rho)}\right)$  $\frac{C\pi}{\rho \cdot (\rho - \pi)}$ ) x + A = 0: for write o,  $\pi$ , and  $\rho$ , respectively for x in

the equation, and there will refult the quantities A, B, and C.

More generally, substitute for x in the given equation the quantities a,  $a + \pi$ ,  $a + \rho$ ,  $a + \sigma$ ,  $a + \tau$ ,  $a + \nu$ , &c. where  $\pi$ ,  $\rho$ ,  $\sigma$ ,  $\tau$ , &c. are very fmall quantities; and let the quantities resulting be A, B, C, D, E, F, &c.; then will more near approximations to the (n) roots of the given equation be  $a + \alpha$ ,  $a + \beta$ ,  $a + \gamma$ ,  $a + \delta$ , &c. where  $\alpha$ ,  $\beta$ ,  $\gamma$ ,  $\delta$ , &c. &c. are the *n* roots (e) of the given equation  $\frac{(e-\pi)(e-\xi'(e-\sigma)(e-\tau)\&c.}{\pm \pi e \sigma \tau,\&c.} \times A + \frac{e(e-\xi)(e-\sigma)(e-\tau)\&c.}{\pi(\pi-\xi)(\pi-\sigma)(\pi-\tau)\&c.}$  $\times \mathbf{B} + \frac{e(e-\pi)(e-\sigma)(e-\tau) & \mathbf{c.}}{e(e-\pi)(e-\sigma)(e-\tau) & \mathbf{c.}} \times \mathbf{C} + & \mathbf{c.} = \mathbf{A} - \left(\frac{\mathbf{A}}{\pi} - \frac{\mathbf{B}}{\pi}\right) e + \left(\frac{\mathbf{A}}{\pi_e} + \frac{\mathbf{A}}{\pi}\right) e + \left(\frac{\mathbf{A}}{\pi} - \frac{\mathbf{B}}{\pi}\right) e + \left$  $\frac{B}{\pi(\pi-e)} + \frac{C}{e(e-\pi)} \times e \cdot e^{-\pi} - \left(\frac{A}{\pi e^{\sigma}} - \frac{B}{\pi(\pi-e)(\pi-\sigma)} - \frac{C}{e(e-\pi)(\rho-\sigma)}\right)$  $\frac{D}{\sigma(\sigma-\pi)(\sigma-\xi)}\Big)\times e\cdot \overline{e-\pi}\cdot \overline{e-\rho} + \Big(\frac{A}{\pi\rho\sigma\tau} + \frac{B}{\pi(\pi-\xi)(\pi-\sigma)(\pi-\tau)} + \frac{B}{\sigma(\pi-\xi)(\pi-\sigma)(\pi-\tau)}\Big)$  $\frac{C}{\ell(\ell-\tau)(\ell-\sigma)(\ell-\tau)\&c.} + \frac{D}{\sigma(\sigma-\tau)(\sigma-\ell)(\sigma-\tau)\&c.} + \frac{E}{\tau(\tau-\tau)(\tau-\ell)(\tau-\sigma)\&c.}$  $\overline{e - \pi} \cdot \overline{e - \varrho} \cdot \overline{e - \sigma} - \left(\frac{A}{\pi \varrho \sigma \tau \nu} - \frac{B}{\pi (\pi - \varrho)(\pi - \sigma)(\pi - \tau)(\pi - \nu)} - \frac{C}{\varrho (\varrho - \pi)(\varrho - \sigma)}\right)$ 

$$\frac{D}{(\xi-r)(\xi-v)} = \frac{1}{\sigma(\sigma-\pi)(\sigma-\xi)(\sigma-\tau)(\sigma-\nu)} = \frac{1}{\tau(\tau-\tau)(\tau-\xi)(\tau-\sigma)(\tau-\nu)} = \frac{F}{v(v-\pi)(v-\sigma)(v-\tau)} e \cdot \overline{e-\pi} \cdot \overline{e-\rho} \cdot \overline{e-\sigma} \cdot \overline{e-\tau} + \&c = 0.$$

Their refolutions were first given in the Meditationes Analyticæ, published in the year 1774, and require the extraction of a quadratic, cubic, and in general of an equation of (n) dimensions; which rules will often give a nearer approximate than the preceding, when the roots are not nearly equal.

3. These rules may be applied to find approximations to the roots of algebraical equations: for example, let the algebraical equation be  $x^n - px^{n-1} + qx^{n-2} - &c. = 0$ , substitute in it for a two quantities a, and a + e much nearer to one root than to any other, and there result  $a^n - pa^{n-1} + qa^{n-2} - &c = A$ , and  $(a + e)^n - p(a + e)^{n-1} + q(a + e)^{n-2} - &c. = B$ ; then, by the rule of

false, B-A: 
$$e:: A: \frac{a^n - pa^{n-1} + qa^{n-2} - &c.}{(na^{n-1} - n - 1pa^{n-2} + n - 2qa^{n-3} - &c.) + &c.}$$

whence a-b a near approximate value to the root fought. If the quantities, in which are involved  $e, e^2, e^3, &c.$  on account of e being very small, be rejected, then will the approximate fought b=

 $\frac{a^n - pa^{n-1} + qa^{n-2} - &c.}{na^{n-1} - n - 1pa^{n-2} + n - 2qa^{n-3} - &c.}$ ; which will nearly be the same as found, where a near approximate is given, from the method given by Vieta, Harriot, Oughtred, Newton, De Lagny, Halley, &c.

- 4. From this expression it follows, that if (a) be a root of the equation  $na^{n-1} \overline{n-1}pa^{n-2} + &c. = 0$ , of which the roots are limits between the roots of the given equation, the approximation found will be infinite.
- 5. In finding these approximations, when there are two or more quantities contained in the given equation dependent on

each other, as the arc and the fine, it is necessary that both should be corrected in every approximation to such a degree as the subsequent approximations require.

6. In the Meditationes it is observed, that in any algebraical equation  $x^n - ax^{n-1} + bx^{n-2} - cx^{n-3} + dx^{n-4} - ex^{n-5} = \pm yx^{n-m+1} = -x^{n-1}$  $bx^{n-m} \pm kx^{n-m-1} = lx^{n-m-2} \pm \&c. = 0$ , if a be much greater than  $\frac{b}{a}$ , and  $\frac{b}{a}$  has to  $\frac{c}{b}$  a much greater ratio than  $a:\frac{b}{a}$ ; and in the fame manner  $\frac{c}{b}$  has to  $\frac{d}{c}$  a much greater ratio than  $\frac{b}{a}$ :  $\frac{c}{b}$ , To on; then will a be a near approximate to the greatest root of the algebraical equation;  $\frac{b}{a}$  a near approximate to the second;  $\frac{\epsilon}{k}$  a near approximate to the third, and  $\frac{k}{k}$  a near approximate to a root, which is much less than m roots of the given equation, but much greater than the remaining (n-m-1) roots.

If the equation above-mentioned  $x^n \pm ax^{n-1} + &c. = 0$ , or which is the same,  $1 \pm \frac{a}{x} + \frac{b}{x^2} \pm \&c. = 0$  be infinite; then will, in like manner, all its roots be possible and their approximate values  $a, \frac{b}{a}, \frac{c}{b}$ , &c. as before.

This easily appears by substituting for a, b, c, &c. their values in terms of the root of the equation.

- 7. A nearer approximate to the above-mentioned root will be  $\frac{k}{h} - \left(\frac{l}{k} - \frac{g k^2}{k^3}\right) + \&c.$
- 8. Equations, of which the fluxions of the quantities contained in the given equations can be found, may be reduced to infinite algebraical equations, in which is involved no irrational function of the unknown quantities contained in the given equations by the incremental theorem; viz. let A = 0 be the given equation

equation, and (a) an approximate much more near to the root required ( $\pi$ ) of the given equation than to any other: write a for (x) the unknown quantity fought in the subsequent quantities, A,  $\frac{\dot{A}}{\dot{x}}$ ,  $\frac{\ddot{A}}{\dot{x}^2}$ ,  $\frac{\ddot{A}}{\dot{x}^3}$ , &c.; and let there result the correspondent quantities  $\alpha$ ,  $\beta$ ,  $\gamma$ ,  $\delta$ , &c.; then will  $\pi - a$  be a root (e) of the infinite equation  $\alpha \pm \beta e + \frac{1}{1 \cdot 2} \gamma e^2 \pm \frac{r}{1 \cdot 2 \cdot 3} \delta e^3 + \frac{1}{1 \cdot 2 \cdot 3 \cdot 4} \epsilon e^4 \pm \delta c$ . = 0, of which a root of the equations  $\alpha \pm \beta e = 0$ ,  $\alpha \pm \beta e + \frac{1}{1 \cdot 2} \gamma e^2 = 0$ , &c. will be an approximate. If two roots of the given equation are nearly = a, then it is necessary to recur to an equation not inferior to a quadratic.

9. The fuccessive approximate values found by these and like rules will ultimately be to each other in a greater than any geometrical ratio: for example, let  $\frac{as}{a+s}$  be an approximate to a root of the quadratic  $x^2 - (a+s)x + as = 0$ , then will the new addition to the approximate to the root s found by the common method at the distance n-1 from the first approximate be  $\frac{sb}{a^b-1}$  nearly, where  $b=2^{n-1}$ .

10. Let an equation  $x^n - Px^{n-1} + Qx^{n-2} - Rx^{n-3} + Sx^{n-4} - &c.$ = 0, of which the roots are a, b, c, d, &c.; and an equation  $x^n - px^{n-1} + qx^{n-2} - rx^{n-3} + sx^{n-4} - &c.$  = 0, where p, q, r, s, &c. differ from the co-efficients P, Q, R, S, &c. by very small quantities: assume the (n) equations  $\pi + \rho + \sigma + \tau + &c. = p - P$ =  $\alpha$ ,  $a\pi + b\varrho + c\sigma + d\tau + &c. = P\alpha - q + Q = \beta$ ,  $a^2\pi + b^2\varrho + c^2\sigma + d^2\tau + &c. = P\beta - Q\alpha + r - R = \gamma$ ,  $a^3\pi + b^3\rho + c^3\sigma + d^3\tau + &c. = P\gamma - Q\beta + R\alpha - s + S = \delta$ , &c.; and from them find the unknown quantities  $\pi$ ,  $\varrho$ ,  $\sigma$ ,  $\tau$ , &c; then will  $a + \pi$ ,  $b + \varrho$ ,  $c + \sigma$ ,  $d + \tau$ , &c. be nearly the n roots of the equation  $x^n - px^{n-1} + qx^{n-2}$ . Vol. LXXVI.

-&c.=c, and confequently  $\pi, \varrho, \&c.$  nearly  $-\frac{a^n - pa^{n-1} + qa^{n-2} - \&c.}{na^{n-1} - n - 1pa^{n-2} + \&c.}$ ,

 $-\frac{b^n-pb^{n-1}+qb^{n-2}-&c}{nb^{n-1}-n-1pb^{n-2}+&c}$ , &c.; whence the convergency of the approximate values found by this rule depends on the principle before delivered.

10. Let there be given (m) equations, which contain m unknown quantities x, y, z, &c.; and let  $\alpha$ ,  $\beta$ ,  $\gamma$ , &c. be nearly correspondent values of the unknown quantities x, y, &c. respectively: assume n + 1 different values of the quantity x, viz.  $\alpha$ ,  $\alpha + \pi$ ,  $\alpha + \pi'$ ,  $\alpha + \pi''$ , &c. &c.; and in like manner affirme n+1 different correspondent values of the quantity y, which let be  $\beta$ ,  $\beta + \varrho$ ,  $\beta + \rho'$ ,  $\beta + \rho''$ , &c.; and so of the remaining; where  $\pi$ ,  $\pi'$ ,  $\pi''$ , &c.  $\rho$ ,  $\rho'$ , &c. &c. are very small quantities; substitute these quantities for their respective values in the given equations, and let the refulting quantities be A, B, C. D, &c. in the first equation; P, Q, R, S, &c. in the second, &c. &c.: assume from the first equation the n simple equations  $a\pi + b_{\ell} + \&c. = B - A$ ,  $a\pi' + b_{\ell}' + \&c. = C - A$ ,  $a\pi'' + b_{\ell}'' + \&c.$ =D-A, &c.; and from the fecond equation the n simple ones  $b\pi + k_{\ell} + \&c. = Q - P$ ,  $b\pi' + k_{\ell}' + \&c. = R - P$ ,  $b\pi'' + k_{\ell}''$ +&c.=S-P, &c. From these equations can be investigated the co-efficients a, b, &c. b, k, &c. &c.; ultimately affume the m equations A + ae + bi + &c. = 0, P + be + ki + &c. = 0, &c. from which can be deduced the values of the quantities e, i, &c.; and  $\alpha + \epsilon$ ,  $\beta + i$ , &c. will be more near values of the quantities, x, y, &c.

power of each of the roots of a given equation, and then extracted the  $2n^{th}$  root of A, viz.  $\sqrt[2n]{A}$  for an approximate value of the greatest root of the equation, and further added some similar rules on the same principle.

In the Miscell. Analyt. and Meditationes the same principle is applied in different rules for finding approximates to the greatest and other roots of the given equation; and also limits of the ratios of the approximate values of the roots found by these rules to the roots themselves are given.

It is observed in the *Meditationes*, that from these rules in general to find the greatest root, it is often necessary that the greatest possible root be greater than the sum of the quantities contained in the possible and impossible part of any impossible root of the given equation: for example, if  $a+b\sqrt{-1}$  be an impossible root of the given equation, then it is necessary that the greatest possible root be greater than a+b.

It may further be observed, that in equations of high dimenfions (unless purposedly made) it is probable, the number of impossible will greatly exceed the number of possible roots; and consequently these rules most commonly fail.

12. M. BERNOULLI affumed a fraction whose numerator is a rational function of the unknown quantity, and denominator the quantity, which constitutes the equation; and reduced the fraction into a series, whose terms proceed according to the dimensions of the unknown quantity; and thence found an approximate value of the greatest or least root of the given equation or its reciprocal, by dividing the co-efficient of any term of the series resulting by the co-efficient of the preceding or subsequent term: for example, let the equation be  $x^n - px^{n-1} + qx^{n-2} - rx^{n-3} + sx^{n-4} \cdot ... \pm Px^3 \mp Qx^2 \pm Rx \mp S = 0$ ; as

fume the fraction 
$$\frac{nx^{n-1}-n-1px^{n-2}+n-2qx^{n-3}-z-3rx^{n-4}+8xc.}{x^n-px^{n-1}+qx^{n-2}-rx^{n-3}+8xc.}$$

$$nx^{-1}+(\alpha+\beta+\gamma+\delta+8xc.)x^{-2}+(\alpha^2+\beta^2+\gamma^2+\delta^2+\epsilon^2+8xc.)$$

$$x^{-3}+(\alpha^3+\beta^3+\gamma^3+\delta^3+\epsilon^3+8xc.)x^{-4}+(\alpha^4+\beta^4+\gamma^4+\delta^4+\epsilon^4+8xc.)$$
O 2

&c.)
$$x^{-3}$$
.... +  $(\alpha^{m-1} + \beta^{m-1} + \gamma^{m-1} + \&c. = P)x^{-m} + (\alpha^{m} + \beta^{m} + \gamma + \&c. = Q)x^{-m-1} + (\alpha^{m+1} + \beta^{m+1} + \gamma^{m+1} + \&c. = R)x^{-m-2} + &c.$ ; then will  $\frac{R}{Q}$  or  $\sqrt[m]{Q}$  be the greatest root nearly.

Ex. 2. 
$$\frac{R-2Qx+3Px^2-&c...nx^{n-1}}{S-Rx+Qx^2-Px^3+&c...x^n} = (\frac{1}{\alpha} + \frac{1}{\beta} + \frac{1}{\gamma} + &c.) + (\frac{1}{\alpha^2} + \frac{1}{\beta^2} + \frac{1}{\sqrt{2}} + \frac{1}{\delta^2} + &c.)x + (\frac{1}{\alpha^3} + \frac{1}{\beta^3} + \frac{1}{\gamma^3} + &c.)x^2 + (\frac{1}{\alpha^4} + \frac{1}{\beta^1} + \frac{1}{\gamma^4} + &c.)x^3 + ... + (\frac{1}{\alpha^{m-1}} + \frac{1}{\beta^{m-1}} + \frac{1}{\gamma^{m-1}} + &c. = P)x^{m-2} + (\frac{1}{\alpha^m} + \frac{1}{\beta^m} + \frac{1}{\gamma^m} + &c. = Q)x^{m-1} + (\frac{1}{\alpha^{m+1}} + \frac{1}{\beta^{m+1}} + \frac{1}{\gamma^{m+1}} + &c.)x^m + &c. then will  $\frac{P}{Q}$  or  $\sqrt[m]{1}$ , the least root nearly.$$

Ex. 3. 
$$\frac{1}{x^{n}-\rho x^{n-1}+qx^{n-2}-\&c.} = x^{-n} + (\alpha+\beta+\gamma+\delta+\&c.)x^{-n-1}$$

$$+ (\alpha^{2}+\beta^{2}+\gamma^{2}+\&c.(+\alpha\beta+\alpha\gamma+\beta\gamma+\alpha\delta+\&c))x^{-n-2} + (\alpha^{3}+\beta^{3}+\gamma^{3}+\&c.(+\alpha^{2}\beta+\alpha^{2}\gamma+\beta^{2}\gamma+\gamma^{2}\alpha+\gamma^{2}\beta+\&c.)+\alpha\beta\gamma+\alpha\beta\delta+\alpha\gamma\delta+\beta\gamma\delta+\&c.)$$

$$\alpha\gamma\delta+\beta\gamma\delta+\&c.) x^{-n-3}+\&c. \text{ and } \frac{S}{S-Rx+Qx^{2}-\&c...x^{n}} = 1+\alpha\gamma\delta+\frac{1}{\beta}+\frac{1}{\gamma}+\&c.)$$

$$(\frac{1}{\alpha}+\frac{1}{\beta}+\frac{1}{\gamma}+\&c.)x+(\frac{1}{\alpha^{2}}+\frac{1}{\beta^{2}}+\frac{1}{\gamma^{2}}+\&c.(+\frac{1}{\alpha\beta}+\frac{1}{\alpha\gamma}+\frac{1}{\beta\gamma}+\&c.))$$

$$x^{2}+\&c. \text{ in each of which all the numeral co-efficients are 1.}$$
The approximate values to the greatest and least root may be found in the same manner as before.

From the preceding examples it appears, that the same obfervations which have been applied to Sir Isaac Newton's method are equally applicable to M. Bernoulli's.

13. In the *Meditationes* this rule is further extended, viz. let the given equation involve irrational and other functions of the unknown quantity; reduce it so that no function of the unknown quantity (x) may be contained in the denominator, and let the resulting equation be A=0. Assume a fraction

 $\frac{B}{A}$ , whose numerator B is a finite rational and integral function of the unknown quantity; reduce  $\frac{B}{A}$  into a series proceeding according to the dimensions of the unknown quantity: for example, let the series be  $A'x' + B'x'' + Cx' + 2x' + \dots + Lx'' + Mx'' + \overline{A''} + Nx'' + \overline{A''} + &c.$ ; then (except is excipiend is) if s be negative, will the greatest root be  $\sqrt[4]{\frac{M}{L}}$  nearly; but, if s be affirmative,  $\sqrt[4]{\frac{L}{M}}$  will be the least root nearly. If l be infinite, then (except is excipiend is, as before-mentioned) the quantities  $\sqrt[4]{\frac{M}{L}}$  and  $\sqrt[4]{\frac{L}{M}}$  will be the above-mentioned roots accurately.

These principles have been applied to find the remaining roots of the given equation as well as the greatest and least.

14. The rule of false has been found very useful in finding approximates to the two unknown quantities contained in two given equations, and has been applied to (n) equations having (n) different unknown quantities: for example, it has been observed, that if two or more (m) values of an unknown quantity (x) are nearly equal to each other and to its given approximate value (x'), the unknown quantity v=x-x' will ascend to two or more (m) dimensions in one of the resulting equations; or in more than one equations will be contained such powers of the quantity (v), that if the more equations were reduced to one whose unknown quantity is v, the resulting equation will contain (m) dimensions of the quantity v. Hence it appears, that in this case also the convergency of the approximate values found will depend on the given approximate being much more near to one root than to any other.

15. When the given equations A=0, B=0, C=0, &c. contain irrational or other quantities whose fluxions can be found; and approximates (a, b, c, d, &c.) are given to each of the unknown quantities (x, y, z, v, &c.) contained in the given equations; let a+x'=x, b+y'=y, c+z'=z, d+v'=v, &c.: fubflitute in the quantities  $A_{1}\left(\frac{\Lambda^{*}}{i}\right), \left(\frac{\Lambda^{*}}{i}\right), \left(\frac{\Lambda^{*}}{i}\right), \left(\frac{\Lambda^{*}}{i}\right), \left(\frac{\Lambda^{*}}{i}\right)$ &c.;  $\left(\frac{\ddot{A}}{a^2}\right)$ ,  $\left(\frac{\ddot{A}}{a^2}\right)$ ,  $\left(\frac{\ddot{A}}{a^2}\right)$ ,  $\left(\frac{\ddot{A}}{a^2}\right)$ , &c.;  $\left(\frac{\ddot{A}}{a^2}\right)$ , &c. for x, y, z, v, &c. respectively a, b, c, d, &c.; let the resulting correspondent values be A',  $\binom{A^*}{k}$ ,  $\binom{A^*}{k}$ , &c.whence may be deduced the equation  $A' + \left( \left( \frac{A^*}{\hat{x}} \right) x' + \left( \frac{A^*}{\hat{x}} \right) y' + \left( \frac{A^*}{\hat{x}} \right) z' + \left$ v' + &c.) +  $\left(\frac{1}{2} \left(\frac{A^{**}}{\dot{x}^2}\right) x'^2 + \frac{1}{2} \left(\frac{A^{**}}{\dot{y}^2}\right) y'^2 + \frac{1}{2} \left(\frac{A^{**}}{\dot{x}^2}\right) z'^2 + \&c. + \left(\frac{A^{*}}{\dot{x}^2}\right)$  $x'y' + \left(\frac{A''}{2z}\right)x'z' + &c.$  + &c. = 0 in which no irrational, &c. function of the approximates x', y', z', &c. is contained; and in the fame manner may the remaining equations B=0, C=0, &c. be transformed into others, in which no irrational function of the approximates (x', y', x', &c.) is contained, and from the refulting equations may be found approximate values of the quantities x', y', z', &c.

If there be given only two equations A = 0 and B = 0 containing two unknown quanties x and y, and all the quantities of the refulting equations, in which are contained more than one dimension of the quantities x' and y' be rejected, there will refult the two equations  $A' + \left(\frac{A''}{x}\right)x' + \left(\frac{A''}{y}\right)y' = 0$  and  $B' + \left(\frac{B'}{x}\right)x' + \left(\frac{B'}{y}\right)y' = 0$ , from which may be found x' and y', the same

fame as given by Mr. Simpson and others. When two or more values of the quantity x are nearly = a, then in a refulting equation or equations, quantities of two or more dimensions of the approximate x' are to be included.

#### PART III.

their roots no further than the quantities, and extracted their roots no further than the quantities themselves: they did not perceive the utility of proceeding any further, otherwise the operation would have been the same continued. Mr. Gregory St. Vincent, and Mr. Mercator divided, and Sir Isaac Newton divided and extracted the roots of quantities (in which only one unknown quantity (x) is contained) by the operations then used by arithmeticians, into series ascending or descending, according to the dimensions of x in infinitum. They clearly saw the utility of it in finding the fluents of fluxions, as Dr. Wallis and others some little

time before had found the fluent of the fluxion  $ax^{\frac{m}{n}}x$ ; or, which is the fame, the area of a curve whose ordinate is  $ax^{\frac{m}{n}}$  and abfaisfa is x.

2. M. LEIBNITZ asked from Mr. NEWTON the cases in which the above-mentioned series would converge; for it would be altogether useless when it diverges, and of little use when it converges slowly.

Case. 1. To this question an answer, I believe, was sirst given in the *Meditationes*, viz. reduce the function to its lowest terms; and also in such a manner that the quantities contained in the numerator and denominator may have no denominator: make the denominator Q = 0, and every distinct irrational quantity contained in it=0; and also every distinct irrational quantity H contained in the numerator =0; then, let  $\alpha$  be the least root affirmative or negative (but not =0) of the above-mentioned resulting equations, the ascending series will always converge, if the value of  $\alpha$  is contained between  $\alpha$  and  $\alpha$ ; but if  $\alpha$  be greater than  $\alpha$  or  $\alpha$ , the above-mentioned series will not converge.

If the above-mentioned feries (S) be multiplied into  $\dot{x}$ , and its fluent found; then will the feries denoting the fluent contained between two values a and b of the quantity (x) converge, when a and b are both contained between a and -a: the fluent always converges faster than the series a, the unknown quantity a having the same values in both.

Ex. Let  $\int \frac{\dot{x}}{a+bx+cx^2+...x^n} = Ax + \frac{1}{2}Bx^2 + \frac{1}{2}Cx^2 + &c.$  and the roots of the equation  $a+bx+cx^2+...x^n=0$  be  $\alpha$ ,  $\beta$ ,  $\gamma$ ,  $\delta$ , &c.; then  $\frac{\dot{x}}{a+bx+cx^2...x^n} = \frac{\pi\dot{x}}{a-x} + \frac{e\dot{x}}{\beta-x} + \frac{\sigma\dot{x}}{\gamma-x} + &c. = A\dot{x} + Bx\dot{x} + Cx^2\dot{x} + &c.$ ; but  $\frac{\pi}{\alpha-x} = \frac{\pi}{\alpha} + \frac{\pi x}{\alpha^2} + \frac{\pi x^2}{\alpha^3} + &c.$  in infinitum,  $\frac{e}{\beta-x} = \frac{e}{\beta} + \frac{e^x}{\beta^2} + \frac{e^x}{\beta^3} + &c.$  &c.; the former feries converges when x is contained between  $\alpha$  and  $-\alpha$ , the latter when x is between  $\beta$  and  $\beta$ , and fo on. In the fame manner the fluents  $\int \frac{\pi\dot{x}}{\alpha-x} = \frac{\pi}{\alpha}x + \frac{\pi x^2}{2\alpha^2} + &c.$  If  $\int \frac{e\dot{x}}{\beta-x} = \frac{e^x}{\beta} + \frac{e^x^2}{2\beta^2} + &c.$  &c. a fortiori converge when x is between  $\alpha$  and  $-\alpha$ ,  $\beta$  and  $-\beta$ , &c. respectively, and fo on: hence the series  $Ax + \frac{1}{2}Bx^2 + \frac{1}{2}Cx^2 + &c.$ 

$$= \int_{\alpha+bx+cx^2...x^n}^{\frac{x}{\alpha}} = \int_{\alpha-x}^{\frac{x}{\alpha}} + \int_{\beta-x}^{\frac{e^{\frac{x}{\alpha}}}{\beta-x}} + \int_{\gamma-x}^{\frac{e^{\frac{x}{\alpha}}}{\gamma-x}} + &c. = \left(\frac{\pi}{\alpha} + \frac{e}{\beta} + \frac{e}{\beta} + \frac{e^{\frac{x}{\alpha}}}{\gamma-x} + &c.\right) + &c. = \left(\frac{\pi}{\alpha} + \frac{e}{\beta} + \frac{e}{\beta} + \frac{e^{\frac{x}{\alpha}}}{\gamma-x} + &c.\right) + &c. = \left(\frac{\pi}{\alpha} + \frac{e}{\beta} + \frac{e^{\frac{x}{\alpha}}}{\gamma-x} + &c.\right) + &c. = \left(\frac{\pi}{\alpha} + \frac{e}{\beta} + \frac{e^{\frac{x}{\alpha}}}{\gamma-x} + &c.\right) + &c. = \left(\frac{\pi}{\alpha} + \frac{e^{\frac{x}{\alpha}}}{\beta} + \frac{e^{\frac{x}{\alpha}}}{\gamma-x} + &c.\right) + &c. = \left(\frac{\pi}{\alpha} + \frac{e^{\frac{x}{\alpha}}}{\beta} + \frac{e^{\frac{x}{\alpha}}}{\gamma-x} + &c.\right) + &c. = \left(\frac{\pi}{\alpha} + \frac{e^{\frac{x}{\alpha}}}{\beta} + \frac{e^{\frac{x}{\alpha}}}{\gamma-x} + &c.\right) + &c. = \left(\frac{\pi}{\alpha} + \frac{e^{\frac{x}{\alpha}}}{\beta} + \frac{e^{\frac{x}{\alpha}}}{\gamma-x} + &c.\right) + &c. = \left(\frac{\pi}{\alpha} + \frac{e^{\frac{x}{\alpha}}}{\beta} + \frac{e^{\frac{x}{\alpha}}}{\gamma-x} + &c.\right) + &c. = \left(\frac{\pi}{\alpha} + \frac{e^{\frac{x}{\alpha}}}{\beta} + \frac{e^{\frac{x}{\alpha}}}{\gamma-x} + &c.\right) + &c. = \left(\frac{\pi}{\alpha} + \frac{e^{\frac{x}{\alpha}}}{\beta} + \frac{e^{\frac{x}{\alpha}}}{\gamma-x} + &c.\right) + &c. = \left(\frac{\pi}{\alpha} + \frac{e^{\frac{x}{\alpha}}}{\beta} + \frac{e^{\frac{x}{\alpha}}}{\gamma-x} + &c.\right) + &c.$$

Where  $\alpha$  is the leaft root of the above-mentioned equation; but where  $\alpha$  is greater than  $\alpha$  or  $-\alpha$ , the feries will diverge.

The infinite feries  $a^m + ma^{m-1}x + m \cdot \frac{m-1}{2}a^{m-2}x^2 + &c. = \overline{a+x}$  will always converge when a is greater than x, and diverge when lefs, and confequently its convergency does not depend on the index m, unlefs when  $x = \pm a$ : and in the *Meditationes Analytica* are given the cases in which it converges or diverges when

=a=x; and also if the series  $x^m + max^{m-1} + &c. = x + a^m$  descends according to the dimensions of x, when it converges or diverges.

Case. 2. Let the above-mentioned quantity be reduced into a series  $Ax^{-r} + Bx^{-r-r} + &c$ . descending according to the dimensions of the unknown quantity x; then will the series  $Ax^{-r} + bx^{-r-r} + bx$ 

 $Bx^{-r-1} + \&c. = P$ , or the feries  $\frac{Ax^{-r+1}}{1-r} - \frac{Bx^{-r}}{r} + \&c. = \int P\dot{x}$  con-

verge, when x is greater than the greatest root ( $\lambda$ ) of the above-mentioned equations, and diverge when it is less; and consequently in this case, when the fluent is required between the two values a and b of x; the series found will converge when b and b are both greater than  $\lambda$ .

Cas. 3. When x is equal to the least root in the former case, and to the greatest in the latter, then sometimes the series will converge, and sometimes not. These different cases are given in the *Meditationes*; but it would be too long to insert them in this Paper.

4. If any roots are impossible as  $a-b\sqrt{-1}$  and  $a+b\sqrt{-1}$ , then the feries will converge when x is in the first case Vol. LXXVI. P

less than  $\pm (a-b)$ , and in the second case greater than  $\pm (a+b)$ ; or, more general, it will converge in the first case when  $a^n$  is always infinitely less than the reciprocal of the quantity  $\frac{(a+b\sqrt{-1})^n+(a-b\sqrt{-1})^n=P}{(a^2+b^2)^n}$ , where n is infinite; and in the latter case it will converge when  $a^n$  is infinitely greater than P.

It may not be improper to observe, that the same values of the root are to be applied in the equations, which are applied in the series.

- 3. Sir Isaac Newton, in the binomial theorem, reduced the power or root of a binomial into a feries proceeding according to the dimensions of the terms contained in the binomial. M. DE MOIVRE reduced the power or root of a multinomial into a like series; but in all cases, except the most simple, we must still recur to the common division, extraction of roots, &c.
- 4. Mess. Euler, Maclaurin, and other mathematicians, finding that the series before-mentioned often converged flowly, or, if the truth may be confessed, commonly not at all, to deduce the area of a curve contained between two values a and b of the absciss, or fluent of a fluxion between two values a and b of the variable quantity x, interpolated the series or area between a and b; that is, found the area or fluent contained between the abscisse a and a + a, then between the abscisse a + a and a + a, and then between the abscisse a + a and a + a, and so on, till they came to the area between a + a and a + a, and a + a, then between a + a and a + a, and then between the abscisse a + a and a + a, and then between the abscisse a + a and a + a, and then between the area between a + a and a + a, and the series expressing the area converges slowly; and therefore,

in order to investigate the area near the points of the absciss, where the ordinares become o or infinite, he transforms the equation, and finds series expressing the area near those points, in which series the abscisse or unknown quantities begin from those points.

- 5. In the Miditationes it is afferted, that in a feries proceeding according to the dimensions of  $\iota$ , if any root of the abovementioned equations be situated between the beginning of the absciss o and its end  $\kappa$ , the series will not converge: it is therefore necessary to transform the absciss so that it may begin or end at each of the roots of the above mentioned equations, and consequently where the ordinates become o or infinite, &c.; those cases excepted where the ordinate becomes o, and its correspondent abscissar is a root of a rational function W of  $\kappa$  without a denominator, and  $\int WP\dot{x}$  is equal to the given series; and in general the abscissar ought to begin from the above-mentioned points; for if they end there the series will converge very slow, if at all.
- 6. It is further afferted, that if a and b, the values of the abscrift between which the area is required, be both more near to one root of the above-mentioned equations than to any other, and n series are to be found, whose sum express the area contained between a and b; then that the sum of the (n) series may converge the swiftest, the distances of the beginnings of each of the n abscrift from the adjacent root will form a geometrical progression.
- 7. Mr. CRAIG found the fluent of any fluxion of the formula  $(a+bx^n+cx^{2n}+&c.)^mx^{\theta-1}x$  by a feries of the following P 2

kind  $(a+bx^n+cv^{-1}+&c.)^{m+1}\times x^0\times (\alpha+\beta v^n+\gamma x^{2n}+&c.$  in infinitum). Sir Isaac Newton, by feriefes of the same kind, found the fluents of fluxions of this formula  $(a+bv^n+cx^{2n}+&c.)^1\times (e+fx^n+gx^{2n}+&c.)^m\times &c. x^{0-1}\dot{x}$ ; the same principle is extended somewhat more general in the Meditationes.

8. Mr. John Bernoulli found the fluent of any fluxion  $\int n\dot{z} = nz - \frac{z^{-n}}{2\dot{z}} + \frac{z^{2n}}{2 \cdot 3\dot{z}^{2}} - &c. \text{ from the principles which Mr.}$  Craig published for finding the fluents of fluxions involving fluents.

In the Meditationes something is added of the convergency of these series; and also,

9. In them a new method is given of finding approximations. Let some terms in the given quantity be much less or greater than the rest; then reduce the quantity into terms proceeding according to the dimensions of the small quantities, or according to the reciprocals of the great quantities, and it is done. If the fluent of the quantity resulting is required, find it from the common methods, if possible; but if not, reduce the terms not to be found into an infinite series, and then find approximate values to each of the terms, &c.

Ex. 1. Let R the radius, and A the arc of a circle whose fine is S and cosine C, and  $A \pm e$  an are of a circle which does not much differ from the arc A, that is, let e be a very small quantity: then will the fine of the arc  $A \pm e$  be  $S(1 - \frac{1}{2} \times \frac{e^2}{R^2} + \frac{1}{2 \cdot 3 \cdot 4} \times \frac{e^4}{R^4} - \frac{1}{2 \cdot 3 \cdot 4 \cdot 5 \cdot 6} \times \frac{e^6}{R^6} + &c.) \pm C(\frac{e}{R} - \frac{1}{2 \cdot 3} \times \frac{e^3}{R^3} + \frac{1}{2 \cdot 3 \cdot 4 \cdot 5} \times \frac{e^4}{R^9} - &c.)$ ; and the cosine of the same arc will be  $C(1 - \frac{1}{2} \times \frac{e^3}{R^2} + \frac{1}{2 \cdot 3 \cdot 4} \times \frac{e^4}{R^4} - &c.$  in infinitum)  $\pm S(\frac{e}{R} - \frac{1}{R^8} + \frac{1}{2 \cdot 3 \cdot 4} \times \frac{1}{R^$ 

$$\frac{1}{2 \cdot 3} \times \frac{e^{3}}{R^{3}} + \frac{1}{2 \cdot 3 \cdot 4 \cdot 5} \times \frac{e^{5}}{R^{5}} - \&c.).$$
Ex. 2. Log.  $(x \pm e) = \int \frac{\dot{x}}{x \pm e} = \log \cdot x \pm \frac{e}{x} \pm \frac{e^{2}}{2x^{2}} \pm \frac{e^{3}}{3x^{3}} \pm \&c.$ 

$$\int \frac{\dot{x}}{a^{3} - (x + e)^{2}} = \int \frac{\dot{x}}{a^{2} - x^{2}} + \frac{e}{a^{2} - x^{2}} + \&c.$$
Ex. 3.  $\int \frac{\dot{x}}{a^{2} + (x - e)^{2}} = \int \frac{\dot{x}}{a^{2} + x^{2}} - \frac{e}{a^{2} + x^{2}} + \&c.$ 
Ex. 4.  $\int \frac{\dot{y}}{\sqrt{1 - (y \pm e)^{2}}} = \int \frac{\dot{y}}{\sqrt{1 - y^{2}}} \pm \frac{e}{\sqrt{1 - y^{2}}} \pm \&c.$ 
Ex. 5.  $\int \frac{\dot{y}}{\sqrt{1 - y^{2}} + e} = \int \frac{\dot{y}}{\sqrt{1 - y^{2}}} - \int \frac{e^{\dot{y}}}{1 - y^{2}} + \int \frac{e^{2\dot{y}}}{(1 - y^{2})^{\frac{1}{2}}} - \int \frac{e^{3\dot{y}}}{(1 - y^{2})^{2}} + \&c.$ 

Ex. 6. Let the fluxion be  $\frac{\sqrt{1-cx^2}\dot{x}}{\sqrt{1-cx^2}}$ , where c is a very small quantity; then, if P be put for  $\sqrt{1-x^2}$ , the fluxion becomes  $\frac{x}{R} = \frac{cx^2\dot{x}}{QR} = \frac{c^2x^4\dot{x}}{RR} = \frac{c^3x^5\dot{x}}{76R} = \&c.$  of which the fluents will be found  $A = \frac{c}{2} \times \frac{1 \cdot A - xP}{2} = \frac{c^2}{8} \times \frac{3B}{4} = \frac{x^3P}{16} \times \frac{5C - x^5P}{6} = &c. \text{ where } A = \frac{1}{2} \times \frac{1}{2} = \frac{1}{2} \times \frac{1} = \frac{1}{2} \times \frac{1}{2} = \frac{1}{2} \times \frac{1}{2} = \frac{1}{2} \times \frac{1}{2} =$  $\int_{\frac{1}{R}}^{\frac{1}{R}}$ , B= $\frac{1 \cdot A - xP}{2}$ , C= $\frac{3B - x^3P}{4}$ , &c.

This is the swiftest converging series for finding the length of the arc of an ellipse nearly circular, which is yet known; for example, let the absciss to the axis beginning from the center = x, the femi-transverse axis of the ellipse be 1, its femi-conjugate 1-d; then will  $c=2d-d^2$ , and let the length of the quadrant of the ellipse be required, in this case x=1, and  $P=\sqrt{1-x^2}=0$ ; and  $A=\frac{3,14159,&c.}{2}=1,57079$ , &c. whence the length required is 1,57079, &c.  $\times (1 - \frac{c}{2 - c} \frac{1 \cdot 3c^2}{2^2 \cdot 4^2} - \frac{1 \cdot 3^2 \cdot 5c^2}{2^2 \cdot 4^2 \cdot 6^2} - \frac{1 \cdot 3^2 \cdot 5^2 \cdot 7c^2}{2^2 \cdot 4^2 \cdot 6^2} & &c.).$ 

Ex.

Ex.7. Let the fluxion be  $\lambda(a^3 + a' + (3a^2b + b')\lambda' + (3ab' + c')\nu' + (b^3 + d')\lambda'' = P\lambda'$ , where a', b', c', &cc. are very finall quantities; then will  $P\lambda = ((a + bx))^m + ma + bv'' + (a' + b'x + c'x' + d'x') + m \cdot \frac{m-1}{2} \cdot \frac{a'}{2} \cdot \frac{bx''''' + ma'}{2} \times (a' + b'x + c'x'' + d'x')' + &c.)\lambda$ , of which the fluint is  $\frac{1}{3m+1+b} \cdot \frac{a' + bx'''' + a'' + a''$ 

12. M. Euler and others, reduced the feries  $Ar + Rx + r + Cx^{r+2s} + &c$ . into a feries A' fin. ra + B fin. r + sa + &c. &c. where a denotes the arc of a circle, whole fine is ax, &c. It may be easily reduced into infinite other ferieses proceeding according to the dimensions of quantities, which are functions of x; but it is most commonly preservable to reduce it into series proceeding according to the sines, cosines, tangents, or secants of the arcs of circle, which sines, &c. can immediately be procured from the common tables.

It has been observed in the first part, that to find the root of an equation, an approximate value much more near to one root of the equation than to any other must be given. In this part it is further observed, that serieses deduced from expanding given quantities, so as to proceed according to the dimensions of the unknown or variable quantities, will not converge if the unknown quantities be greater than the least roots of the abovementioned equations; and that they will not converge much, unless the unknown quantities have a small proportion to the least roots: and if the given quantities be expanded into serieses descending according to the dimensions of the unknown quantities, then the serieses resulting will not converge if the

greatest roots of the equations before-mentioned be greater than the unknown quantities; and unless the unknown quantities have a great ratio to the greatest roots the serieses will converge slowly: for example, the serieses  $\int \frac{\dot{x}}{1+x} = x - \frac{1}{2}x^2 + \&c.$ ,  $\int \frac{\dot{x}}{1+x} = x - \frac{1}{2}x^2 + \&c.$ ,  $\int \frac{\dot{x}}{1+x} = x - \frac{1}{2}x^2 + \&c.$ ,  $\int \frac{\dot{x}}{1+x} = x - \frac{1}{2}x^2 + \&c.$ ,  $\int \frac{\dot{x}}{1+x} = x - \frac{1}{2}x^2 + \&c.$ ,  $\int \frac{\dot{x}}{1+x} = x - \frac{1}{2}x^2 + \&c.$ ,  $\int \frac{\dot{x}}{1+x} = x - \frac{1}{2}x^2 + \&c.$ ,  $\int \frac{\dot{x}}{1+x} = x - \frac{1}{2}x^2 + \&c.$ ,  $\int \frac{\dot{x}}{1+x} = x - \frac{1}{2}x^2 + \&c.$ , will never converge if x, x, or y, be greater than x; but will always converge when less than x = 1 or x = 1 or x = 1 or x = 1 or x = 1. The series  $x + \frac{1}{2}x^3 + \&c.$  will always converge when x = 1 is structured between x = 1 or x = 1

If in either of the above-mentioned feriefes the unknown quantity x, z, or y, has a great proportion to 1, the feries will converge very flow; for example, if x=1, ten thousand numbers at least are to be calculated, to procure the sum of the series true to four figures; therefore, in these and most other series it is necessary first to find a near value, viz. when x either =z, when e is very small; or =e, when z is very small; and then write z+e for x in the quantity, and reduce it in the former case into a series proceeding according to the dimensions of e, in the latter case according to the dimensions of z, and there will arise two series, of which the fluents properly corrected, viz. by adding the fluent contained between the values a and e to the latter, and that between a and z to the former, will give the same fluent.

fluent. The first term of the series, in which e is supposed very small, will be the fluent of the given fluxing when x=x.

- 11. If a fluxion  $P\dot{x}$ , where P is a function of x, be tr. Giormed into another  $Q\dot{z}$ , where Q is a function of z, and they be reduced into series A and B, proceeding according to the dimensions of x and z respectively; find  $\alpha$  and  $\pi$ , correspondent values of the quantities x and z; then in ascending series, if  $\alpha$  has a less ratio to the least root of the equation P = 0, than  $\pi$  has to the least root of the equation Q = 0, the series A (exceptis excipiendis) will converge swifter than the series B.
- between the absciss x and ordinate y, found y in the two first terms of x, viz. y=a+bx, which is an equation to the asymptotes of the curves. Sir Isaac Newton, from an algebraical equation given, expressing the relation between y and x, found a series proceeding according to the dimensions of x, expressing y in terms of x. M. Leibnitz performed the same problem by assuming a series  $Ax^n + Bx^{n+r} + Cx^{n+2r} + &c$ . with general co-efficients, and substituting this series for y in the given equation, &c. from equating the correspondent terms he deduced the indexes and co-efficients. M. de Moivre, Mr. Mac Laurin, &c. observed, that when the highest terms of the given equations have two or more (m) divisors equal; for example,  $(y-ax^n)^m$ ; to which we must add, and when a value of y in this case is required nearly equal to  $Ax^n$ , a series

 $Ax^n + Bx^{n+\frac{r}{m}} + &c.$  is to be affirmed, whose indexes differ only by  $\frac{r}{m}$ , &c. if otherwise they would differ by r.

This reduction feldom answers any other purpose than finding the fluents of fluxions as  $\int y\dot{x}$ , &c.; or the asymptotes, &c.

of curves, which depend on some of the first terms of the series; but will very seldom be used for finding the roots of an equation; the rule of salse, or method given by VIETA, will ever be substituted in its stead.

13. The values of x may be required between which the abovementioned feries Ax"+Bx"+r+Cx"+2r+&c. will converge, as the infinite series answers no purpose when it diverges. First, if an ascending be required, write for y in the given algebraical equation an infinite quantity, and find the roots of x in the equation thence resulting P=0; which for y write in the same equation, and find the roots of x in the resulting equation which contain irrational quantities, viz. if one root be x = a; then let it contain  $(x-a)^m$ , where m is not a whole number; find the roots of the equations refulting from making every irrational function of (x) contained in the given equation =0, there being no irrational function of y contained in it; then, if x be greater than the least root not =0 of the above-mentioned equations, the feries will not converge; but if it be a feries descending according to the dimensions of x, and x be less than the greatest root of the above-mentioned equations, the feries will not converge.

In interpolating feriefes to investigate the fluent contained between two values a and b of the fluxion  $(Ax^n + Bx^{n+1} + &c.)t\dot{x}$ , it is preferable to make the abscissive begin from every one of the above-mentioned roots contained between a and b.

Most commonly these series will not converge unless x be less, &c. than other quantities not investigated by this rule.

14. Sir Isaac Newton gave an elegant example of this rule in the reversion of the series,  $y = ax + bx^2 + cx^3 + &c$ . from which the investigation of the law of the series has never been attempted. In the year 1757 I sent the first edition of my Vol. LXXVI.

Q

Meditationes

Meditationes Algebraicæ to the Royal Society, and published it in 1760, and afterwards in 1762, with another part added, on the Properties of curves, under the title of Miscellanca Analytica, in all which was given the law of a series for finding the sum of the powers of the roots of an equation from its co-efficients. That great mathematician M. LE GRANGE and myself printed about the same time an observation known to me at the time that I printed the above-mentioned book, that the law of its powers and roots, if it proceeds in infinitum, is the same; from which series of mine, with great sagacity, M. LE GRANGE sound the law which Sir Isaac Newton's reversion of series observes. In the Meditationes the law is given, and the series is made to proceed according to the dimensions of x, &c.

15. It is afferted in the Meditationes, that in most equations of high dimensions, unless purposedly constituted, the sum of the terms which, from the given hypothesis, become the greatest, being supposed = 0, only an approximate to the value  $Ax^n$  of y in the resulting equation can by the common algebra be deduced. In this case the approximate to the quantity A is to be sound so near as the approximate value of the quantity sought requires; or perhaps it is preserable to correct in every operation the approximate values of the quantities A, B, C, &c. in the series required  $A'x^n + B'x^{n+r} + C'x^{n+2r} + &c$ .

In the equation the quantity z = e may be substituted for x, and from the equation resulting a series expressing the value of y may be found, proceeding either according to the dimensions of the quantity z, or its reciprocals, according to the conditions of the problem.

16. If there are more than one (n) equations having (n+1) unknown quantities (x, y, z, &c.): in each of the equations for y,

z. &c. write respectively  $Ax^n$ ,  $A'x^m$ , &c.; and suppose the terms of each of the equations, which refult the greatest from the given or affumed hypothesis =0, and from the resulting equations may be found the first approximates Ax\*, A'x\*, &c. either accurately or nearly; then, in the given equations for y, z, &c. write  $y' + (A + a) x^n + B x^{n+n'} + &c.z' + (A' + a') x^m$ +  $B'x^{m+m'}$ , where a, a', &c. are very small quantities; and suppose the terms of each of the equations which become greatest from the above-mentioned hypothesis respectively = 0, and from the equations refulting deduce the quantities a, a', &c.; n', m', &c.)  $x^n + (B + \mathbf{1}b + b\mathbf{1} + &c.) x^{n+n} + &c.$ ;  $z = (A' + \mathbf{1}a' + a'\mathbf{1} + a')$ &c.) $x^{m} + (B' + 1b' + b' + 2c.)x^{m+m} + 2c.$  &c.; fubflitute thefe quantities for their values in the given equations, and from equating the correspondent terms of the resulting equations may be deduced the quantities required.

The differences of the indexes n', &c. m', &c. may be deduced by writing  $x^m$ ,  $x^m$ , &c. for y, z, &c. in the given equations, from the differences of the indexes of the quantities refulting. The fame principles may be applied in finding the abovementioned differences, when two or more values are  $Ax^m$ , &c. which were applied in a like case to one equation having two unknown quantities.

The same principles which discover the cases in which a series deduced from an equation having two unknown quantities will converge, may be applied for the same purpose to these series.

17. In the equations for x, y, z, &c. write respectively x' + e, y' + f, z' + g, &c.; and from the equations resulting find y', z', &c. in serieses either proceeding according to the dimensions

of

of the quantities e, f, o, &cc.; or according to the dimensions of the quantity x', as the conditions of the problem require.

- 18. Given one or more (n) algebraical equations involving (n+m) unknown quantities, one unknown quantity (v) may be expressed by a series proceeding according to the dimensions of the m-1 remaining ones (x, z, v, &c.), in which any dimensions of z, v, &c assumed may be supposed to correspond to (1) dimensions of the quantity (x).
- 19. In a fluxional equation of the  $m^{th}$  order, expressing the relation between x, y, and their fluxions, where  $\dot{x}$  is constant, Mr. Euler substitutes in the given equation for  $\dot{y}^{m}$ ,  $\dot{y}^{m-1}$ ,  $\dot{y}^{m-2}$ ,  $\dot{y}^{m}$ , &c. respectively  $Ax^{n-m}\dot{x}^{m}$ ,  $\frac{A}{n-m+1}x^{m-m+1}\dot{x}^{m-1}+a\dot{x}^{m-1}$ ,

 $\frac{A}{(n-m+1)(n-m+2)} x^{n-m+2} \dot{x}^{m-2} + ax \dot{x}^{n-2} + b\dot{x}^{m-2}, \frac{A}{(n-m+1)(n-m+2)}$  $\frac{1}{(n-m+3)} x^{n-m+3} \dot{x}^{m-3} + \frac{1}{2} a x^2 \dot{x}^{m-3} + b x \dot{x}^{m-3} + c \dot{x}^{m-3}, \quad \&c. \text{ where}$ a, b, c, &c. are any quantities to be assumed in such a manner as the conditions of the problem require; from supposing the aggregate of the terms of the refulting equation, which are the greatest, = 0, may be deduced the first approximate Ax", or else (as is beforementioned) A'x" a near approximate to Ax", and by proceeding as in algebraical equations another approximate may be found, and so on. The same may be found by assuming y = $Ax^{n} + Bx^{n+r} + Cx^{n+2r} + &c. + ax^{m} + bx^{m-1} + cx^{m-2} + &c.$  or y = $(A + ia + ai + &c.)x^n + (B + ib + bi + &c.)x^{n+r} + (C + ic + ci$ + &c.) $x^{n+2r} + &c. + ax^{m} + bx^{m-1} + cx^{m-2} + &c.$  and fubflituting it and its fluxions for their values y, y, y, &c. in the given equation, and supposing the aggregate of each correspondent terms, which do not very much differ from each other, =0; from the refulting equations can be deduced the co-dificients A, B, C, &c.; or A, 1a, a1, &c.; B, 1b, b1, &c.; C, 1c, c1, In&c. &c.

In the given equation for y, x, and their fluxions substitute y'+f, x'+g, and their fluxions, where the quantities f and g, &c. are assumed, so as to render the quantities y' and x', &c. very small.

In finding the feries which expresses the value of y in terms of x, there will always occur as many invariable quantities to be affumed at will as is the order of the fluxional equation, provided the series begins from its first terms; and to find them there will result equations easily reducible to homogeneous fluxional equations, of which the orders do not exceed  $m_x$ .



V. Experiments on Hepatic Air.
3y Richard Kirwan, Esq. F. R. S.

# Read December 22, 1785.

which is obtained from combinations of fulphur with various fubstances, as alkalies, earths, metals, &c. It possesses many peculiar and distinct properties; among which the most obvious are, a disagreeable characteristic smell emitted by no other known substance; inflammability, when mixed with a certain proportion of respirable or nitrous air; miscibility with water, to a certain degree; and a power of discolouring metals, particularly silver and mercury. These properties were first discovered by that incomparable analyst M. Scheele.

This air acts an important part in the economy of nature. It is frequently found in coal-pits; and the truly excellent and ever to be regretted M. BERGMAN has shewn it to be the principle on which the sulphureous properties of many mineral waters depend, and thus happily terminated the numerous disputes which the obscurity of that subject had occasioned. There is also great reason to think, that it is the peculiar product of the putrefaction of many, if not all, animal substances. Rotten eggs and corrupt water are known to emit the smell peculiar to this species of air, and also to discolour metallic sub-

stances in the same manner. M. VIELLARD has lately discovered several other indications of this air in putressed blood.

Yet, deserving as this substance appears to be of a thorough investigation, it has as yet been very little attended to. The experiments of M. Bergman have not been sufficiently numerous, and thereby led him into some mistakes. Dr. Priestley has intirely overlooked it. The researches of the ingenious M. Sennebier, of Geneva, have indeed been very extensive; but as, for particular reasons, he operated on this air over water (by which it is in great measure absorbed) instead of quickfilver, his conclusions appear in many respects objectionable, as will be seen in the sequel. The experiments I have now the honour of laying before the Society were all made over quickfilver, and several times repeated.

#### SECTION E.

Of the Substances that yield Hepatic Air, and the means of obtaining it.

It is well known, that faline liver of fulphur is formed, in the dry way, of a mixture of equal parts of vegetable or mineral alkali and flowers of fulphur, melted together by a moderate heat, in a covered crucible. I examined the circumfrances of its formation, and observed, that when this mixture was slightly heated, it emitted a bluish smoke, which gradually grew whiter as the heat was increased, and at last, when the mixture was perfectly melted, and the bottom of the crucible slightly red, became perfectly white and inflammable. To examine the nature of this smoke, I made a pretty pure fixed alkali, by deflagrating equal parts of cream of tartar and nitre

nitre in a red-hot crue ble in the usual way; and mixing this falt perfectly dry with flowers of fulphur in much smaller quantity, as I believe (for I did not weigh the falt, least it thould, during the weighing, attract mosture) I gradually heated the mixture in a small coated glass retort, and received the air proceeding from it over quicksilver.

The first portion of air that passed with a very gentle heat was that of the retort itself, slightly phlogisticated. It amounted to 1.5 cubic inches, and with Dr. PRIESTLEY's nitrous test (that is, an equal measure of nitrous air) its goodness was 1,29. It contained no sixed air.

The second portion of air obtained by increasing the heat amounted to about 18 cubic inches. It was of a reddish colour, and seemed a mixture of nitrous and common air. It slightly acted on the mercury.

The third portion confifted of 20 cubic inches, and appeared to be of the same kind as the last, but mixed with a little fixed air.

This was succeeded by 64 cubic inches of almost perfectly pure fixed air; and the bottom of the retort being now red, some sulphur sublimed in its neck. When all was cold, liver of sulphur was found in the bulb of the retort.

Hence we see, that the blue smoke consists chiefly of fixed air, and the white or yellow smoke of sulphur sublimed; and that no hepatic air is thus formed; nor vitriolic air, unless the retort be so large as to contain a sufficiency of common air to admit the combustion of part of the sulphur.

adly, That the acrial or any other acid, combined with the alkali, must be expelled before the alkali will combine with the sulphur. Liver of sulphur exercises a strong solving power on the earth of crucibles, and readily pierces through them.

The above experiment feems to show that liver of sulphur will not yield hepatic air without the addition of an acid: and I believe this to be true when the experiment is made in the dry way, and nearly fo in the moist way; for having added 200 grains of fulphur to a concentrated folution of strong caustic vegetable alkali, by a strong and long-continued heat I obtained only 1 cubic inch of hepatic air; vet it is well known, that a strong folution of liver of fulphur constantly emits an hepatic smell, even in the temperature of the atmosphere; and the substance so emitted contains so much hepatic air as to discolour filver and lead, and even their folutions: which fhews, that an incomparably small quantity of this air is capable of producing this effect. To discover whether this extrication of hepatic air might be caused by the deposition of fixed air from the atmosphere, I threw some pulverised calcareous hepar into aërated water, and by the application of heat endeavoured to obtain hepatic air, but in vain: and, indeed, the very circumstance that the hepatic smell, and its effects, are always strongest the first instant that a bottle of the hepatic folution is opened, feems to indicate that fixed air is no way concerned in its production.

The best liver of sulphur is made of equal parts of salt of tartar and sulphur; but as about one-sists of the salt of tartar consists of air which escapes during the operation, it seems, that the proportion of sulphur predominates in the resulting compound; yet as some of the sulphur also sublimes and burns, it is not easy to fix the exact proportion. 100 grains of the best, that is, the reddest liver of sulphur, afford, with dilute marine acid, about 40 cubic inches of hepatic air, in the temperature of 60°: a quantity equivalent to about 13 grains of sulphur, as will be seen in the sequel.

The marine acid is the best adapted to the production of hepatic air. If the concentrated nitrons acid be used, it will afford nitrous air; but having diluted some nitrous acid, whose specific gravity was 1,347, with 20 times its bulk of water, I obtained, with the assistance of heat, as pure hepatic air as with any other acid.

The concentrated vitriolic acid, poured on liver of fulphur, affords but little hepatic air without the affiftance of heat, though it inflantly decomposes the liver of fulphur; and it is partly for this reason that the proportion of air is so small; for it is during the gradual decomposition of sulphureous compounds that hepatic air is produced.

Distilled vinegar extricates this air in the temperature of the atmosphere; but it is not pure, its peculiar smell being mixed with that of vinegar.

The acid of fugar also produced some quantity of this air in the temperature of 59°.

20 grains of fedative falt, or acid (as it should more properly be called) dissolved in an ounce of water, being poured on liver of sulphur, afforded hepatic air only when in a boiling heat, or nearly so.

Neither the aërial nor arsenical acids produce any.

Liver of fulphur is foluble not only in water but in spirit of wine, and in caustic volatile alkalies; and the colour of both solutions is red. Sulphur is precipitable from the former by the addition of water or of an acid, but from the latter only by an acid.

Having made fome liver of fulphur, in which the proportion of fulphur much exceeded that of the alkali, I poured on part of it some oil of vitriol, whose specific gravity was 1,863: by this means I obtained hepatic air, so loaded with

with fulphur, that it deposited some in the tube through which it was transmitted, and on the upper part of the glass This air I transferred to another receiver: but though it was then perfectly clear and transparent, and amounted to 6 cubic inches, yet the next morning the infide of the glass was thickly lined with fulphur, and the air reduced to 1 cubic inch, which was pure vitriolic air. Hence it appears, first, that a species of elastic fluid may exist in a state intermediate between the aërial and the vaporous, which is not permanently elastic like air, nor immediately condensed by cold like vapour, but which, by the gradual loss of its specific heat, may be reduced to a concrete form. 2dly, That so large a quantity of sulphur may be combined with vitriolic air, as to enable it to exhibit the properties of hepatic air, for some time at least. A mixture of three parts pulverifed quick-lime and one part fulphur, heated to whiteness in a covered crucible for one hour, became of a stony hardness, and being treated with marine acid, afforded hepatic air. If a piece of this stone be heated in pure water it becomes bluish, and hence the origin of the blue marles generally found near hot fulphurated waters.

A calcareous hepar may also be formed in the moist way, as is well known.

Magnesia free from fixed air, heated in the same manner with sulphur, afforded no hepatic air when an acid was poured on it.

I also procured this air from a mixture of three parts filings of iron and one of sulphur, melted together, and treated with marine acid. It is remarkable, that this sulphurated iron, diffolved in marine acid, affords scarce any inflammable, but mostly hepatic air.

A mixture.

A mixture of equal parts filings of iron and fulphur, made into a paste with water, after heating and becoming black, afforded hepatic air when an acid was poured on it; but this hepatic air was mixed with inflammable air, which probably proceeded from the uncombined iron. After a few days, this paste lost its power of producing hepatic air.

M. BERGMAN has remarked, that combinations of sulphur with some other metals yield hepatic air.

I attempted extracting air from a mixture of oil of olives with caustic vegetable alkali. It immediately whitened, and on applying heat effervesced so violently as to pass over into the receiver: nor had I better success on adding an acid, as I might well foresee. The event was different when on a few grains of sulphur I poured some of the oil, and heated them in a phial with a bent tube; for as soon as the sulphur melted, the oil began to act on it, grew red, and emitted hepatic air, similar to that produced by other processes.

I also obtained this air in great plenty from a mixture of equal parts sulphur and pulverised charcoal, out of which its adventitious air had been as much as possible expelled by keeping it a long time heated to redness, in a crucible on which a cover was luted, with a small perforation to permit the air to cscape. This air was inflammable, as appeared by holding a lighted candle before it during its emission; yet it is hardly possible to free charcoal wholly from foreign air, for it soon re-attracts it when exposed to the atmosphere.

This last mixture, when distilled, affording a large quantity of hepatic and some inflammable air, without the addition of any acid, I imagined, that as the retort was only half full, it might contain a sufficiency of atmospheric air to admit the combustion of part of the sulphur, and thus surnish the neces-

fary acid; but when I filled the retort with air phlogisticated by the nitrous test unto 1,8, and in this air distilled the above mixture, the result was exactly the same as when the retort was filled with atmospheric air.

Six grains of pyrophorus, made of alum and fugar, effervesced with marine acid, and afforded 2,5 cubic inches of hepatic air. This pyrophorus had been made six years before, and was kept in a tube hermetically sealed, and for many summers exposed to the strongest light of the sun. It was so combustible, that some grains of it took sire while it was introduced into the phial out of which the hepatic air was expelled.

A mixture of two parts white fugar (previously melted in order to free it from water) with one part sulphur, when heated to about 600 or 700 degrees, gave out hepatic air very rapidly. This air had a smell much resembling that of onions; it contained no fixed air, nor saccharine, or other acid. But sugar and sulphur, melted together, gave out no hepatic air when treated with acids. Water, spirit of wine, and marine acid, decompose this mixture, dissolving the sugar, and leaving the sulphur.

A mixture of fulphur and *plumbago* afforded me no hepatic air.

I then tried whether fulphur could combine with elastic fluids, and the results were as follows.

12 grains of fulphur, heated in a retort, filled with metallic inflammable air, afforded no hepatic air; though when the retort was cold, and for some time exposed to the air, it smelled of hepatic air. It is true, the heat I applied might be insufficient; for the inflammable air passing over with a slight heat, the mercury ascended so high into the neck of the receiver, that, feating the rupture of the retort, I was obliged to interrupt the

the operation. I had no better fuccess when the sulphur, previous to its distillation, had been moistened with marine acid.

Again, I exposed 18 grains of liver of sulphur to six cubic inches of fixed air, thermometer 70°, for sour days. The liver of sulphur was somewhat whitened on the surface; the air had not an hepatic smell, but rather that of bread. It was not converted into phlogisticated air, but seemed to have taken up some sulphur, which lime-water separated. It was not in the least diminished, and therefore seems to have received an addition of hepatic air, or rather of sulphur.

I also exposed a quantity of fulphureo-martial passe to fixed air, for five days. The fixed air was not diminished, but received a slight accession of inflammable air. The passe itself, taken out of this air, and exposed to the atmosphere, heated strongly.

Lastly, I exposed 3 grains of sulphur to about 12 cubic inches of marine air. It was not diminished in four days; nor was the sulphur sensibly. On adding one cubic inch of water to this air, it was absorbed all to one inch, and this had an hepatic smell; so that neither was the sulphur decomposed, nor the marine acid converted into inflammable air. The water had also an hepatic smell, and evidently contained sulphur; for it precipitated the solution of silver brown mixed with white, and the nitrous solution of copper reddish brown, and when vegetable fixed alkali was dropped into it, let fall a white precipitate, namely, the sulphur.

#### SECTION II.

## Of the general Characters of Hepatic Air.

I found the absolute weight of this air by weighing it in a glass bottle, previously exhausted by Mr. Hurter's new improved airpump, whose effect is so considerable as to leave in general only and frequently but weighe part of unexhausted air. This bottle contained 116 cubic inches nearly; and this quantity of hepatic air weighed 38,58 grains, the thermometer being then 67°,5, the barometer 29,94, and M. Saussure's hygrometer 84°, the weight of 116 cubic inches of atmospheric air being at the same time 34,87 grains; hence a cubic foot of hepatic air weighs, in these circumstances, 574,7089 grains, and 100 cubic inches of it weigh about 33 grains; and its weight, relatively to that of common air, is as 10000 to 9038 \*. This hepatic air was extracted from artificial pyrites by marine acid.

The inflammability of this air has been already mentioned. It never detonates with common air; nor can it be fired, in a narrow-mouthed veffel, unless mixed with a confiderable proportion of this air. M. Scheele found it to inflame when mixed with two-thirds of this air. According to M. Sennebier.

<sup>\*</sup> Hence the weight which'I have affigned to common air in my first paper, after M. Fontana, is evidently erroneous; and, indeed, by that determination common air would not be even 700 times lighter than water, in the temperature of 55°, and the barometer 29,5, which contradicts all barometrical and aerostatic experiments: and I cannot omit mentioning the very near agreement of the weight of common air here found with that resulting from the calculation of Sir George Shuckburgh, it is so great as to differ only by 2 grains in a cubic foot.

it cannot be fired by the electric spark, even when mixed with any proportion of respirable air. I found a mixture of one part of hepatic air and 1,5 of common air to burn blue, without flashing or detonating. During the combustion fulphur is constantly deposited, and a smell of vitriolic air is perceived. A mixture of half hepatic and half nitrous air burns with a bluish, green, and yellow lambent flame; fulphur is also deposited, and in proportion as this is formed, a candle dipped in this air burns more weakly, and is at last extinguished. A mixture of two parts nitrous and one of hepatic air partially burns, with a green flame, and a candle is extinguished in the residuum, which then reddens on coming in contact with atmospheric air. I made a mixture of one part nitrous and one part hepatic air, and to this admitted one part also of common air; the instant the common air was introduced, fulphur was precipitated, and the three measures occupied the space of 2,4 measures; this burned on the furface with a wide greenish flame, but the candle was extinguished when sunk deeper.

A mixture of four parts common air and one part hepatic burned blue and rapidly; but a mixture of one part dephlogisticated and one part hepatic, which had stood eight days, went off with a report as loud as that of a pistol, and so instantaneously that the colour of the flame could scarce be discerned.

Every species of hepatic air turns the tineture of litmus red. M. Bergman seems to think, that, if this air were washed, it would not produce this effect; yet, when I had passed two measures of it through one of water, or when I had boiled it out of water impregnated with it, or even when I passed that which had already reddened litmus, into a fresh quantity of litmus, it still preserved the same property, which I therefore consider as essential to it.

With respect to folubility in water, hepatic airs extracted from different materials differ confiderably. In the temperature of 66°, water diffolves, by flight agitation, two-thirds of its bulk of alkaline or calcareous hepatic air, extracted by marine acid: three-fourths of its bulk of martial hepatic air, extracted by the fame acid; eight-tenths of that extracted by means of the concentrated vitriolic acid, or the dilute nitrous or faccharine acids in the temperature of 60°; seven-tenths of sedative hepatic air; nine-tenths of acetous hepatic air, and of that afforded by oil of olives; and its own bulk of that produced from a mixture of fugar and fulphur. In general, I imagined that which required most heat for its production to be most foluble: though in some instances, particularly that of acetous hepatic air, that circumstance does not take place.

But the most remarkable phænomenon attending the union of hepatic air with water is, that it is not permanent. Even water, out of which its own air had been boiled, in a few days after faturation with hepatic air grows turbid, and in a few weeks deposits most of it in the form of sulphur, though the bottle be ever so well stopped, or stand inverted in water or mercury. Yet water no way decomposes hepatic air by absorbing it; for the part left unabsorbed by a quantity of water is abforbable by a larger quantity of water, and burns like other hepatic air. Heat does not expel this air from water, until carried to the degree of ebullition.

No fpecies of hepatic air, which I have examined, precipitates lime from lime-water, except the carbonaceous; and even this scarcely produces a sensible precipitation, unless a large quantity of it be made to pass through a small quantity of lime-water. The

The folution of acetous baro-selenite, (that is, ponderous earth diffolved in distilled vinegar) is rendered brown and turbid by this air, but that of marine baro-selenite is not altered; nor are the folutions of other earths. Metallic folutions are affected by it in the same manner as by hepatic water, of which I shall treat in the fifth fection.

But of all the tests of hepatic air, the most delicate and senfible is the folution of filver in the nitrous acid. This, according as the nitrous acid is more or less faturated with filver, becomes black, brown, or reddish brown, by contact with hepatic air however mixed with any other air or substance. When the acid is not faturated, or is in large proportion, the brown or black precipitate, which is nothing but fulphurated filver, is re-diffolved.

It should also be remarked, that all hepatic air is somewhat diminished by long standing on mercury, whose surface is then blackened by it. This is particularly the case of carbonaceous hepatic air, which certainly carries over and volatilizes part of the charcoal from which it is extracted, especially that portion of air which comes over in the greatest heat; this it deposits on the addition of water.

### SECTION III.

Of the Action of Hepatic and other Aerial Fluids on each other.

Six cubic inches of common and fix of hepatic air being mixed with each other, and standing over mercury for cight days, were not in the least altered in their dimensions or otherwife; though a diminution of a \* th part might be perceived. The mercury was flightly blackened. The event was the fame when three measures of common and one of hepatic air were used. Water took up the hepatic air. No fixed air was tound.

Five measures of hepatic, and five of dephlogisticated air so pure that one measure of it and two of nitrous air made only three-tenths of a measure, remained unaltered for eight days, the mercury only being blackened. No fixed air was produced, nor the dephlogisticated air phlogisticated. When the mixture was fired, it went off all at once with a loud report.

Four measures of phlogisticated and four of hepatic air remained undiminished for sixteen days: water then took up the hepatic, and left the phlogisticated air.

Four measures of *inflammable* and four of hepatic air remained unaltered for fix days.

Two measures of hepatic and two of marine acid air suffered no diminution in three days. The mercury on which they stood was not blackened. Water took up both, and precipitated the solution of silver black.

The fame quantity of hepatic and fixed air remained four days without any fensible diminution. Four measures of water absorbed the greater part of both, had an hepatic smell, precipitated lime from its solution, and also silver, as usual. The residuum extinguished a candle.

But vitriolic, nitrous, and alkaline airs had very remarkable effects on hepatic air.

Two measures of hepatic being introduced to two of vitriolic air, a whitish yellow deposition immediately covered both the top and sides of the jar, and both airs were, without any agitation, reduced to little more than one measure; but the opecity of the incrusted glass prevented my then ascertaining the diminution with precision. Hence I repeated this experiment more at large, in the following manner. To sive measures of vitriolic air (each measure containing a cubic inch) I added one

of hepatic air. In less than a minute, without any agitation, the fides of the glass were covered with a whitish scum, which feemed moift, and a diminution took place of more than one measure. In four hours after, I introduced a second measure of hepatic air, which was followed by a fimilar diminution and deposit. The next day I added three more measures of this last, at the interval of four hours between each; and still finding a confiderable diminution after each, I the following day added another measure; the diminution produced by this last appeared to me not to exceed one measure. I then poured off the refiduary air into another jar, and found it not to exceed three measures; so that here eleven measures, namely, five of vitriolic and fix of hepatic air, were reduced to three. Into one measure of this residuary air I introduced a lighted candle: it was immediately quenched. To the two remaining measures I added one measure of water: by agitation it took up fourtenths of its bulk. To part of the remainder I added nitrous air, which had no effect upon it. Another part of it extinguished a candle. It had not a vitriolic fmell.

The water which had taken up four-tenths of its bulk of this air did not precipitate lime; nor did it affect acetous barofelenite in less than a quarter of an hour, and then produced a very flight cloud. It sensibly reddened litmus, and precipitated the solution of silver white; and hence it appears to have taken up a very minute portion of vitriolic acid. And what was not taken up by water seems to have been mere phlogisticated air.

I afterwards washed the sulphur, which coated the jar, with distilled water. This water slightly reddened litmus, precipitated not only the acetous, but also marine baro-selenite copiously, as well as marine and nitrous selenite; also the nitrous solutions of silver, lead, and mercury, all white. It even precipitated

precipitated lime from lime-water, forming a cloud in it, which neither the fixed nor volatile acid of vitriol can produce. Hence this water contained nothing hepatic; but, on the contrary, a confiderable proportion of the aërial and vitriolic acids \*.

With nitrous air I made the following experiments. First, I found that two measures or cubic inches of nitrous and two of hepatic air were little altered when first mixed, even by agitation; but after thirty-six hours both were reduced to nearly one-third of the whole, but something more. Yellow particles of sulphur were deposited both on the mercury, and on the sides of the jar, but the mercury was not blackened. The residuary air had still an hepatic smell, and was somewhat further diminished by water; and in the unabsorbed part a candle burned naturally. The water had all the properties of hepatic water.

Perceiving by this experiment that I had not employed enough of nitrous air to condense the hepatic persectly, to eight cubic inches of hepatic air I added nine of nitrous air, all at once; a yellowish cloud instantly appeared, a slight white scum was deposited on the sides of the jar, and the whole seemed diminished about two cubic inches, or between one-ninth and one-eighth, the temperature of the room being then 72°. I then laid by the mixture, and in forty-eighthours after, I sound the whole reduced to six cubic inches, and the top and sides of the jar covered with a white cake of sulphur, the heat of the room being constantly kept between 60° and 70°. Finding the diminution to reach no surther in-

<sup>\*</sup> Note, the vitriolic acid air here employed was the purest possible was extracted from sulphur distilled with precipitate per se.

twenty-four hours more, I examined the refiduary air. It exhibited the following appearances.

- 1°, It had the smell of alkaline air pretty strongly; at least that smell issued from the jar that contained it after the air itself was poured into another jar.
  - 2°, A candle burned in it naturally.
- 3°, It did not affect tincture of litmus or lime-water, or ace-
- 4°, No species of air had any effect on it except the dephlogisticated, with which it produced a slight reducts and diminution.
- 5°, It produced a flight white precipitate in folution of filver.

It is plain, this air is the same as that which Dr. PRIEST-LEY calls dephlogisticated nitrous air, and which, I think, may more properly be called deacidisted nitrous air. A further examination of it would lead me too far from the present subject: I shall therefore defer it until another opportunity.

As it appeared to me, from the experiment mentioned in the fecond fection (in which I found fulphur precipitated from a mixture of nitrous and hepatic air, immediately after the admiffion of common air) that an uncombined acid in the nitrous air was the cause of the precipitation of sulphur; I attempted depriving nitrous air of any loose acid it might contain, before I should mix it with hepatic air.

th, I made fome nitrous air from filver very carefully over boiled and filtered water, and found it to contain an acid, for it strongly reddened tincture of litmus.

2dly, I admitted alkaline air to this nitrous air until it no longer caused any cloud, and then washed out the ammoniacal compound in distilled water; after which I transferred this purified

purified nitrous air to the mercurial tub. It appeared to lose, by privation of its acid, about one-fixth of its bulk; and it was diminished by common air just in the same manner as unpurified nitrous air is.

Then to 8 cubic inches of this purified nitrous air I admitted all at once 7 cubic inches of hepatic air. No cloud, diminution, or deposit, appeared; but in six hours after (the temperature of the room being all the time at 76°), the whole was reduced to 5 cubic inches; the diminution went no further eighteen hours after. Sulphur, much whiter than in the former experiments, was deposited, and both in this and in the former experiments that part of it which, by the rifing of the mercury, was intercepted between it and the jar, was of a yellow and red shining colour, and not black as that deposited on mercury usually is. The residuary air flashed with so much vehemence as to extinguish the candle dipped into it, by the violence of the blaft. The flame was exceeding white and vivid; but it did not detonate in the least, but rather refembled dephlogisticated air. The jar out of which it had been transferred had a sharp alkaline smell.

This air was not in the least diminished by nitrous air, even when heated to 150 degrees; which heat I contrived to produce by passing the upper part of the jar that contained this air into another wider jar, furnished with a perforated cork bettern, and filling this with water heated to that degree.

Water poured into the jar in which the sulphur was deposited, produced a bluish white cloud in solution of silver, though insipid to the taste.

Hence it appears to me, that, whatever this air may be it had been deacidified by hepatic air full more perfectly than that that in which a candle burns naturally; and that it is by no means dephlogisticated.

Lastly, Alkaline and hepatic airs, perfectly pure and mixed in proper proportions, would probably destroy each other completely, though I have not been able to effect this intirely. Six measures of hepatic air from liver of sulphur and 6 of alkaline air immediately throw up a white cloud, leave a whitish scum on the sides of the jar, and are reduced to about 1 measure. On adding water this is reduced to about one-half; and in this I found a candle to burn naturally: but the following experiments, being made with more care, prove that this residuary air was only the common air of the vessels.

To 6 cubic inches of calcarcous hepatic air I admitted, all at once, 7 of alkaline air; a white cloud and a little white fourm at first appeared; but in a few seconds the whole was reduced to fix sevenths of a cubic inch; and on adding 2 measures of water, only one-ninth of a cubic inch of air remained. This could not be inflamed. The water, thus impregnated, precipitated a solution of silver black. In this experiment great care was taken to have each of the mixed airs as pure as possible, and the alkaline was admitted all at once, instead of by different portions, merely with that view; and it is probable, that, if the due proportion were hit upon, nothing would remain. The scum appears to be almost liquid, and as soon as the jar is emptied of mercury, it breaks out into a white smoke, with an exceeding sharp urinous smell.

Five measures of martial hepatic air were, upon the admission of 5‡ of alkaline air, reduced to something more than one measure, and upon the addition of water there remained but half a measure; and this was inflammable, with detonation; the inflammable

inflammable air undoubtedly proceeding from the folution of the iron.

Five cubic inches of faccharine hepatic air, mixed with 5 of alkaline air, were diminished more slowly; for after five minutes there still remained 4,5 cubic inches. I then added another measure of alkaline air: in three hours after there remained but 1,25 cubic inches. In passing this residuum through water it was reduced to about half a cubic inch; and this burned with a blue lambent slame, without leaving a vitriolic smell or any deposit on the glass; so that it clearly was inflammable air from the sugar.

I once imagined I had obtained inflammable air from a mixture of alkaline air with hepatic air drawn from liver of sulphur; but I afterwards found this inflammable air proceeded from a very slight contamination of zinc in the mercury over which my airs had been produced; the alkaline air acted on this zinc, and must have produced the inflammable air; for when I afterwards received and mixed these airs over mercury, perfectly purified, I obtained no more inflammable air.

## SECTION IV.

Of the Action of Hepatic Air, and Acid, Alkaline, and Inflammable Liquids, on each other.

One measure of oil of vitriol, whose specific gravity was 1,863, absorbed two measures of hepatic air all to one-tenth. The acid was whitened by a copious deposition of sulphur. I also introduced, over mercury, a measure of red nitrage acid, whose specific gravity was 1,430, to an equal measure of hepatic; air; red Vol. LXXVI.

vapours instantly arose, and only one-tenth or one-twelfth of a measure remained in an aërial form; but as the acid acted on the mercury, I was obliged to carry the jar into the water tub, by which means the whole was absorbed: no sulphur was here precipitated.

I repeated this experiment in another manner. Having produced 4,5 measures of hepatic air over mercury, I transferred them to the water tub, and instantly by means of a syphon blew into them one measure of the above concentrated nitrous acid; but though I managed as quickly as possible, the hepatic air was something diminished by contact with the water, before the acid had entered the tube that contained the air. I then stopped the tubé with a ground glass stopper, and laid it by for twelve hours; after which interval I found the liquor in the tube white and turbid, and but weakly acid, much water having entered in spite of my endeavours to exclude it. The remaining air flightly detonated on presenting to it a lighted candle, and had an hepatic finell. But as this hepatic air was obtained from fulphureo-martial paste, it does not prove that sustammable air enters into the composition of other hepatic airs, derived from the union of fulphur with fubstances that do not yield inflammable air.

Finding it so difficult to subject hepatic air to the direct action of the concentrated nitrous acid, I diluted it to that precise degree at which it could not act on mercury without the uffishance of heat, and then passed through it an equal back of the same hepatic air; the acid was whitened, and eight-tenths of the air absorbed, and the residuum detonated. Repeating the same experiment with hepatic air from liver of sulphur, I found still more of it absorbed by the acid; but the residuum

no longer detonated, but burned with a blue and greenish flame, and sulphur was deposited on the sides of the jar.

Observing this dilute acid to absorb nearly three times its bulk of alkaline hepatic air, I expelled this air from it by heat, but obtained only one-sixth of the air that had been absorbed; and in this a candle burned naturally.

Two measures of alkaline hepatic air, being exposed to one of strong marine acid, were absorbed, by slight agitation, all to one-fifth of a measure. A third measure of air being then added, there remained, after some agitation, but half a measure. Sulphur was precipitated as usual; but the mercury over which the acid stood attracted it from the acid; for it was blackened, which did not happen when the former acids were used. The residuum burned just as pure hepatic air.

Distilled vinegar absorbs nearly its own bulk of air, and becomes slightly whitened; but by agitation it may be made to take up about twice it bulk, and then becomes very turbid.

One measure of caustic vegetable alkali, whose specific gravity was 1,043, absorbed nearly four measures of alkaline hepatic air. It was at first rendered brown by it; but after some time it grew clear, sulphur was deposited, and the surface of the mercury blackened. This shews that alkalies are not dephlogisticated by silver or other metals, as Mr. Baumé imagined, but only cleared of part of the sulphur, which they commonly contain, it being formed by the tartar vitriolate contained in the plant, and coal, during combustion.

One measure of caustic volatile alkali, whose specific gravity was 0,9387, absorbed 18 of hepatic air. If the caustic liquor contained more alkali, it would absorb more hepatic air, as of measures of hepatic unite to 7 of alkaline air; and thus the strength of alkaline liquors, and their real contents, may be to 7 of alkaline liquors.

determined better than by any other method. Also the smoaking liquor of BOYLE, which is difficultly prepared in the usual way, may easily be formed by placing the volatile alkali in the middle glass of Dr. Noorh's apparatus for making artificial mineral waters, and decomposing artificial pyrites, or liver of sulphur, in the lower glass, by marine acid.

Oil of olives absorbs nearly its own bulk of this air, and obtains a greenish tinge from it.

But new milk fcarcely absorbs one-tenth of its bulk of this air, which is very remarkable, and is not in the least coagulated.

Oil of turpentine also absorbs its own bulk of this air, and even more; but then becomes turbid. Water seems also to precipitate this air from it, for when shaken with it a white cloud appears.

Spirit of wine, whose specific gravity was 0,835, absorbed nearly three times its bulk of this air, and became brown. By this means sulphur may be combined with spirit of wine much more easily than by Count Lauragais' method, the only hitherto known. Water precipitates the sulphur in part.

Sulphurated spirit of wine does not tinge litmus red; but it precipitates lime-water, as highly rectified spirit of wine singly does. It also precipitates and gives a brown colour to acctous baro-selenite, which spirit of wine alone also does. It turns the solution of silver black and reddish brown. Concentrated vitriolic acid precipitates the sulphur from it, which neither the nitrous nor marine acids can effect.

When hepatic air is mixed with an equal bulk of vitriolic æther, the bulk of the air is at first increased; but afterwards half of it is absorbed, and a slight precipitation appears. The small of the æther is mixed with that of the hepatic air; but on adding water it becomes very offensive, resembling that of putrefying animal substances.

To one measure of hepatic air I added 1,5 of the nitrous folution of filver: the air was immediately, without agitation, reduced to half a measure, and the solution blackened. The remaining air admitted a candle to burn naturally. Hepatic air was also absorbed, but not so readily, nor in such quantity, by the solution of vitriols of iron and filver; that of silver was blackened; that of iron at first became white, but by agitation darker. The residuary air burned blue, as hepatic air usually does.

### SECTION V.

Of the Properties of Water saturated with Hepatic Air.

This water turns tincture of litmus red.

It does not affect lime-water.

It does not form a cloud in the folution of marine, though it does in that of acetous baro-felenite.

The folutions of other earths in the mineral acids are not aftered by it.

When dropped into a folution of vitrial of iron or marine falt of iron, it produces a white precipitate.

In nitrous falt of copper it causes a brown precipitate, and the liquor is changed from blue to green. The precipitate rediffolves by agitation. In vitriol of copper it forms a black precipitate.

The folution of tin' in aqua regia is precipitated by it of a yellowish white colour; that of gold, black; that of persons, antimony.

antimony, red and yellow; that of platina, red mixed with white.

The folution of filver in the nitrous acid, and also that of lead, whether in the acetous or nitrous acid, are precipitated black. If the folutions are not perfectly faturated with metal, the precipitates will be brown or reddish brown, and may be redisfolved by agitation.

The nitious folution of *mercury* is precipitated of a yellowish brown; that of sublimate corrosive, yellow mixed with black; but by agitation it becomes white.

The nitrous folution of bisinut becomes, by mixture with this water, reddish brown, and even assumes a metallic appearance; that of cobalt becomes dark; that of zinc, of a dirty white; that of arsenic, in the same acid, yellow mixed with red and white, or piment and realgar being formed.

If oil of vitriol, whose specific gravity is 1,863, be dropped into hepatised water, it renders it slightly turbid; but, if the volatile vitriolic acid be dropped into it, a bluish white and much denser cloud is formed in the water.

Strong nitrous acid, whether phlogisticated or not, causes a copieus white precipitation; but dilute nitrous acid produces no change. Green nitrous acid, whose specific gravity was 1,328, immediately precipitated sulphur from it.

Strong marine acid produced a slight cloud; but neither disfilled vinesar nor acid of sugar had any effect.

It is faid by Mr. BERGMAN, that hepatifed water in a well closed wessel essents a solution of iron in a sew days; but this experiment, on repeated trials, did not succeed with me: nor could I dissolve any other metal in this water; the sulphur indeed unites to many of them, but forms an insoluble mass;

fo that, I prefume, metallic fubstances can never be found in hepatifed mineral waters.

### SECTION VI.

Of the Properties of Alkaline Liquors impregnated with Hepatic Air.

I have already mentioned the proportion of air they are able to take up. Colourless fixed alkaline liquors receive a brownish tinge from this air. The residuum they leave is of the same nature as the part they absorb.

A caustic fixed alkaline liquor, saturated with this air, precipitates barytes from the acetous acid, of a yellowish white colour. It also decomposes other earthy solutions, and the colour of the precipitates varies according to their purity, and perhaps this test might be so far improved as to supply the place of the Prussian alkali.

It precipitates the solution of vitriol of iron, and also marine salt of iron, black; but this latter generally whitens by agitation. That which I used was very saturate.

The folutions of filver and lead are also precipitated black with some mixture of white; that of gold is also blackened; but that of platina becomes brown.

Solutions of copper let fall a reddish black or brown preci-

Sublimate correspond by this test discovers a precipitate partly. white and black, and partly orange and greenish.

In the introdes foliation of anjenic it forms a yellow, and orange; and in that of rebulks of anximony, in square, an orange precipitate mixed with black.

Nitious

Nitrous folution of zinc, thus treated, shews a dirty white; that of bifmuth a brown mixed with white; and that of cobalt a brown and black precipitate.

As Prussian alkali always contains some iron, it gives a purple precipitate with this test, which precipitate is easily dissolved.

It turns tincture of raddishes, which is my test for alkalies, green.

The action of liver of fulphur on metallic substances in the dry way is described by many authors, and particularly in an excellent Differtation by M. Engestrom; but its action in the moist way has not been mentioned, as far as I recollect, by any. Hence I tried its effect on a few grains of iron, copper, lead, tin, zinc, bismuth, regulus of antimony, and of arsenic. Putting each into a bottle, containing about three half ounces of liquid liver of sulphur, so far diluted that its colour was yellow; in about sisteen days I sound they all, except the zinc and tin, had attracted sulphur from the fixed alkali. Iron, arsenic, and regulus of antimony and lead, were most altered; copper next, and bismuth least: but the liquors held none of the metals in solution; that which contained iron became green; on adding an acid sulphur was precipitated; if it held iron it could not at that period be detected.

Water faturated with the condensed residuum of alkaline and hepatic air, that is, with the purest volatile liver of sulphur, does not precipitate marine felenite, though it forms a slight brown and white cloud in that of marine baro-felenite.

It produces a black precipitate in the folution of vitriol of iron, and a black and white in that of marine falt of iron; but by agitation this last becomes wholly white.

It precipitates both vitriol of copper, and the nitrous falt of copper, red and brown.

Tin in aqua regia gives a yellowish precipitate; gold a dilute yellow and reddish brown; platina a slesh-coloured precipitate; and regulus of antimony a yellowish red.

Silver is precipitated black; and so is *lead* both from the nitrous and acetous acids.

Sublimate corresive appeared for an instant red; but soon after its precipitate appeared partly black and partly white.

The nitrous folution of bismuth affords also a precipitate, partly black, partly white, and partly reddish brown, and of a metallic appearance; that of cobalt is also black or deep brown.

Arsenical folutions give yellow precipitates more or less red; but those of zinc only a dirty white.

All these colours vary in some degree, according as the liquors are more or less saturated previous to and after their mixture, and the time they have stood together.

### SECTION VII.

# Of the Constitution of Hepatic Air.

From an attentive confideration of the above experiments, which I purposely disengaged from all theory, it is difficult to conclude, that hepatic air consists of any thing else than sulphur itself, kept in an aerial state by the matter of heat. Every attempt to extract inflammable air from hepatic air, when drawn from materials that previously contained nothing inflammable, namely, from alkaline or calcareous hepars, Vol. LXXVI.

proved abortive: on the contrary, when the materials could previously supply inflammable air, as when martial carbonaceous and saccharine compounds were employed, inflammable air, in ever so small a proportion, was detected: nor could hepatic air be procured from the direct union of inflammable air and sulphur, as we have seen.

Some have imagined, that this air confifts of liver of fulphur itself volatilized, and consequently that an alkali enters into its composition; but many weighty reasons oppose this supposition. In the first place this air is evidently, though weakly acid, since it reddens litmus, and precipitates acetous baro-selenite. 2dly, It may be extracted from materials that either contain no alkali at all, or next to none, as iron, sugar, oil, charcoal: and, lastly, it is not decomposed by marine or fixed air, by which, nevertheless, liver of sulphur is decomposable.

I formerly thought that fulphur was held in folution in hepatic air, either by vitriolic or marine air; yet though both of them may hold fulphur in folution, as we have feen, still neither of them is effential to the constitution of hepatic air as fuch, since it is producible from materials that contain neither of these acids; and, from whatever subject it is obtained, it exhibits the characters of one and the same acid, namely, the vitriolic exceedingly weakened; and such an acid we may suppose sulphur itself to be.

In effect, fulphur, even in its concrete state, affords many characters of acidity. It unites with alkalies, calcareous and ponderous earths, and most metals, as a weak acid might: and except a manifest solubility in water (a property which some other concrete acids also possess in a very weak degree) it exhibits every character of acidity. But its acidity is the weakest possible, since it decomposes only acetous, and not marine baro-

felenite,

felenite, and is separable from alkalies and earths by all other acids.

That the matter of heat enters into the composition of this air, is evident from the experiments of M. Scheele, who paid particular attention to that object. He found, that acids excite much less sensible heat in uniting with liver of sulphur, whether alkaline or calcareous, than while uniting with a proportion of caustic fixed alkali or lime equal to that which enters into the composition of those livers; whence he justly infers, that the difference enters into the composition of the hepatic air produced. I have proved the fame thing another way: for, instead of decomposing an alkaline hepar by marine acid, I tried to decompose it by a saturate solution both of marine felenite and marine Epfom. The decomposition indeed took place, but no hepatic air was produced: for the acid having given out its specific heat on uniting to the earths, had none to lose or communicate on uniting to the alkali, and consequently the fulphur receiving none could not be thrown into an aërial state.

It is remarkable, that bodies capable of an aërial form receive the latent heat necessary for that form, much more readily from a body that parts with its specific heat than by the mere application of sensible heat. Thus aërated barytes cannot be decomposed by mere heat, as Dr. WITHERING has shewn, though its air is easily separated from it by an acid; and in the same manner antimony cannot be desulphurated even by vitrefaction, though it may by acids: so liver of sulphur will not give hepatic air by mere heat, though it will by the intervention of an acid, even the weakest. The reason of which seems to be this: the matter of heat has no particular affinity with any substance, as is evident from its passing indifferently

indifferently from any hot body to a colder, of whatever fort or kind the bodies may be; but it is determined to unite with this or that body in a latent state, in greater or lesser quantity, in proportion to the greater or lesser copacity of these bodies to receive it. Now acids, by uniting to the alkaline basis of liver of sulphur, expel the sulphur, and give it their heat, at the instant the sulphur, by its separation, has the capacity to receive it; whereas sensible external heat, acting alike on both the constituent parts of liver of sulphur, separates neither; or if it separates them, yet, by its successive action, it throws one of them into a vaporous state sirst, and bodies that sirst acquire this state can never after acquire an aërial state by any subsequent accession of heat.

The vitriolic and nitrous acids are less adapted to the production of hepatic air than the marine acid, though they contain more specific heat than the mere acid part of the marine acid: the most probable reason of which is, because they have a stronger attraction to sulphur itself, and so detain it.

Hepatic air is much disposed to give out its latent heat, particularly when in contact with substances to which it has any affinity; thus it is condensed in water in a few days; it is also condensed by long exposure to fresh surfaces of mercury or silver or other metals, particularly if they are moist. M. Bergman found it in great measure condensed into sulphur, when inclosed alone in a bottle\*. In this case it probably contained an excess of sulphur; for hot hepatic air is capable of keeping a farther quantity of sulphur in solution, and deposing it when cold, as I have frequently observed.

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<sup>\*</sup> See a note in the second volume of M. Morviau's translation of the secondvolume of Bergman's Works, p. 341.

The precipitation of metallic substances by this air is owing partly to the union and phlogistication of the acids by this air, and partly to its union with the metals themselves, for it evidently unites in most cases to both.

As alkalies and fulphur are known to have an affinity to each other, we easily understand why hepatic and alkaline airs are condenfed when mixed with each other; nor is there any difficulty in conceiving why hepatic air is not condenfed by common, dephlogisticated, inflammable, or phlogisticated airs, or remarkably by marine air; but it feems very extraordinary, that hepatic air and vitriolic air should be condensed, and in great measure converted into sulphur by their mutual action on each other, particularly as they both feem nearly of the fame species, or at least nearly allied to each other. The attraction of two bodies, thus circumstanced, is certainly very extraordinary; yet that their union proceeds from attraction feems pretty evident, for concentrated vitriolic acid, and particularly volatile vitriolic acid, precipitates fulphur copiously from hepatised water. Volatile vitriolic acid frequently holds some sulphur in folution, as appears from the experiments of Dr. PRIESTLEY and M. BERTHOLLET; and hence it deposits some when it loses its aërial form, or by mere length of time; but the whole of this condensed air is not turned into sulphur, for the water that washed the precipitated sulphur took up a quantity of volatile acid and fixed air, as has been shewn.

The condensation of hepatic air by nitrous air seems owing to the same cause; for when the nitrous air was in great degree deprived of superfluous acid, the condensation of the hepatic was much slower; and that which after all took place seems to have been effected by the decomposition of the nitrous air, and the consequent extrication of an acid.

The

The decompositions effected by fixed and volatile livers of fulphur obviously proceed in most cases from a double affinity.

### SECTION VIII.

# Of Phosphoric Hepatic Air.

As phosphorus, in respect to its constituent parts, bears a strong resemblance to sulphur, I was naturally led to examine its phænomena when placed in the same circumstances: I therefore gently heated about 10 or 12 grains of phosphorus. mixed with about half an ounce of caustic fixed alkaline solution, in a very small phial, furnished with a bent tube, and received the air over mercury. Upon the first application of heat two fmall explosions took place, attended with a yellow flame and white smoke, which penetrated through the mercury into the receiver; these were followed by an equable production of air. At last the phosphorus began to swell and froth, and fearing the rupture of the phial, I stopped the tube to prevent the access of atmospheric air, and removed the phial to a water tub. intending to throw it in; but in the mean while the phial burst with a loud explosion, by reason of an obstruction in the tube, and a fierce flame immediately issued from it. However I obtained about 8 cubic inches of air.

This air was diminished very slightly, by agitation with an equal bulk of water, and then became cloudy like white smoke, but soon after recovered its transparency. Upon turning up the mouth of the tube to examine the water, the unabsorbed air instantly took sire, and burned with a yellow slame without exploding, leaving a reddish deposit on the sides of the tube.

Water impregnated with phosphoric air, and over which this air had burned, slightly reddened tincture of litmus:

Did not affect Prussian alkali:

Had no effect on the nitrous folutions of copper or lead, zinc or cobalt, nor on marine folution of iron or tin, or of tin in aqua regia, nor on the vitriolic folutions of iron, copper, tin, lead, zinc, regulus of antimony, arsenic, or manganese; nor on the marine folutions of iron, copper, lead, zinc, cobalt, arsenic, or manganese.

But it precipitated the nitrous folution of filver black, and vitriol of filver brown; also nitrous folution of mercury made without heat brown and black; but vitriol of mercury first became reddish, and afterwards white; and sublimate corrosive yellow and red mixed with white.

Gold dissolved in aqua regia is precipitated purplish black, and from the vitriolic acid brownish red and black; but regulus of antimony in aqua regia is precipitated white by this phosphorated water.

The nitrous folution of bismuth shewed first a white, and presently after a brown precipitate. Vitriol of bismuth and marine salt of bismuth were also precipitated brown; this latter re-dissolved by agitation.

The nitrous folution of arfenic also became brown, but redisfolved by agitation.

I afterwards impregnated some water with this air, without suffering the air to burn over it: it scarcely affected litmus, did not precipitate lime-water; but it caused a black precipitate in solution of silver, a white precipitate of regulus of antimoxy in A, and a whitish yellow in that of sublimate corresive.

To a measure of this air I let up a measure of water, and through this some small bubbles of common air; every bubble slamed.

flamed and produced a white smoke until about half as much common air was introduced as there was originally of phosphoric; and yet the original bulk did not appear increased; the flame each time produced a small commotion, and a smoke descended after inflammation into the water: when slame coased to be produced, smoke still followed the introduction of more common air. Bubbles of phosphoric air, escaping through mercury into the atmosphere, slame, crackle, and smell, exactly like the electric spark \*.

To a measure of phosphoric air I let up a half measure of nitrous air: a white smoke appeared, with an exceeding slight diminution, and the transparency was soon restored, a slight scum being deposited on the sides of the jar. Another half measure of nitrous air produced no smoke or diminution; but on adding water, and agitating the air in it, much more of it was absorbed. Upon turning up the jar the nitrous air first escaped in the form of a red vapour, and this was followed by a whitish smoke. The water had a phosphoric smell, and precipitated the solution of silver brown. In this experiment the acid of the nitrous air seems to have acted the same part that it does in hepatic air.

Phosphoric air was scarce at all diminished by the addition of an equal measure of alkaline air; and water being put up to these, took up in appearance little else than alkaline air, yet on turning up the mouth of the jar, the residuary air smoked without staming.

<sup>\*</sup> A few months after I made these experiments on phosphoric air, the tenth volume of the Mémoires des Savans Étrangers was published; and in this I found, that the spontaneous inflammation of this air was known to M. Gingember in the year 1783. His experiments are now published in Rozzer's standard for October, 1785.

The water, thus impregnated, had exactly the smell of onions. It turned tincture of radifnes green.

It precipitated folution of *filver* black; and that of *copper* in the nitrous acid brown; but this precipitate was re-diffolved by agitation, and the liquor became green. Sublimate corrofive was precipitated yellow mixed with black.

Iron was precipitated white, both from the vitriolic and marine acids; but a pale yellow folution of it in the nitrous acid was not affected; and a red folution of it in the same acid was only congrumated.

Regulus of antimony in aqua regia gave a white, cobalt in nitrous acid a very slight reddish, and bismuth in the same acid a brown precipitate.

But neither the nitrous folution of lead or zinc, nor that of tin in marine acid or aqua regia, nor that of regulus of antimony in aqua regia, were any way affected.

Fixed air, mixed with an equal proportion of phosphoric air, produced a white smoke, some diminution, and a yellow deposit. On agitating the mixture in water, the fixed air was taken up all to one-tenth. The residuum smoked, but did not inflame spontaneously.

To a small portion of phosphoric air I introduced some precipitate per se. It soon grew black, and a white smoke appeared. In two days the precipitate remained solid, yet acquired a shining pale white colour, like that of steel: the air lost its spontaneous inflammability; but I am not certain that this want of inflammability did not proceed from some other cause; for two days after I made this air, I sound a quantity of it, which had rested all night on water, had deposited a yellow scum on the sides of the jar, and lost its spontaneous inflammability next morning. The temperature of the air was

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then 53°; and when it inflamed before, the temperature was 68°.

From these few experiments, which the small quantity of air I then obtained did not suffer me to repeat, I think we may conclude, that phosphoric air is nothing else but phosphorus itself in an aërial state, and differs from sulphur in this, among other points, that it requires much less latent heat to throw it into an aerial form, and hence may be disengaged from fixed alkalies, without the assistance of an acid.



VI. Observations on the Affinities of Substances in Spirit of Wine, In a Letter to Richard Kirwan, Efg. F. R. S. by John Elliot, M. D.

## Read January 19, 1786.

3 I R,

IN your excellent papers on the attractive powers of the mineral acids, you show that metallic calces have stronger attractions to those acids, than alkalies and earths. The following experiments not only confirm this doctrine, but also a position that I have lately ventured to advance \*, " that cer-"tain decompositions will take place in spirit of wine, which " will not at all in water, nor in the dry way."

I have shewn, that if expressed oil be mixed with slaked lime into a paste, so as to form calcareous soap, and mild alkali be added, the latter will not decompose the former, either in water or by fusion. But that if spirit of wine be fubstituted for water, an alkaline foap and mild calcareous earth will be formed. As fea falt contains the fossil alkali, and as by your table of affinities acids have stronger attraction to metallic calces than to alkalies, I concluded, that if sea falt were added to a metallic foap, a fimilar double decomposition would take place.

X 2

<sup>\*</sup> In an Appendix to the second edition of the " Elements of the Branches of " Natural Philosophy connected with Medicine."  $T_0$ 

To try this I took some diachylum, which had been bought at Apothecaries-Hall, and added to it sea salt; then covered them to a sufficient height with spirit of wine, and set the bottle over the fire. Soon after they had boiled, the decomposition of the diachylum began to be apparent. When the boiling had continued some time, I removed the vessel from the fire, and after it had stood a few minutes, decanted the clear liquor while hot; then evaporating it, obtained a true alkaline soap. The residuum of course contained a quantity of calx of lead, combined with marine acid.

But much of the diachylum remained either wholly or partly undecomposed: I therefore added more sea salt and spirit of wine, and obtained a surther yield of soap. But though much sea salt remained behind, diachylum was still found in the residuum. I found, indeed, that if the ingredients were previously freed from their water, the process succeeded to somewhat better advantage.

From five ounces of diachylum I did not get quite three ounces of foap. This foap was likewise soft, and contained a portion of oil not combined with a sufficient quantity of alkali. The oil, I suppose, had existed in a similar state in the diachylum: and I remarked, that as the spirit evaporated, it gave out the true soap first, the unsaturated oil not till afterwards; so that the latter might easily be obtained separate from the former.

If too much falt was employed, much of it was taken up by the liquid, and communicated to the foap, at least if the ingredients had not been previously deprived of their water. To separate this falt I dissolved the soap in hot water. When the liquor was cold, the soap sloated at top, the salt remaining in the water underneath. If too little salt was used, this inconvenience inconvenience did not happen, or not in so great a degree, though then less soap was of course obtained.

As diachylum, though with a greater proportion of litharge, and boiled longer than that I had from the Hall, still contained oil not sufficiently saturated, I made the metallic soap in another way. To a solution of sugar of lead in water I added a solution of alkaline soap in the same liquid. A double decomposition took place, the oil uniting with the calx of lead, the alkali with the acid of salt. Using this metallic soap instead of the other, I obtained an alkaline soap harder and more perfect than in the preceding process; but still sound that part of the oil remained with the calx of lead in the residuum, and adhered so firmly, that repeated quantities of sea salt and spirit of wine did not wholly separate it.

As I have given this process more with a philosophical view than any other, I have been thus particular in my account of it, to shew that however eligible it may appear at first view, it will not answer for making soap for common sale. The alkali indeed is procured much cheaper than from barilla, as the lead may be revived and re-calcined into litharge. But the whole of the oil or fat cannot easily be converted into soap, though in order the better to effect it, I have mixed fand with the diachylum: and as the oil and litharge must, in the large way, be united by boiling, a confiderable part of the former will not be sufficiently saturated. Fuel must be used, not only for forming the metallic foap, but likewise for decomposing that foap, and then distilling off the spirit, which will also require additional time and labour. The quantity of spirit of wine lost, though the process (so far as that liquid is concerned) be performed in a still, will alone nearly counterbalance the faving in respect to alkali. And in the process itself therethere is confiderable danger, not only of the spirit taking fire from the carelessies of the workmen, but likewise from the frequent explosions that happen during the decomposition of the metallic sorp.

As in the experiment with calcareous earth and mild alkali, fo in this, I found that the decomposition would not take place when water was used, nor by fusion. In the latter case, I found that the salt was so strongly attracted, that it quitted its water of crystallisation to unite to the metallic soap. If spirit of wine was added to this mass, a double decomposition took place, as already described.

Instead of sea salt, I added to diachylum GLAUBER's sait, freed from its water of crystallisation by heat. I expected that it would have acted on the metallic soap more speedily than the sea salt; but the contrary appeared on trial. On adding a small quantity of sal sodæ, the decomposition went on better, and sufficiently to shew that the ingredients were capable of acting on each other. And I suppose, from your table, that other neutral and earthy salts will have a similar effect, especially if deprived of any superfluous acid by the addition of a little alkali or earth; though I have not made the trials.

Professor Bergman has divided his table into two parts; the affinities as they take place in the moist, and in the dry way. But these experiments shew, that in the moist way the affinities take place differently, according as water, or spirit of wine, is used. Perhaps a like difference would be found on using other liquids, each of which would probably afford a different table: for much depends on the attraction which the ingredients themselves have to the liquid employed, as I have endeavoured to shew in the work before referred to; for the liquid is to be considered as one of the ingredients.

I beg leave to add, Sir, that I think I have fince hit upon a better method of making foap, and without spirit of wine; but as I have not yet made all the experiments on this subject that I intended, I cannot at present give you an account of them. If they succeed, I will take the liberty to acquaint you with the result.

I am, Sir, with the greatest respect, &c.

J. ELLIOT.

Great Marlborough-Street, October 31, 1785.

P. S. Since writing the above I have found, that if mild fixed alkali be added to diachylum in hot water, they unite into a gelatinous mass, which is miscible with the water. This may be considered as a kind of bepar. If this substance be put into hot spirit of wine, the decomposition already described takes place. If chalk be substituted for alkali, there is a similar result. I have found that nitre is decomposed by diachylum in spirit of wine. I have also found, that if the compound of diachylum and common salt be put into hot spirit of turpentine, the diachylum is dissolved, but the salt remains at the bottom of the vessel.



VII. An Account of some minute British Shells, either not duly observed, or totally unnoticed by Authors. In a Letter to Sir Joseph Banks, Bart. P. R. S. by the Rev. John Lightsoot, M. A. F. R. S.

## Read January 26, 1786.

DEAR SIR,

A S you were pleased to think a few shells, which I lately submitted to your inspection, might not be unworthy the notice of the Royal Society; encouraged by so respectable an opinion, I shall now beg leave to lay before you some Drawings which I have caused to be made of them, together with such remarks concerning them as may tend, in some degree, to illustrate their natural history.

The first I shall mention is an univalve, coiled up into a spiral form, the cavity of which is divided into three, sour, or more distinct chambers or apartments by solid transverse septa, which communicate with each other by a trivadiated aperture.

These characters accord with no genus of shells, hitherto established, so well as the Nautilus. It is true, it has not so many chambers as others of that genus, nor are the apertures of the septa of a tubular form; but as these, according to the laws of method, are to be considered as marks of a specific rather than generic nature, so I shall not hesitate to refer the shell under consideration to the samily of Nautilus, at least till

we are authorised, by the discovery of many more of a similar structure, to rank it under a new genus.

That I may give a more full and specific description of this singular shell, it must be observed, that its sigure is a flatted spiral, umbilicated on one side, convex on the other, but yet slightly depressed in the centre, measuring in diameter about a quarter of an inch; that it is generally couled up into sour volutions, which are convex above, and so nearly plane beneath as to form an acute or carinated margin; and that each of these volutions, on the upper side, has a narrow thread-like border or sillet on the interior edge. The front view of the mouth is obliquely semioval, the upper edge projecting farther than the lower.

The substance of the shell is very brittle and pellucid, and, when alive, of a reddish brown or chesnut colour throughout, except about three or four faint white lines, which appear like rays running from the central umbilicus to different and nearly equidistant parts of the circumference. These white lines are not straight, but shaped each like a short curve, or comma, on the upper side, and are nothing else but the shades of the septa in the cavity of the shell.

Such is its external appearance. The internal structure is extremely curious; for the whole cavity is divided into three, four, or five chambers or compartments (according to the age of the shell) at nearly equal distances, by transverse septa of a hard white brittle semipellucid substance, resembling agate or enamelled glass. Each of these septa has a triradiated aperture not unlike the Greek capital upsilon, or the Roman Y, inverted, (X) through which the animal, by means of its soft compressible and extensible nature, easily contrives to extrude Vol. LXXVI.

itself, as much as is necessary, when in search of food, or in the act of moving from one place to another.

It may not be amiss here to observe, that the fepta abovementioned are totally foreign, both in use and structure, from what are called opercula in other shells: I mean those temporary covers or stoppers, made use of by many testaceous animals to close up the mouths of their shells, and defend them from injury in their quiescent state.

The opercula, however various in substance, are always observed to be fingle, imperforate, moveable at the will of the
animal, and constantly placed, as a security, in the mouth,
never in any other part of the cavity of the shell; whereas the
septa, in the subject now before us, are repeatedly constructed
in several parts of the cavity, are all of them perforated, intimately connected with the substance of the shell, and consequently fixed and permanent, as in all the Nautili.

And as to the use of these septa, though I dare not say what might be the real intention of nature in their formation, yet it will be no presumption to affirm, that they could not be designed for the same purpose as opercula in other shells; not only because they are placed where they cannot answer the same end, but more especially on account of their open structure, which intirely excludes them from the possibility of affording a proper defence to the enclosed animal.

Should it be faid, that they only serve to point out the different periods or stages of the shell's growth, and are nothing else but the limits or terminations of the animal's periodical increase, I will not dispute the opinion; it may perhaps be very true; but supposing it to be so, is it not equally probable, that the transverse septa in all the Nautili are nothing else?

But I must not conclude my remarks without taking some notice of the inhabitant of this fingular shell. It appears to be of the flug kind, but differs from the common land forts in this respect, that the Antennæ are filiform, and the eyes not placed upon their fummits and retractile, but fixed upon the head near their bases, as is probably the case in all the truly aquatic kinds, at least in all such as I have hitherto examined. The animal is of a foft and flexible nature, and grey brown colour, and has a power of extending itself out of the shell through the aperture of the exterior feptum; at which time it affumes a triradriated shape, not very dissimilar from the aperture itself, or like an inverted Y ( , ), the thickest ray of which is the head and body; one of the lines which form the angle is the tail, and the other is a kind of dorfal ligament, which extends from the back of the animal, through one of the rays of the aperture, and through the whole cavity of the shell, and all its septa, to the centre, as may be seen by placing the fhell between the eye and the light (fee fig. 3. Tab. I.).

In the concise LINNEAN mode of description this shell may be named,

Nautilus (lacustris) testa spirali compressa umbilicata carinata, ansractibus tribus supra convexis contiguis, apertura semiovata, septis triradiato-persoratis.

The Fresh-water Nautilus.

I find no author who has taken any notice of this shell, except Mr. WALKER, who, in his late curious publication on Minute Shells, has described it under the name of

Helix lineata dorso convexo umbilicata margine acuto; and has given a figure of it in the same work, Pl. I. fig. 28.

But this ingenious gentleman is free enough to confess, that its chambered structure had entirely escaped his notice, Y 2 otherwise otherwise he would doubtless not have ranked it among the

The place where the shell is to be found, is in deep ditches of clear water, adhering to the roots of Carices. It was collected near Upton Church, not far from Eton, in Buckinghamshire, in the spring season. Mr. Walker reports it to be found on slags in Hornhill Brooks, in Kent, but very rare.

The figures annexed will explain what I have been describing much better than words.

- Fig. 1. (Tab. I.) The shell of its natural size, with the umbilicated side uppermost.
- 2. The same with the depressed side uppermost; the dark shade in both shewing how far the cavity of the shell is occupied by the dead animal included.
- 3. The shell magnified with the depressed side uppermost, shewing the live animal within it, its head and antennæ protruded. Here the white lines appear double, being the shade of the septa on both sides of the shell.
- 5. The same magnified with the umbilicated side uppermost, the head and under side of the animal appearing to view.
- 4. The fame magnified in a perpendicular view, with the mouth in front, but cut away down to the first feptum, in order to shew not only the carina or keel of the shell, but more especially the exact appearance of the triradiated feptum nearest the mouth, and in what manner the animal contrives to extrude itself through the aperture, the head and tail being accommodated to pass through two of the parts of the inverted Y (X), while the dorsal ligament occupies the third.
  - 8. The animal's excrement.
- 6. 7. Horizontal sections of the shell, in order to shew the internal structure, or the appearance of the septa, when the shell

shell is ground down or divided in that direction. Fig. 6. shewing the shell ground away in part, with its umbilicated side uppermost. Fig. 7. the same more deeply and evenly ground, with the depressed or more convex side uppermost.

The fecond shell I shall take notice of has much of the same external face with the preceding, and is nearly of the same size and colour, but materially differs from it in having an uninterrupted cavity from the mouth to the center; that is, no divided chambers or compartments. This therefore evidently belongs to the genus of Helix.

It is strongly umbilicated on one side, and almost plane on the other, the central wreaths being nearly of equal height, or but slightly depressed, and destitute of that narrow border or sillet mentioned in the preceding shell. It consists most commonly of three volutions, convex on both sides, with an obtusely carinated margin, and semioval mouth.

It may be named,

Helix (fontana) testa compressa obtuse carinata, hinc umbilicata, anfractibus tribus utrinque convexis, apertura semiovata.

Fountain Helix.

The figures here given represent this shell, on both sides, in its natural and magnified state, so that more words to describe it are needless.

- Fig. 1. (Tab. II.) The shell of the natural size, with the most convex side uppermost.
  - 2. The same, with the umbilicated side uppermost.
  - 3. The shell magnified, the most convex side uppermost.
  - 4. The same magnified, the umbilicated side uppermost.

I do not find that it has been noticed by any author.

It was found in the bottom of a spring of clear water, adhering to the under side of rotten leaves, near Bullstrode, in Buckinghamshire, in the month of April. It has also been found in some other clear waters in the same neighbourhood, but not common.

A third shell I have to mention is a very minute but curious Helix of a subconical form, consisting of about five convex wreaths, gradually diminishing towards the apex. The shell is umbilicated at the base, and the wreaths are transversely surrounded with numerous sharp-edged rings, which are produced in the middle or back of each wreath into a kind of spur, formed of compressed and very tender spines. The mouth is a segment larger than a semicircle, but not round enough to constitute the shell a Turbo, to which it is nevertheless nearly allied. The colour of the whole shell is brown.

It may be named,

Helix (*spinulosa*) testa subconica umbilicata, anfractibus 5 convexis, annulis membranaceis acutis cinctis, dorso spinuloso-carinatis, apertura suborbiculari.

Tender prickly Helix.

The figures here given represent this shell in different positions, in its natural and magnified state.

Fig. 1. 2. (Tab. II.) The shell, in different positions, of the natural size.

3. 4. 5. The same magnified.

I know no author who has hitherto noticed it.

It was found near Bullstrode, at the foot of pales, upon old bricks and stones, after rainy weather, in June and July.

A fourth is a minute shell of the Turbo kind.

It strongly resembles the depressed Helices; but its circular mouth forbids its being ranked in that genus.

It confifts of four cylindric or rounded volutions, of nearly equal height on one fide, but funk or umbilicated on the other. These volutions are transversely surrounded with numerous sharp-edged membranaceous rings, which are very fragile and deciduous. The mouth, when perfect, is bordered with a compressed erect margin. The colour of the shell is uniformly brown.

It may be named,

Turbo (helicinus) testa depresso-plana, hinc umbilicata, anstractibus 4 torosis, annulis numerosis acutis membranaceis cinctis.

The fine-ringed Turbo.

The figures herewith exhibit both sides of the shell, in its natural and magnified state.

Fig. 1. 2. (Tab. III). The shell, on both sides, of the natural fize.

3. 4. The same, on both sides, magnified.

No author, that I know of, has described it.

It was found near Bullstrode, upon bare stones, in the spring season, and at other times in moist weather.

The fifth and last shell I have to mention, is a small thin oblong compressed Patella, of a horn colour, about a quarter of an inch long, and one-tenth of an inch wide, having a pointed vertex nearest to the lower end, turned downwards, and leaning to one side.

It may be called,

Patella (oblonga) testa integerrima oblonga compressa membranacea, vertice mucronato reflexo obliquo.

Oblong fresh-water Patella.

It is perfectly distinct from the Patella lacustris of LINNEUS both in shape, and slexure of the vertex, as well as being destitute of radiated streaks.

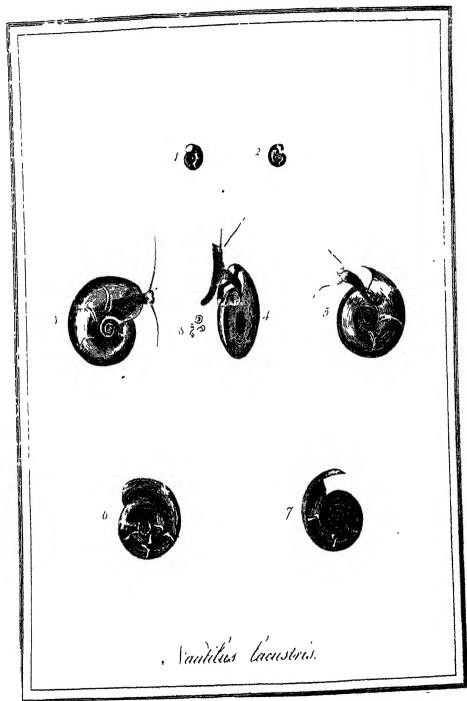
Fig. 1. 2. 3. and 4. (Tab. III.) The natural fize in different attitudes.

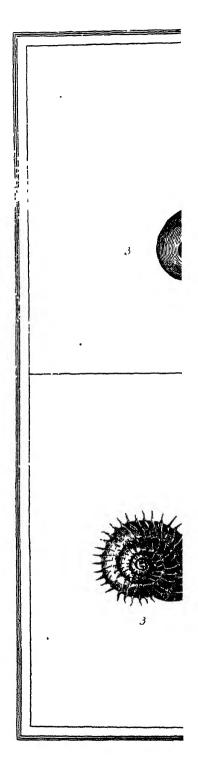
- 5. A shell magnified, with its vertex upward.
- 6. Patella lacustris Lin. shewing the plan of the two different species.

It has escaped the notice of all the authors I am acquainted with.

It was found adhering to the leaves of the Iris Pseudacorus in waters near Beaconsfield, in Buckinghamshire, by Mr. Agnew, Gardener to the late Duchess Dowager of Port-LAND; by whose sagacity all the preceding shells were discovered, and by whose faithful pencil they were drawn.

I have now done with describing the shells I intended; but before I conclude, it may not be thought, perhaps, quite foreign to my present subject, to remove, in some degree, an error which has been almost universally adopted by the dealers and collectors in shells, respecting certain subjects, brought from Jamaica, and other parts of the West-Indies, commonly known by the name of Gold Shells. They are yellow glossy substances, of an obtusely conical figure, and size of tares or vetch-seeds, composed of several concave brittle imbricated scales, closely compacted, so as to resemble the soliaceous gem or bud of some tree, and have generally a hole or perforation in some part. These are commonly supposed to be shells, or the











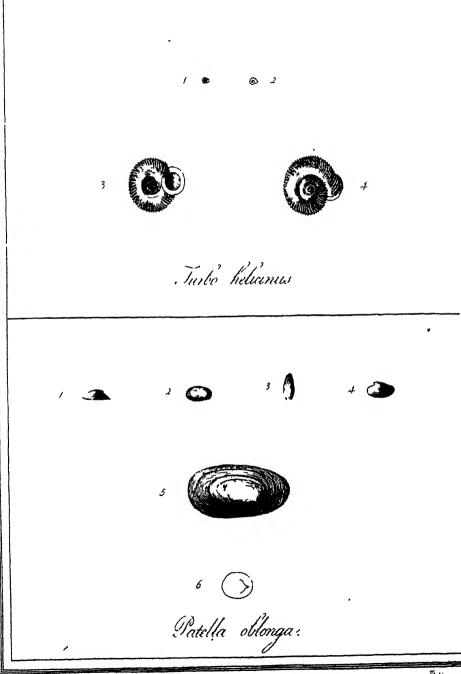
Helix fontuna







Hélix spinulósa.



embryos of shells taken out of some bag or ovary. It is certain. however, that this is a mistake; for having collected a few of the largest and most opaque of these supposed shells, and such as had no perforation to be found in them, I immersed them for a few minutes in hot water, and then carefully developing the scales of which they were composed, I found in the centre of all the largest and most perfect a small insect, enveloped in a mealy substance, about the fize of a finall bed-bug, of a roundish oval figure, dark brown colour, convex on the back, flightly concave beneath, and in every instance, except one (out of at least fifty which I opened), all without wings. The body was composed of about eight imbricated fegments or rings; the head was very fhort, and almost concealed under the margin of the thorax; however, I plainly discerned, in some of the specimens, that it was furnished with two short filiform antennæ. The trunk had fix legs; the feet terminated each with a sharp red claw. The body of the fingle specimen which had wings was oblong, and narrower than the apterous ones. The wings appeared to be glued down to the body, just as in a bee or wasp, when it is almost ready to emerge from the Pupa state. Whether they were two or four wings I am not absolutely certain; but they appeared to be of the filmy transparent kind, at least near the extremities; for I clearly perceived the nerves as in the wings of a fly. From hence it evidently appears, that these Gold Shells are really no other than the cases or cells of an infect in its Pupa state; and from considering the form of its body, the difference of the sexes, the one being apterous, the other winged, I have no doubt but it is a species of cochineal or coccus, and probably one not hitherto described by naturalists. The cases do not effervesce with acids, therefore they are not of a testaceous nature. They seem to be a vegetable Vol. LXXVI.  $\mathbf{Z}$ 

table substance of the resinous kind; for they bubble a little on being burnt on a hot iron, and when triturated dissolve slowly in a warm spirituous menstruum to a sweet-smelling viscid matter. But we must wait for a better elucidation of the subject from those who collect these substances in their native place.

I have the honour to be, with the utmost respect, &c.

JOHN LIGHTFOOT.



## F 171 7

VIII. Observations on the Sulphur Wells at Harrogate, made in July and August, 1785. By the Right Reverend Richard Lord Bishop of Landaff, F. R. S.

#### Read February 2, 1786.

IN 1733, when Doctor Short first published his Treatise on Mineral Waters, there were only three sulphur wells at Harrogate; there are now four. I made fome inquiry respecting the time and occasion of making the fourth well, and received the following account from an old man, who was himself principally concerned in the transaction. About forty years ago, a person who, by lease from the Earl of Burlington, had acquired a right of fearthing for minerals in the forest of Knaresborough, made a shew as if he had a real intention of digging for coal, on the very fpot where the three fulphur wells were fituated. This attempt alarmed the apprehensions of the inn-keepers and others at Harrogate, who were interested in the preservation of the wells: they gave him what legal opposition they could, and all the illegal that they durst. At length, for the fum of one hundred pounds, which they raifed amongst themselves, the dispute was compromised, and the defign real or pretended of digging for coal was abandoned. Sulphur water, however, had risen up where he had begun to dig. They inclosed the place with a little stone edifice; and putting down a bason, made a fourth well. By a chause in the act of parliament for including Knaresborough Forest, passed in  $Z_2$ 

in 1770, it is rendered unlawful for any person whatever to fink any pit, or dig any quarry or mine, whereby the medicinal springs or waters at Harrogate may be damaged or polluted; so that no attempts of the kind above-mentioned need be apprehended in suture.

This fourth well is that which is nearest to one of the barns of the Crown-Inn, being about ten yards distant from it. In digging, a few years since, the foundation of that barn, they met with sulphur water in several places. At a very little distance from the four wells there are two others of the same kind; one in the yard of the Half-Moon-Inn, discovered in digging for common water in 1783, and another which breaks out on the side of the rivulet below that Inn. On the banks of that rivulet I saw several other sulphureous springs: they are easily distinguished by the blackness of the earth over which they slow.

On the declivity of a hill, about a quarter of a mile to the west of the fulphur wells at Harrogate, there is a bog which has been formed by the rotting of wood: the earth of the rotten wood is in some places four feet in thickness, and there is a stratum consisting of clay, and small loofe decaying fand-stones, every where under it. The hill above is of grit-stone. In this bog there are four more fulphur wells; one at the top, near the rails which separate the bog from the Common; and three at the bottom, though one of these, strictly speaking, is not in the bog but at the fide of it in the stratum on which the bog is situated, and at the distance of a yard or two from a rivulet of fresh water, which runs from thence to Low Harrogate, passing close to the fide but above the level of the fulphur wells of that place. On the other fide of the hill, above the bog, and to the west of it, there is another fulphur well on the fide of a brook; and it has been thought that the wells both at Harrogate and in the bog are supplied from this well. In a low ground, between High Harrogate and Knoresborough, there is a sulphur well; another to the north of it in Bilton Park, at about the distance of a mile; and another to the south of it, at a less distance, was discovered this year in digging for common water by a person of the name of RICHARDSON; and, lastly, there is another at a place called Hookstone Crag: none of these last mentioned wells are above two miles distant from High Harrogate; and by an accurate search a great many more might, probably, be discovered in the neighbourhood.

It is not unufual to dig within a few yards of any of these sulphur wells, and to meet with water which is not sulphureous. I ordered a well to be dug in the fore-mentioned bog, sixteen yards to the south of the sulphur well which is near the rails, and to the same depth with it; the water with which it was presently silled was chalybeate, but in no degree sulphureous. I had another well dug, at about thirty yards distance from the three sulphur wells which are situated at the lower extremity of the bog; this well, by the declivity of the ground, was ten or twelve feet below their level, but its water was not sulphureous. From the first well which I dug, it is evident, that every part of the bog does not yield sulphur water; and from the second, which was sunk into the clay, it is clear that every part of the stratum on which the bog is placed does not yield it, though one of the wells is situated in it.

The sulphur wells at Harrogate are a great many feet below the level of those in the bog; but they communicate with them, if we may rely on what Doctor Short has told us—
"That about the beginning of this century, when the concourse of people was very great to the Spaw at Harrogate, one ROBERT WARD, an old man, made a bason in the clay under

the moss of a bog where the strongest and briskest of these sulphur springs rise, and gathered half an hogshead of water at a time for the use of the poor; but when he laded this he almost dried the three sulphur wells at the village, whence it is evident, that all have the same origin and communicate with one another." By converfing with some of the oldest and most intelligent people at Harrogate, I could not find that they entertained any opinion of the water at the bog having a communication with that at the spaw. This circumstance might easily be ascertained; and, if the fact should be contrary to what Doctor SHORT fupposed, the wells at the bog ought to be covered from the weather as those at the village are; they would by this mean yield great plenty of water for the baths which are wanted by invalids, and which are often very scantily supplied by the wells at Harrogate, notwithstanding the attention which is used in preserving the water which springs at the four wells, by emptying them as often as they become full during both the day and night time. And indeed it is furprifing, that the well on the fide of the rivulet below the Half-Moon-Inn, which is so well situated for the purpose, has never been inclosed for the furnishing sulphureous water for the baths. The present mode of carrying the water in casks to the feveral houses where the persons lodge who want to bathe in it, is very troublesome, and the water thereby loses of its virtue. Some of the wells about the village, that for inflance which has been discovered at the Half-Moon-Inn, the water of which, I believe, fprings from a different fource from that which supplies the four sulphur wells, should be either enlarged to a greater horizontal breadth, or funk to a greater depth, in order to try, by one or both of these ways, whether the quantity and strength of the water might not be increased; and and if that should, as it probably would be the case, one or more baths might be crected after the manner of those at Buxton and other places; or, by proper additional buildings, warm bathing in sulphureous water might be practifed, as is done in common water in the bagnios in London. The faltness of the fulphureous water, if that should be thought useful, might eafily be made even greater than that of fea water, by adding a quarter of a pound of common falt to every gallon of the water used in forming a bath. The waters at Harrogate, though they have long been very beneficial, have not yet been rendered fo useful to mankind, as an intelligent and enterprifing person might make them. The alternate strata of fand, stone, and shale, which compose the lower hills near the wells at Harrogate, dip very much, as may be feen in a stone quarry about two hundred yards from the wells; and the same circumstance may be observed in dry weather, in following the bottom of the brook from the village up to the bog; and hence, if there be a communication between the waters of the bog and of the village, as Doctor Short afferts, it is probable, that the same stratum of shale which is seen at the bottom of the wells at the village, breaks out again at the bog above the village, and that the water finds its way from the bog to the village through the crevices of that stratum.

After having observed, as carefully as I could, the number and situation of the sulphur wells about Harrogate, I tooknotice of the temperature of the sour at the village. In the month of June, 1780, when the thermometer in the shade was 72°, and the pump water at the Granby-Inn, the well of which is sifty feet deep, was 48°, the strongest of the sulphur wells, being that of which invalids usually drink, was 50°. On the 29th of July in this year, after the earth had been parched with.

with drought for many months, the heat of the strongest well was 54°; the water of the Granby pump was on the same day 48°, and the heat of the air in the shade 76°. Doctor WALKER, who has lately written a treatise on Harrogate water, says, that the heat of this spring was 48°, when that of an adjoining rivulet was 53°. And I have little doubt in believing, that if the experiment was made in cold weather, the temperature of the same well would be found to be several degrees below 48. This variation of temperature in the fulphur water indicates its fpringing from no great depth below the furface of the earth: or at least it indicates its having run for a considerable distance in a channel so near to the surface of the earth, as to participate of the changes of temperature, to which that is liable from the action of the fun. But the heat of the fulphur water is not only variable in the same well, at different times, but it is not the same in all the wells at the same time. call the strongest well the first, and reckon the rest in order, going to the right, the third well, which is reckoned the next strongest, was 57° hot when the first well was 54°. In support of the conjecture that the fulphur water of the strongest well would in a cold feafon make the thermometer fink below 48°, which is the constant temperature of springs situated at a great depth in the earth in this country, it may be observed, that though the first and the third well are never frozen, yet the second and the fourth well are frozen in severe weather. When the fecond and the fourth well are covered with icc. it is probable, that the first and the third have a temperature far below 48°; but that the fea falt, which is more abundant in them than in the other two wells, and which of all falts relists most powerfully the congelation of the water in which it is diffolved, preserves them from being frozen in the coldest feasons incident to our climate.

As the temperature of these four wells is not the same in all of them at the same time, nor invariable in any of them. fo neither does there feem to be any uniformity or constancy in them, with respect to the quantity of falt which they contain. The falt with which they are all impregnated is of the same kind in all, and it is almost wholly common salt; and though the quantity contained in a definite portion of any one of the wells is not, I think, precifely the same at all seasons of the year, yet the limits within which it varies are not, I apprehend, very great. A method is mentioned in the LXth volume of the Philosophical Transactions, of estimating the quantity of common falt diffolved in water, by taking the fpecific gravity of the water: this method is not to be relied on, when any confiderable portion of any other kind of falt is diffolved along with the fea falt; but it is accurate enough to give a good notion of the quantity contained in the different wells at Harrogate. On the 13th of August, after several days of rainy weather, I took the specific gravities of the four Sulphur wells at the village, the drinking well being the first .-Rain water 1.000; first well 1.009; second well 1.002; third well 1.007; fourth well 1.002. By comparing these specific gravities with the table which is given in the LXth volume of the Transactions, it may be gathered, that the water of the first well contained 7's of its weight of common falt; that of the second and fourth, 318; and that of the third, 31. After four days more heavy rain I tried the strongest well again, and found its specific gravity to be 1.008. It is worthy of observation, that the water, as it springs into the first and third well, is quite transparent, but usually of a pearl colour in the second and fourth. Vol. LXXVI. A a

fourth, similar in appearance to the water of the first or third well after it has been exposed a few hours to the air; hence it is probable, that the external air has access to the water of the fecond and fourth well before it springs up into the bason. A great many authors have published accounts of the quantity of common falt contained in a gallon of the water of the strongest well; they differ fomewhat from each other, fome making it more, others less, than two ounces. These diversities proceed either from the different care and skill used in conducting the experiment; or from a real difference in the quantity of falt with which the water is impregnated at different feafons of the year. The medium quantity of falt contained in a gallon falls. fhort of, I think, rather than exceeds two ounces. The fea water at Scarborough contains about twice as much falt as is found in the strongest sulphur well at Harrogate. The sulphur wells at the bog are commonly faid to be fulphureous, but not feline. This, however, is a mistake; they contain falt, and falt of the same kind as the wells at the village. I could not diffinguish the kind of falt by the method in which I had effimated the quantity contained in the fulphur wells; I therefore evaporated a gallon of the water of the well in the bog which is near the rails, and obtained a full ounce of common falt, of a brownish colour: the colour would have gone off by calcination. In what degree the medicinal powers of Harrogate water depend on its fulphureous, and in what degree on its faline impregnation, are quaftions which I meddle not with: I would only just observe on this head, that any strong sulphureous water, such as that of Keddlestone in Derbyshire, or of Shap in Westmoreland, which naturally contains little or no sea falt, may be rendered similar to Harrogate water, by diffolving in it a proper proportion of common falt. The four fulphur fulphur wells at Harrogate are very hear to each other; they might all be included within the circumference of a circle of feven or eight yards in diameter; yet, from what has been fail it is evident, that they have not all either the fame temperature, or the fame quantity of faline impregnation. This diverfity of quality, in wells which have a proximity of fituation, is no uncommon phænomenon; and though at the first view it seems to be surprising, yet it ceases to be so on reflexion: for the waters which feed wells so circumstanced, may flow through strata of different qualities situated at different depths, though in the same direction; or through strata placed both at different depths, and in different directions; and that this is the case at Harrogate is probable enough, there being hills on every side of the hollow in which the village is placed.

With respect to the sulphuseous impregnation of these waters. I made the following observations.

The infide of the bason, into which the water of the ftrongest well rises, is covered with a whitish pellicle, which may be easily scraped off from the grit-stone of which the bason is made. I observed, in the year 1780, that this pellicle on a hot iron burned with the flame and fmell of fulphur. this year repeated the experiment with the same success; the substance should be gently dried before it is put on the iron. I would further observe, that the sulphur is but a small part of the substance which is scraped off. That I might be cortain of the possibility of obtaining true palpable sulphur from what is scraped off from the bason, and at the same time give some guess at the quantity of sulphur contained in it, I took three or four ounces of it, and having washed it well, and dried it thoroughly by a gentle heat, I put two ounces into a clean glass retort, and sublimed from it about two or three grains of yellow A a 2

yellow fulphur. This fulphur, which stuck to the neck of the retort, had an oily appearance; and the retort, when opened, had not only the fmell of the volatile fulphureous acid, which usually accompanies the sublimation of sulphur, but it had also the strong empyreumatic smell which peculiarly appertains to burnt oils; and it retained this finell for feveral days. It has been remarked before, that the falt feparable from the fulphur water was of a brownish colour; and others, who have analysed this water, have met with a brown fubstance, which they knew not what to make of; both which appearances may be attributed to the oil, the existence of which was rendered so manifest by the sublimation here mentioned. I will not trouble the Society with any conjectures concerning the origin of this oil, or the medium of its combination with water; the discovery of it gave me some pleasure, as it seemed to add a degree of probability to what I had said concerning the nature of the air with which, in one of my Chemical Essays, I had supposed Harrogate water to be impregnated. I will again take the liberty of repeating the query which I there proposed. "Does this air, and the inflammable" air separable from some metallic substances, consist of oleaginous particles in an elastic state?" When I ventured to conjecture, in the Effav alluded to, that fulphurcous waters received their impregnation from air of a particular kind, I did not know that Professor BERGMAN had advanced the same opinion, and denominated that species of air, Hepatic Air. I have since then feen his works, and very readily give up to him not only the priority of the discovery, but the merit of prosecuting it. And though what he has faid concerning the manner of precipitating fulphur from these waters can leave no doubt in the mind of any chemist concerning the actual existence of sulphur

in them; yet I will proceed to the mention of some other obvious experiments on the Harrogate water, in support of the same doctrine.

Knowing that, in the baths of Aix-la-Chapelle, sulphur is found sticking to the sides and top of the channel in which the sulphureous water is conveyed, I examined with great attention the sides of the little stone building which is raised over the bason of the strongest well, and saw them in some places of a yellowish colour: this I thought proceeded from a species of yellow moss, commonly sound on grit-stone: I collected, however, what I could of it by brushing the sides of the building, at the distance of three or sour feet from the water in the bason: on putting what I had brushed off on a hot iron, I sound that it consisted principally of particles of grit-stone, evidently however mixed with particles of sulphur.

Much of the sulphureous water is used for baths at Harrogate; and for that purpose all the four wells are frequently emptied into large tubs containing many gallons apiece; thefe constantly stand at the wells, and the casks, in which the water is carried to the feveral houses, are filled from them. On examining the infides of these tubs, I found them covered, as if painted, with a whitish pellicle. I scraped off a part of this pellicle: it was no longer foluble in water; but, being put on a hot iron, it appeared to confift almost wholly of fulphur. Some of these tubs have been in use many years, and the adhering crust is thick in proportion to the time they have been. applied to the purpose; but the fulphur pellicle was sufficiently observable on one which was new in the beginning of this feafon. The water when it is first put into these tubs is transparent; when it has been exposed to the air for a few hours, it becomes milky; and, whereithe quantity, is large, a white cloud' cloud may be seen slowly precipitating itself to the bottom. This white precipitate consists partly, I am not certain that it consists wholly, of sulphur; and the sulphur is as really contained in the waters denominated sulphureous, as iron is contained in certain forts of chalybeate waters; in the one case the iron is rendered soluble in water by its being united to fixed air, or some other volatile principle; and in the other sulphur is rendered soluble in water by its being united to sixed air, or some other volatile principle: neither iron nor sulphur are of themselves soluble in water, but each of them, being reduced into the form of a salt by an union with some other substances, becomes soluble in water, and remains dissolved in it, till that other substance either escapes into the air, or becomes combined with some other body.

About forty years ago, they took up the bason of the third well, and a credible person, who was himself present at the operation, informed me, that in all the crevices of the stone on which the bason rested, there were layers of pure yellow sulphur. This I can well believe, for I ordered a piece of shale to be broken off from the bottom of the sourth well; it was split, as shale generally is, into several thin pieces, and was covered with a whitish crust. Being laid on a hot iron, in a dark room, it cracked very much, and exhibited a blue slame and sulphureous smell.

If the water happens to stand a few days in any of the wells, without being disturbed, there is found at the bottom a black sediment; this black sediment also marks the course of the water which slows from the well, and it may be esteemed characteristic of a sulphur water. The surface of the water also, when it is not stirred for some time, is covered with a whitish scum. Doctor Short had long ago observed, that both

both the black fediment, and the white fcum, gave clear indications, on a hot iron, of their containing fulphur: I know not whence it has come that his accuracy has been questioned in this point; certain I am, that on the repetition of his experiments I found them true. The white fcum also, which is found sticking on the grass over which the water slows, being gently dried, burns with the flame and fmell of fulphur. From what has been faid it is clear, that fulphur is found at Harrogate, sticking to the bason into which the water springs; fublimed upon the stones which compose the edifice furrounding the well; adhering to the fides of the tubs in which the water stands; subsiding to the bottom of the channel in which the water runs; and covering the furface of the earth, and of the blades of grass, over which it flows. It is unnecessary to add another word on this subject; it remains that I risk a conjecture or two, on the primary cause of the sulphureous inpregnation observable in these waters.

In the Chemical Essay before referred to, I have shewn, that the air separable from the lead ore of Derbyshire, or from Black-Jack, by solution in the acid of vitriol, impregnates common water with the sulphureous smell of Harrogate water; and I have also shewn that the bladder sucus or sea-wrack, by being calcined to a certain point, and put into water, not only gives the water a brackish taste, but communicates to it, without injuring its transparency, the smell, taste, and other properties of Harrogate water. Professor Bergman impregnated water with a sulphureous taste and sinell, by means of air separated by the vitriolic acid from hepar sulphuris, made by susque of equal weights of sulphur and pot-ashes, and from a mass made of three parts of iron silings melted with two of sulphur; and he found also, that Black-Jack and native Siberian iron

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iron yielded hepatic air, by folution in acids. This, I believe, is the main of what is known by chemits on this subject; what I have to suggest, relative to the Harrogate waters in particular, may perhaps be of use to suture inquirers.

I have been told, that on breaking into an old coal-work, in which a confiderable quantity of wood had been left rotting for a long time, there issued out a great quantity of water fmelling like Harrogate water, and leaving, as that water does, a white fcum on the earth over which it passed. On opening a well of common water, in which there was found a log of rotten wood, an observant physician assured me, that he had perceived a strong and distinct smell of Harrogate water. DARWIN, in his ingenious Account of an artificial Spring of Water, published in the first part of the LXXVth volume of the Philosophical Transactions, mentions his having perceived a flight fulphureous fmell and tafte in the water of a well which had been funk in a black, loofe, moist earth, which appeared to have been very lately a morafs, but which is now covered with houses built upon piles. In the bog or morass above-mentioned there is great plenty of fulphurcous water, which feems to fpring from the earth of the rotten wood of which that bog confifts. These facts are not sufficient to make us certain, that rotten wood is efficacious in impregnating water with a fulphureous finell; because there are many bogs in every part of the world, in which no fulphurcous water has ever been discovered. Nor, on the other hand, are they to be rejected as of no use in the inquiry; because wood, at a particular period of its putrefaction, or when fituated at a particular depth, or when incumbent on a foil of a particular kind, may give an impregnation to water, which the same wood, under different circumstances, would not give.

The bilge water, usually found at the bottom of ships which are foul, is faid to fmell like Harrogate water: I at first supposed, that it had acquired this smell in consequence of becoming putrid in contact with the timber on which it rested, and this circumstance I considered as a notable support to the conjecture I had formed of rotten wood being, under certain circumstances, instrumental in generating the smell of Harrogate water. But this notion is not well founded; for the bilge water is, I suppose, falt water; and Dr. Shorr says, that sea water, which had been kept in a stone bottle six weeks "ftunk not much short of Harrogate sulphur water." It has been remarked above, that calcined fea-wrack, which contains a great deal of fea falt, exhales an odour fimilar in all respects to that of Harrogate water; and in confirmation of the truth of this remark, I find that an author, quoted by Dr. Short, fays, that "Bay falt thrice calcined, diffolved in water, gives exactly the odour of the fulphur Well at Harrogate." From these experiments confidered together, it may, perhaps, be inferred, that common falt communicates a fulphureous fmell to water both by putrefaction and calcination. Hence some may think, that there is some probability in the supposition, that either a calcined stratum of common falt, or a putrescent falt spring, may contribute to the production of the sulphureous smell of Harrogate water; especially as these waters are largely impregnated with common falt. However, as neither the falt in fea water, nor that of calcined fea-wrack, nor calcined bay falt, are any of them absolutely free from the admixture of bodies containing the vitriolic acid, a doubt still remains, whether the fulphureous exhalation, 'here spoken of, can be generated' from Substances in which the vitriblic acid does not exist.

The shale from which alum is made, when it is first dug out of the earth, gives no impregnation to water; but by exposure to air and moilture its principles are loofened, it shivers into pieces, and finally moulders into a kind of clay, which has an aluminous taffe. Alum is an earthy falt refulting from an union of the acid of fulphur with pure clay; and hence we are fure, that shale, when decomposed by the air, contains the acid of fulphur; and from its oily black appearance, and efpecially from its being inflammable, we are equally certain that it contains phlogiston, the other constituent part of sulphur. And indeed pyritous fubstances, or combinations of fulphur and iron, enter into the composition of many, probably of all forts of shale, though the particles of the pyrites may not be large enough to be seen in some of them; and if this be admitted, then we need be at no loss to account for the bits of fulphur, which are sublimed to the top of the heaps of shale, when they calcine large quantities of it for the purpose of making alum: nor need we have any difficulty in admitting, that a phlogistic vapour must be discharged from shale, when it is decomposed by the air. Dr. Short fays, that he burned a piece of aluminous shale for half an hour in an open fire; he then powdered and infused it in common water, and the water fent forth a most intolerable sulphureous smell, the very fame with Harrogate water. He burned feveral other pieces of shale, but none of them stunk so strong as the first. This difference may be attributed, either to the different qualities of the different pieces of shale which he tried, or to the calcination of the first being pushed to a certain definite degree; for the combination of the principles on which the finell depends may be produced by one degree of heat, and destroyed by another. I have mentioned, briefly,

briefly, these properties of shale, because there is a stratum of shale extended over all the country in the neighbourhood of Harrogate; feveral beds of it may be feen in the stone quarry above the fulphur wells; many of the brooks about Harrogate run upon shale, and the sulphur wells spring out of it. They have bored to the depth of twenty yards into this shale, in different places, in fearch of coal, but have never penetrated through it. Its hardness is not the same at all depths. of it will strike fire, as a pyrites does, with steel; and other beds of it are foft, as if in a state of decomposition, and the fulphur water is thought to rife out of that shale which is in the foftest state. But whatever impregnation shale when calcined, or otherwise decomposed to a particular degree, may give to the water which passes over it, it must not be concluded, that shale in general gives water a sulphureous impregnation; fince there are many fprings, in various parts of England, arifing out of shale, in which no such impregnation is observed.

I forgot to mention, in its proper place, that having vifited the bog, so often spoken of, after a long series of very dry weather, I found its furface, where there was no grass, quite candied over with a yellowish crust, of tolerable consistency, which had a strong aluminous taste, and the smell of honey. BERGMAN speaks of a turf found at Helsingberg in Scania, confifting of the roots of vegetables, which was often covered with a pyritous cuticle, which, when elixated, yielded alum; and I make no doubt, that the Harrogate morals is of the same kind.

Whether nature uses any of the methods which I have mentioned of producing the air by which fulphureous waters are impregnated, may be much questioned; it is of use, however, to record the experiments by which her productions may be imitated; for though the line of human understanding will never fathom the depths of divine wisdom, displayed in the formation of this little globe which we inhabit; yet the impulse of attempting an investigation of the works of God is irresistible; and every physical truth which we discover, every little approach which we make towards a comprehension of the mode of his operation, gives to a mind of any piety the most pure and sublime satisfaction.



IX. Observations and Remarks on those Stars which the Astronomers of the last Century suspected to be changeable. By Edward Pigott, Esq.; communicated by Sir Henry C. Englesield, Bart. F. R. S. and A. S.

### Read February 9, 1786.

IT is about a century fince Hevelius, Montanari, Flam-STEED, MARALDI, and CASSINI, noticed a cortain number of stars which they supposed had either disappeared, changed in brightness, or were new ones; and yet to this day we have acquired no further knowledge of them. This may be attributed to the difficulty of finding out what star is meant, and the not having exact observations of their relative brightness. I therefore have drawn up the following catalogue, and made the necessary observations; so that in future we can examine them without much trouble, and be certain of any change that may take place. To accomplish this, it was requisite to compare with attention many authors and most of the catalogues of stars; in doing which I have perceived several undoubted errors, and others highly probable; but as entering into a discussion of such disagreements would swell this account confiderably, and make it very intricate, I shall avoid, as much as possible, any thing of the kind that is not immediately necessary.

In order to separate certainty from doubt, I have classed these stars in two divisions; the first are undoubtedly changeable;

the others remain yet to be better authenticated: Though some of them bear all the appearance of being variable, still no certainty of their being so has come to my knowledge. To those of the first class are subjoined observations made on them within these last four years, from which the period and progreffive changes of some are deduced, though never settled before, and if already known are more exactly determined by comparing my observations with former ones. Also, as the position of several are determined only by ancient astronomers, and therefore inaccurately, I have observed them with great exactness, the declinations being taken with a BIRD's eighteeninch quadrant, and the right afcentions with a three-feet transit instrument: these last may serve in future to discover their proper motions in right ascension, for which reason I shall fpecify the stars to which they were compared. The stars of the fecond class have either their relative brightness exactly fettled, or their non-existence ascertained. I have also pointed out the probability of a mistake in several, and in general given an account of the appearance they have had within these few years.

Catalogue of variable Stars, reduced to the beginning of 1786.

#### Class the first.

Names.	R. A		Dec	lina	tion.	and			From whence reduced.	
Nova 1572, in Caffilopea, Octi Algol MAYER'S 420th in Leo In Hydra Nova 1604 in Serpentarius Pentarius Se Lyræ Near the Swan's head Antinoi In the Swan's neck' In the Swan's breaft Cephei	00 13 2 8 2 54 9 36 13 18 17 18 18 42 19 38 19 41	33 19 5 4+ 90-	3 40 12 22 21 33 26 00 32	57 6 25 9 10 7 48 28 22 22	25 S 55 N S 38 S 46 N N N N N N N N N N N N N N N N N N N	2 2 6 4 I 3 3 5 3 5 3	- - - 4-	400040500	RICCIOLUS'S Almagestum, &c. BRADLEY. MAYER. MAYER. From my observat. Phil. Tr. N° 346. BRADLEY. Phil. Tr. N° 65. LA CAILLE. From my observat. Flamsteed.	

#### Class the second.

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46 or & Andromedæ			46	44	24	00 N	4.	5-5	5.6	FLAMSTEED.
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MEVELIUS'S 41 Androm.	I	28	40		31	₹N	5	-		Hevelius.
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55 or Neb. Andromedæ	I		30	39	40	3 N	6		•	FLAMSTEED.
Prol. and UL. BEIGH Eridani	2,	42	•	9	40	. s	4		0	Ul. Beigu.
41 Tauri	3	52	27	27	00	39 N	5			FLAMSTEED.
47 Eridani			54	8	41	40 S	4			FLAMSTELD.
Near 53d Eridani .			00	12	30	± S	4	_		By estimation.
, Canis Majoris.	6	54	15	15	19	36 S	3		Q	LA CAILLE.
8 Geminorum	7	32	11+	28	31	38 N	I	-	3	MASKELYNE.
¿ Leonis			24	12	14	23 N	4	-		MAYER.
4 Leonis		32		14	59	36 N	5 -	6 —	0	Mayer.
25th Leonis	9	46	8	12	20	36 N	6.	7	0	FLAMSTEED.
BAYER S ! Leonis .		52	<u>I</u>	15	30	. N	6			Тусно.
1 Urfæ Majoris	12	4	45	58	13	. N 24 N	2		4	LA CAILLE.
2										Clais

Class the second continued.

Names.	R. A. in Time.	Declination	Greatest and least magnitudes.	From whence 15-
n Vitginis  BAYER'S * nearging In N. thigh of Vitgo 91 Virginis  Draconis  In west scales of Libra  Ptol. and Ul. Belgh's 6th unformed in Libra  **Libræ*  Tycho's 11th Libræ 33 Selpentis  Near * Ulsæ Minoris  Ptol. 14 Ophiuchi  Ptol. 13 Ophiuchi  Ptol. 18 Ophiuchi  **Serpentis  Tycho's 27th Capricor  Tycho's 27th Capricor  Tycho's 22d Androm.  Tycho's 19 Aquarii  **Andromedæ*  LA CALLE' 483  Zodi. Cat.	12 53 00 13 29 + 13 43 43 13 58 30 14 53 ½ 15 29 + 15 29 39 15 37 ½ 15 38 00 16 ¼ 17 2 14 17 18 + 17 18 + 17 22 00 18 45 35 21 41 2 22 25 2 52 6	24 10	6	MAYER. From maps. From maps. Flamsteld. BRADLFY. [Mém.de l'Acad.] des Sciences.  UL. BEIGH.  LA CAILLE. TYCHO. FLAMSTEED. From maps. BRADLEY. PTOL. MAYER. LA CAILLE. TYCHO. TYCHO. TYCHO. TYCHO. LA CAILLE.

I shall now proceed to give a short account of these stars, and begin with those of the first class.

# The famous Nova of 1572 in Cassiopea.

Several astronomers are of opinion, that it has a periodical return, which Keill and others have conjectured to happen every 150 years. This is also my opinion; and I cannot think its not being noticed at the completion of every term a material.

rial

rial objection, fince perhaps, as with most of the variables, it may at different periods have different degrees of lustre, so as sometimes to increase only to the ninth magnitude; and if this be the case, its period is probably much shorter. This induced me, in September 1782, to take a plan of the smallest stars near its place, and which I have examined often since, but found no alteration.

#### o Ceti.

Since the end of 1782 I have observed very exactly the decrease of brightness of this star; but never have seen it of above the 6th magnitude. Oct. 29, 1782, it was of the 7th magnitude, and gradually decreased till Dec. 30, it being then of the 8.9th magnitude.

1783, Feb. 16, certainly less than the 9th magnitude.

1783, August 25, of the 6th magnitude, and gradually decreased until Dec. 14, being then of the 10th magnitude, and equal to the little star close to it.

1784, Jan. 11, I thought it by intervals still less than the same little star.

1784, Sept. 12, it was of the 7.8th magnitude, and gradually decreased until Dec. 9, and then was of the 9th magnitude, and rather brighter than the little star.

As a matter of curiofity, I have deduced its period from the times when it was equal to a certain flar in the course of its decrease; the results were 320-337 and 328 days; but M. Cassini determined its mean period with greater exactness to be 334 days. Mr. Goodricke saw it Aug. 9, 1782, of the 2d magnitude, rather brighter than  $\alpha$  and less than  $\beta$  Ceti. Sept. 5, it was of the 3d magnitude, being equal to  $\gamma$  Ceti.

#### Algol.

The period of Algol, discovered by Mr. Goodricke, gave us some new light into the nature of the fixed stars. Though the phænomena seem to attract the attention of most astronomers, still there are some points which require suther investigation. Its degree of brightness, when at its minimum, is different in different periods; and also, I think, when at its full, it is sometimes brighter than a Persei, and at other times less. Whether these differences return regularly after a certain number of periods remains yet to be examined. My last observations, when it was at the middle of its minimum, are,

1785, July 8, at 11 50 undoubtedly less than e Persei.

July 31, at 9 50 equal to e Persei.

Sept. 12, at 10 45

a remarkable observation; rather less than e Persei; evidently brighter than e; nearly of the 3d mag.

MAYER'S Nº 420, lately discovered to be variable by M. Koch.

A few years before 1782, M. Koch faw the N° 420 undoubtedly less than the N° 419 of MAYER's Catalogue.

In February 1782, he found them both exactly of the same brightness, therefore of the 7th magnitude.

From an extract of a letter I have lately seen, the variable was of the 9th magnitude in April, 1783, and of the 10th in April, 1784.

I have often feen the N° 419, but never the variable, though I have frequently looked for it with a night-glass, and on the 4th of April, 1785, in a 3-feet achromatic transit instrument.

#### Variable in Hydra.

MARALDI, in 1704, having found that this star had a periodical variation, continued to examine it for several years, and concluded its period to be about two years, though with considerable variations; in which he was much mistaken, as will appear from the following results, which shew that its period in all probability is tolerably regular, and only of 494 days.

Dates when it was at the middle of its greatest brightness, estimated from MARALDI's observations.

1704, March 14, he faw it nearly of the same magnitude from the beginning of March until the beginning of April; it then decreased.

1705, . . . he saw it very faint in November, 1705, and found it decreasing: this observation is too imperfect.

1708, May 22, accurately determined; its increase and decrease being well observed.

1709, Nov. 10, :: doubtful, its decrease only being observed.

1712, May 1, :: ditto, ditto, ditto.

1784, Jan. 26, by me, very accurately, its increase and decrease being observed. See the Observations that conclude this paper.

1785, May 27, ditto, ditto, ditto.

The four greatest intervals of MARALDI's Observations give for single periods in days thus 495—517—480 and 510, the mean being 500½, which is tolerably exact considering how

Cc 2 doubtful

doubtful the observations of 1709 and 1712 are. My two make it 487 days; but at the interval is only a single period, it may err 10 days; I therefore shall take a mean between the results, which is 474, and proceed on to the following comparisons of Maraldi's two best observations with mine.

1708, May 22, interval of 56 periods, each of 493\frac{2}{3} days.
1784, Jan. 26, interval of 57 periods, each of 493\frac{1}{2} days.
1785, May 27, interval of 57 periods, each of 493\frac{1}{2} days.
1704, Mar. 14, interval of 59 periods, each of 494\frac{1}{2} days.
1704, Mar. 14, interval of 60 periods, each of 494\frac{1}{2} days.
1785, May 27, interval of 60 periods, each of 494\frac{1}{2} days.

A fingle period, on a mean, 494 days.

If MARALDI's observations of 1704 and 1708 are exact to a month, and there is no reason to believe otherwise, the period at that time seems to have been a few days longer than it is at present, and therefore the one here deduced may be esteemed as the mean period.

## Particulars of the changes it undergoes.

- when at its full brightness it is of the 4th magnitude, and has no perceptible change for about a fortnight.
- 2. It is about fix months in increasing from the 10th magnitude, and returning to the same.
- 3. Therefore it may be confidered as invisible also during six months.
- 4. It is confiderably quicker in increasing than in decreasing, perhaps by half.

Though

Though when at its full it may always be stilled of the 4th magnitude, it does not constantly attain exactly the same degree of brightness, but the differences are very small, as shewn below.

1704, brighter than 
$$\psi$$
.

1784,  $\begin{cases} \text{much brighter than } \psi, \text{ being nearly} \end{cases}$ 

1708, brighter than  $\psi$ .

1785, rather brighter than  $\psi$ .

Its mean right ascension, computed from my observations, and reduced to Jan. 1, 1784, is

199 29 30 { from 4 observations, compared to \$ mg, made between March and May 1784...

199 29 21 from 2 ditto, compared to MAYER's 538, made in May, 1784.
199 29 20 from 5 ditto, compared to 7 Hydræ, made between March and May, 1784.

199 29 24 - mean right ascension for Jan. 1, 1784, on a mean.

HEVELIUS'S 30th Hydræ is the above star; he marks it of: the 6th magnitude; I find it in no other Catalogue.

## The famous Nova of 1604, in Serpentarius.

A full account of this star is given by KEPLER, and it seems to have had a similar appearance to the Nova in Cassiopea; therefore the reslections delivered there need not be again repeated. In July, 1782, I took a plan of the smallest stars near its place, which was examined every year since, but not alteration was perceived.

#### β Lyræ.

Mr. Goodricke discovered the variation and period of thisstar; and hopes soon to settle its different phases with more exactness: exactness; I shall therefore not enter into any detail, being certain it cannot be in better hands. In his last account he mentions having first suspected the period to be only of six days nine hours; such has always been my opinion, and which material point will probably be more satisfactorily determined in his next publication.

### Nova near the Swan's Head of 1670.

This star was first seen in December 1669 by Don AN-THELME; it soon became of the 3d magnitude, and disappeared in 1672, after having undergone several variations. I have constantly looked for it since November, 1781, without success; had it increased to only the 10th or 11th magnitude, I should have perceived it, having taken an exact plan of all the surrounding stars.

#### n Antinoi.

The variation and period of this star I discovered last year, and had the honour of communicating an account of it to the Society: as at present a long interval is elapsed since my first observations, and that lately I have noted some of its phases with exactness, I shall compare them to those observed in 1784, which of course will give results more satisfactory. The period, as settled in my former paper, is 7 d. 4 h. 38'; but for reasons there alledged, it must be much less precise than the following.

1785, July 18, at 9 h. Sept. 6, at 18
Sept. 27, at 22

times when 7 Antinoi was between its least and greatest brightness.

Thefe

These being compared to similar observations of Sept. 12 and 19, 1784, make the length of a single period thus:

I see no reason to alter materially the other points; but believe them more exact thus:

40 hours at its greatest brightness.

66 — in decreasing.

at its least.

36 — in increasing.

It also, in every period, seems to attain the same degree of brightness when at its full, and to be equally decreased.

#### Variable in the Swan's Neck.

During these three years I have observed this star with particular attention, as may be seen by the observations that conclude this Paper, and determined the middle time of its greatestr brightness very exactly, thus:

The second of these, being compared to that of Nov. 20, 1687, made by Kirch, gives 406 days exactly for one period, the interval between them being 35322 days, and divided by 87 periods. I make the divisor 87, in order to get a result nearest to that settled by Maraldi and Cassini of 405, and by M. Le Gentil of 405,3 days. We cannot suppose that these great astronomers have made any mistake; and on the other hand, it seems hardly possible, that the mean of my observations alone, which makes the period 392 days, can err 14; but perhaps its period is irregular; to determine which several intervals of 15 years ought to be taken, and I am much inclined to believe, that it will be found of only 396 days 21 hours.

## Particulars of the changes it undergoes.

- 1. When at its full brightness it has no perceptible change for about a fortnight.
- 2. It is about 3½ months in increasing from the 11th magnitude to its full brightness, and the same in decreasing.
- 3. Therefore it may be confidered as invisible during fix months.
- 4. It does not attain the same degrees of brightness at every period, being sometimes of the 5th, and other times of the 7th magnitude.

Its mean right ascension, computed from my observations, and reduced to Aug. 1, 1783, is

- 295 33 46 from 2 observ. compared to v Cygni, made in July and August, 1783.
- 295 33 45 from 2 ditto, compared to 7 Lyræ, ditto.
- 295 33 45 from 1 ditto, compared to a Lyrae, made in August, 1783.
- 295 33 55 from 3 ditto, compared to & Lyræ, made in July and August, 1783.
- 295 33 52 from 2 ditto, compared to & Cygni, made in August 1783.
- 295 33  $48\frac{\pi}{2}$  mean right ascension for August 1, 1783, on a mean.

#### Variable in the Swan's Breaft.

This star was first seen by G. Jansonius in 1600, and afterwards frequently observed by different astronomers, but with intervals of ten or more years, which is probably the reason why no regularity in its changes has yet been deduced. I have examined minutely the observations made in the last century, and shall venture to give the following results.

- 1. Continues at its full brightness for about five years.
- 2. Decreases rapidly during two years.
- 3. Invisible to the naked eye for four years.
- 4. Increases slowly during seven years.
- 5. All these changes, or its period, are completed in 18 years.
  - 6. It was at its minimum at the end of the year 1663.

It does not always increase to the same degree of brightness, being sometimes of the 3d, and at other times only of the 6th magnitude. I am intirely ignorant whether it is subject to the same changes since this century, having not met with any series of observations on it; but if the above conjectures are exact, it will be at its minimum in a very sew years. Since November, 1781, I have constantly seen it of the 6th magnitude, being rather less than N° 28, 29, and m, and rather brighter than

36 and 40 Cygni. Sometimes I suspect it has rather decreased within these two last years, though in a very small degree.

Its mean right ascension, computed from my observations, and reduced to Sept. 1, 1782, is

302 26 43 from 3 observations, compared to γ Cygni, made in October, 1781.

302 26 46 from 3 ditto, compared to 2 Cygni, made in August, 1782.

302 26 52 from 1 ditto, compared to & Aquilæ, made ditto.

302 26 46 from 1 ditto, compared to a Cygni, made ditto.

302 26 39 from I ditto, compared to & Andromedæ, made in October 1781.

302 26 45 mean right ascension for Sept. 1, 1782, on a mean.

FLAMSTEED has this star in his Catalogue; but, I believe, observed it only once.

### 8 Cephei.

This is the last variable star discovered, and again by Mr. GOODRICKE. Its changes are very difficult to be seen, unless examined when at its minimum and full brightness. I have lately made some good observations on it thus:

1785, Aug. 30, at 14 h. less than & Cephei.

31, at 9 h. equal if not brighter than ζ Cephei.

Sept. 15, at 12½ h. less than & Cephei.

16, at 8 h. between ε and ζ Cephei.

- at 11 h. increased, but not as bright as ζ.

17, at 11 h. rather brighter than ζ.

26, at 11½ h. equal or less than s.

27, at 8 h. evidently brighter than ζ.

Therefore it was between its least and greatest brightness August 31, at noon, and Sept. 26, at 21 h.: these being compared to my first observations, when also between its least and greatest brightness on Nov. 20, at 3 h. and Nov. 30, at 15 h.

1784,

1784, give the following refults, the mean of which corroborates that deduced by Mr. Goodricke of 5 d. 8 h. 37'1.

D.	H.	M.
5	8	35
5	8	4 I
5	8	33
5	8	<b>3</b> 9

Length of a fingle period 5 8 37 on a mean.

& Cephei concludes the stars of the first class; those that follow are of the second.

## Hevelius's 6th Cassiopeæ.

In 1782 I first perceived that this star was missing; nor could I find it in 1783 and 1784.

### 46th or & Andromedæ.

This star is said to have diminished in brightness. In 1784 and 1785 I found it, by very exact observations, less than u, equal to  $\omega^*$ , and brighter than d and  $\chi$ ; yet I must mention that it is marked in my journal as being sometimes brighter, and at other times less than  $\omega^*$ ; but still I am not convinced, that it varies in brightness. FLAMSTEED, in his Catalogue, annexes no character to his 46th Andromedæ; but in vol. II. of his Hist. Cœlest. p. 135. and 138. he marks it  $\xi$ .

<sup>\*</sup> I suspect an error in this character, but cannot be certain. H. E.

FLAMSTEED'S 50, 52, 7 Andromedæ, and Hevelius's 41 Andromedæ.

As the position and characters of these stars differ considerably in different Catalogues, and that some of them are mentioned by Cassini to have disappeared and re-appeared, I shall give their brightness as observed in 1783, 1784, and 1785.

FLAMSTEED's 50th of the 4.5th magnitude, and equal, if not rather less than φ Andromedæ.

7 of the 5th magnitude, and equal to 4.6 and 48 Andromedæ.

HEVELIUS'S 41 of the 5.6th magnitude, and are of the fame brightness.

A star between FLAMSTEED'S 52 and Hevelius's 41 is of the 6th magnitude, or rather less. I could not see Tycho's 19th Andromedæ; but I take this star to be the same as Hevelius's 41 Andromedæ.

#### Tycho's 20th Ceti.

This must be the star which HEVELIUS said had disappeared, being Tycho's second in the Whale's belly. There can hardly be any doubt but that it is the  $\chi$ , misplaced by Tycho. This  $\chi$  is of the 4.5th magnitude, and of the same brightness as the three  $\psi$  Aquarii.

FLAMSTEED'S 55th Andromedæ, marked Neb. in his Catalogue.

It is mentioned in the latest Catalogues of Nebulæ that this nebula could not be found. FLAMSTEED, who, I believe, only.

only observed it once, viz. Oct. 17, 1691, does not mark it nebulous; nor does it appear to me such, but as a star of the 6th magnitude. There are a few small stars near it, which to the naked eye, when the air is very clear, make it appear nebulous, which probably is the reason why Flamsteed marked it thus in his Catalogue.

### σ or PTOL. and UL. BEIGH's 17th Eridani.

FLAMSTEED fays, he could not see this star in 1691 and 1692. In 1782, 1783, and 1784, I observed one of the 7th magnitude in that place; the relative brightness of which appeared always the same, viz. less than two little stars near and below magnitude.

### FLAMSTEED'S 41 Tauri.

This star was thought by Cassini to be a new one or variable. I see little or no reason to be of that opinion; that it is not new is evident, since it is UL. Beigh's 26th and Tycho's 43d. In 1784 and 1785 I found it of the 5th magnitude, being equal to  $\varphi$ , and brighter than  $\psi$ , P, and  $\chi$  Tauri.

Star about 2° 4 North of 53d Eridani, and 47 Eridani.

The first of these stars Cassini thought a new one, and that it was not visible in 1664. In 1784 I found it was less than  $\omega$ , and d, brighter than A, and seemed equal to  $\psi$  Eridani.

CASSINI mentions another star thereabouts, which he also esteemed a new one: this is probably FLAMSTEED'S 47th. In. 1.784 it appeared rather less than 46th.

# 2 Canis Majoris.

MARALDI could not see this star in 1670; but in 1692 and 1693 it appeared of the fourth magnitude. I have very frequently noticed it since 1782, but perceived not the least variation, being constantly of the 4th magnitude, very little brighter than  $\theta$ , and decidedly brighter than  $\epsilon$ .

### α β Geminorum.

If either of these stars have changed in brightness, it is probably the  $\beta$ . In 1783, 1784, 1785, the  $\beta$  was undoubtedly brighter than  $\alpha$ .

## & Leonis.

Montanari fays, this star was hardly visible in 1693. I found it constantly in 1783, 1784, and 1785, of the same brightness, being of the 5th magnitude; less than A,  $\pi$ , and, if any difference, rather brighter than b and w Leonis. Tycho, Flamsteed, Mayer, Bradley, &c. mark it of the 4th magnitude.

### ψ Leonis.

This star is said to have disappeared before the year 1667. It is now, and has ever been since 1783, of the 5.6th magnitude, being less than  $\omega$ , and brighter than i, FLAMSTEED'S 46th.

## 25th Leonis.

In 1783 I first perceived this star was missing; nor was it visible in 1784 and 1785, even with the transit-instrument.

BAYER's i Leonis, or Tycho's 16 Leonis.

It was not visible in 1709, nor could I see it in 1785. This is a different star from the i Leonis of the other Catalogues, though Tycho's description of its place is the same.

### d Ursæ Majoris.

This star is suspected to change in brightness (see Long's Astronomy), on account of its being marked by Tycho, Prince of Hesse, &c. of the 2d magnitude; while Hevelius, Bradley, and others, have it of the 3d. At present, and for these three years past, it appears as a bright 4th magnitude, being rather less than 1, equal to a, and rather brighter than 2 Draconis.

### n Virginis.

This star is supposed to be variable, because Flamsteed, on the 27th of January, 1680, says he could not see it. He observed it May 12, 1677, and some years afterwards, since it is in his Catalogue. I examined it frequently in 1784 and 1785, without perceiving the least change, being of the 6th magnitude, less than c, and rather brighter than a star three degrees lower in a right line with c and n Virginis.

BAYER's star of 6th magnitude, 1° South of g Virginis.

This star is not in any of the nine Catalogues that I have. MARALDI looked for it in vain; and in May, 1785, I could not see the least appearance of it. It certainly was not of the 8th magnitude.

## In the northern thigh of Virgo.

This star, which is marked by RICCIOLUS of the 6th magnitude, could not be seen by MARALDI in 1709; nor was it of the 9th magnitude, if at all visible, in 1785.

## 91 or 92 Virginis.

In 1785 I found that one of these stars was missing, and which seems to be the 91: the remaining one is of the 6.7th magnitude.

#### a Draconis.

I am of Mr. HERSCHEL'S opinion, that it is highly probable this star is variable. BRADLEY, FLAMSTEED, &c. mark it of the 2d magnitude; at present it is only of a bright 4th. I have frequently examined it since October, 1782, without perceiving the least change, being constantly rather less than Draconis, equal to & Ursæ Majoris, and rather brighter than E Draconis.

### BAYER's star in the west scales of Libra.

MARALDI fays he could not fee this star; nor could I in 1784 and 1785. With a night-glass may be seen thereabouts fome

some small stars of about the 8th magnitude, none of which are near as bright as the 2d v Libræ.

PTOL. and UL. BEIGH'S Nº 6 of the unformed in Libra.

In examining different Catalogues I do not find this star in any other than the above, though it is marked of the 4th magnitude. If PTOLEMY had not the z it might be thought to be that. In 1785 I frequently observed a star of the 7th magnitude very near its place, which appeared rather less than FLAMSTEED'S 41. FLAMSTEED has not this little star in his Catalogue; but he observed it May 9, 1681.

#### z Libræ.

This star is thought to be variable. I am not of that opinion; though certainly it is rather singular that Hevelius, whose attention was directed to this part of the heavens, to find Tycho's 11th, did not observe the  $\kappa$ ; and the more so, as he has noticed two much lesser stars not far from it. During these three years I have sound the  $\kappa$  constantly of the 5th magnitude, being less than  $\psi$  or  $\theta$ , equal to  $\lambda$ , and brighter than  $\eta$ .

#### Tycнo's 11th Libræ.

HEVELIUS says he could not find a star of the 4th magnitude in Libra noticed by Tycho. This must be Tycho's 11th, since he has all the others. It was not visible in 1783, 1784, and 1785, nor probably ever existed; for it is, I think, evident, that this 11th is no other than the 2, with an error of two degrees in longitude.

### 33 Serpentis.

In 1784 I perceived that this star was missing; nor was it visible in 1785 with a night-glass.

A flar marked by BAYER near & Urfæ Minoris.

Cassini could not fee this star. In 1782 I took, with a night-glass, a plan of all the stars near its place, and near the  $\epsilon$ , none of which were brighter than the 7.8th magnitude. I have since re-examined the plan, but sound no alteration.

The e or Ptol. and Ul. Beigh's 14th Ophiuchi or FLAMsteed's 36th.

I have no doubt but that this is the star which is said tohave disappeared before 1695. It is also evident, by what: Hevelius says in his Catalogue on the  $\theta$  and B, that the  $\varrho$ was not seen by him. In 1784 and 1785 I found it of the 4.5th magnitude, much brighter than 39, also rather brighter than 51 and 58, and less than 44. On the 30th of June, 1783, I have marked it in my journal equal to 39, and less than 51 and 58; but as the observation was not repeated, I am far from being certain it has undergone any change, particularly as this star has a southern declination of 26°, and therefore great attention must be given to the state of the atmosphere.

PTOL.

PTOL. 13th and 18th Ophiuchi, 4th magnitude.

If there is no error in the Catalogue, these two stars have disappeared; but I am confident that PTOLEMY's 13th is FLAM-STEED'S 40th, and that PTOLEMY'S 18th ought to be marked with a north latitude instead of fouth, which would make it agree nearly with FLAMSTEED'S 58th.

## σ Sagittarii.

Mr. Herschel, with great reason, has placed this star among those which probably have changed their magnitudes. I had long fince remarked the fingular difagreement in all the Catalogues, which induced me to observe it frequently, particularly in 1783, 1784, and 1785, when it appeared of the 2. 3d magnitude, and brighter than m Sagittarii.

## 8 Serpentis.

MONTANARI fays he faw this star of the 5th magnitude, and that the next year it grew bigger. I examined it frequently in 1783, 1784, and 1785, and found it always less than & Aquilæ, equal to \( \beta \) Aquilæ, and P Ophiuchi; 4th magnitude.

# Tycнo's 27th Capricorni.

This star was not visible in HEVELIUS's time; nor could I fee it 1778, 1782, 1784, with the transit-instrument.

Tycho's

### Tycho's 22d Andromedæ and o Andromedæ.

CASSINI remarked, that the star placed by Tycho at the end of the chain of Andromeda as of the 4th magnitude, was grown so small that it could scarcely be seen. This is Tycho's N° 22, the longitude and latitude of which places it near the two  $\pi$  Cygni, and where no star was visible in 1784 and 1785.

As possibly, by Tycho's description, Cassini took the 22d for the o Andromedæ, I have also examined this star, and in 1783, 1784, and 1785, found its relative brightness thus: less than α Cephei; equal to ζ Cassiopeæ, though, if any difference, rather brighter; and brighter than λ, κ, or Andromedæ.

## Tycho's 19th Aquarii.

This is the star that Hevelius says was missing, and that Flamsteed could not see with his naked eye Nov. 18, 1679; nor could I see the least appearance of it in 1782. I am convinced it is the same star as Flamsteed's 56th, marked f by Bayer, from which it is only 1°½. Flamsteed's 53d, marked f in Ptolemy's Catalogue, is a different star.

## LA CAILLE'S 483 Aquarii.

I first discovered that this star was missing in 1778. It was not visible in 1783, 1784.

There are a few other stars suspected by the ancient astronomers to have been new or altered a little in brightness, which I have omitted, not seeing any reason to think them so; and some that are certainly variable, but cannot be observed in these latitudes. I have also, contrary to my first intention, added several which are not mentioned by them; such are those that I lately discovered to be missing.

Perhaps many perfons would place in the first class several stars which I have put in the second, relying on the positive affertions we have of their having disappeared, diminished, or being new; for my part, I am confident that most of these fupposed changes may be attributed to mistakes; and in general for those that are said to be lost, an attentive comparison of different Maps and Catalogues will point out the error; and thus I have ventured to give my opinion of Tycho's 20th Ceti, 11th Libræ, and 19th Aquarii, &c. Since FLAM-STEED'S Catalogue has been more particularly investigated, the number of these supposed lost stars is considerably increased; but if the second volume of his Hist. Coelest. is also examined. many errors will be detected; among which it will appear very unaccountable, that the 71st, 80th, and 81st of Hercules, which were discovered to be missing by Mr. HERSCHEL, are not in FLAMSTEED's observations under the name of Hercules, though I looked for them with particular attention, and find the 70th. The 19th Persei, which Mr. HERSCHEL also could not see, was observed but once by Flamsteed, viz. Jan. 16, 1693, and in all probability is the r with the time of its transit erroneously set down. The T was observed on Jan. 17, 1693, and Jan. 18, 1694. Besides these Mr. Goodricke has found several other errors still more evident. I scarcely need add, that these corrections do not in the least intimate any mistake or diminish the merit of those that first point them out, but fall entirely on the ancient catalogues and observations.

Mr. HERSCHEL, in felecting several stars which possibly may be reckoned new ones, very judiciously gives us plausible reasons

not to lay great stress on their being so; and the following remark only confirms what he there suggests; for that star of the 5th magnitude following  $\tau$  Persei, mentioned by him, and which with great reason might be esteemed a new one, is in all probability the same as one observed by FLAMSTEED, Jan. 18, 1694, though not inserted in his Catalogue.

With regard to those stars which are said to have diminished or increased, as those in Andromeda, Leo, &c. they are, in my opinion, far from being confirmed as variable. I know, from repeated experience, that even more than a single observation, if not particularised and compared with neighbouring stars, is very little to be depended on; different states of the weather, thin streaks of clouds, have several times made me err a whole magnitude in the brightness of a star.

Whether these apparent changes in the stars proceed intirely from themselves; or whether they are effected by any foreign power that may in part occasion some of their particular appearances and irregularities, we have not sufficient data to determine: but whatever are the causes, a division of the different phænomena seems to be the most probable means of forwarding any conjecture that hereafter may be formed; I shall therefore divide the first class into three orders.

The first contains those that are periodical with long intervals; and such I reckon o Ceti, that in Hydra, that in the Swan's breast and neck, and also MAYER'S N° 420.

For the second order I shall mention only three, though others might be added; but the accounts of them are so unsatisfactorily recorded, and their places so little known, that I prefer selecting only that in Cassiopea of 1572, that in Serpentarius of 1604, and that near the Swan's head. The phænomena of these certainly bear a great resemblance to the first:

first: still their sudden appearance, and no certainty of a period, or at least infinitely longer, are, I think, sufficient reasons to separate them.

Lastly, Algol,  $\eta$  Antinoi,  $\beta$  Lyræ, and  $\delta$  Cephei, are so similar to each other, and so different from the above, that there can be but little or no hesitation in distinguishing them; also the cause of their changes seem in general to be attributed to spots, and a rotation on their axis. This property of the fixed stars, though often suspected, was far from being evident till within these two years; and we are not only indebted to Mr. Goodricke for the discovery of the first, but also for three of the only sour known.

Further may be added, that all those of the first order (MAVER'S 420 being yet so little known remains doubtful) attain in different periods different degrees of brightness when at their full; also the progressive increase of brightness of that in Hydra, that in the Swan's breast, of o Ceti,  $\beta$  Lyræ,  $\eta$  Antinoi, and  $\delta$  Cephei, is not similar to their decrease. This peculiarity with regard to Algol is yet uncertain, owing to the rapidness of its changes, so that there is only one that seems to have these points uniform, viz the variable in the Swan's neck.

I shall now conclude with the observations from which some results, given in this Paper, have been deduced; they are here collected together, in order to avoid confusion.

## Observations on the variable in Hydra.

```
1783, Dec. 11. A.M. much less than 4, and rather less than k.
               24. A.M. equal, if not less than, $\psi$; of the same colour as $\psi$.
               4. A.M. \begin{cases} \text{brighter than } \psi; \text{ of about } \frac{1}{4} \text{ of the difference between} \\ \psi \text{ and } \gamma; \text{ of a more copper colour than } \psi. \end{cases}
               9. A.M. if any difference brighter.
                25. A.M. {with the naked eye, it appeared in brightness nearly between $\psi$ and $\gamma$; and of a more copper colour than either $\psi$ or $\gamma$.
                  Feb. 1. 7 of the same brightness, but seemed of a more copper
                          2. colour.
                        23. between 4 and k; air not clear.
                               between \psi and k, but nearer the brightness of \psi.
               March 10.
                 April 11.
                         rather brighter than k.
                          Q. rather less than k, and brighter than x.
 1784, Dec. 1. A.M. did not fee the variable; firong moon-light,
                                     ditto
                                                                      ditto.
                   Q. A.M.
                 22. A.M.
                                      ditto
                                                                      ditto.
                                                                      ditto.
  1785, Mar. 4. or II:
                                      ditto
                  April 17. faw the x, but not the variable.
                   May 4. { visible to the naked eye; less than ψ, and much brighter than k; of a more copper colour than ψ.
                         7. } rather less than \psi.
```

2785, May 14. equal to \$; air not very clear, and moon-light.

15. equal to \$; air clear; moon-light.

19. undoubtedly brighter than 4; little hazy; moon near.

22.  $\left.\begin{array}{c} 22. \\ 27. \end{array}\right\}$  rather brighter than  $\psi$ ; moon-light strong.

fune 10. rather brighter than 4, though I think decreased.

12. equal to 4: but am not fure if the sky was quite clear.

13. rather less bright than 4; air clear.

Mr. GOODRICKE also frequently observed the variable, and his observations agree with the above.

### Observations on n Antinoi.

h. 1785, May 20. at 121 equal or less than . Antinoi. 21. - 12½ equal to,, evidently less than β; moon-light. 22. —  $12\frac{1}{4}$  equal if not brighter than  $\beta$  Aquilæ; moon. - 12<sup>T</sup>/<sub>3</sub> thought it brighter than β; air clear. June 10. - 121 rather brighter than : Antinoi. 12. - 113 rather brighter than , less than β. 13. — 12 $\frac{1}{2}$  a little brighter than  $\beta$ , much less than  $\delta$ . July 15. - 12½ less than β, brighter than .. 17. - II less than i, brighter than μ. 18. — 11 between 1 and  $\beta$ , I think rather nearer  $\beta$ . 19.  $-\frac{10\frac{1}{2}}{11\frac{1}{4}}$  between  $\beta$  and  $\delta$ , rather nearer  $\beta$ ; air clear. 20. — 11 rather brighter than  $\beta$ , certainly equal. Aug. 30. - 91 rather brighter than &, at least equal to it. 31. - 9 much brighter than 8. Sept. 6. - 9 less than .; a single view of it, not very satisfactory. 7. — 9½ much brighter than β. 26. —  $9^{\frac{1}{4}}$  much less than  $\beta$  or  $\beta$ , brighter than  $\beta$ . 27. —  $\frac{8}{10^{\frac{7}{2}}}$  much less than  $\beta$ , less than  $\gamma$ , brighter than  $\mu$ . 28. - 93 rather brighter than β. - 11 increased a little in brightness. The

F f

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The brightness of the stars to which n Antinoi is compared are given in the Philosophical Transactions, vol. LXXV. part I.

# Observations on the variable in Cygnus's Neck.

c of 8.9— I have annexed the fame letters to the stars.	3 *	* * * * * * * * * * * * * * * * * * *	* ¢	* %	b of 9th — the same letters
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Dates.	Mag.	
1783 Mar. 28 June 9 11 23 30 July 15	7 7 6.7 6.7 6.7	if visible, not of the 8th magnitude. rather brighter than d or e. rather increased. less than x. rather increased. of the same brightness as on the 30th of June. a little brighter than d or e.
Aug. 7	7 7 7 7 8 7 8 7 8 8	rather brighter than d; decreased, equal to d. less than d, brighter than e. less than e. think brighter than a. equal to a. much less than a, equal to c, and brighter than b.
22 24 Oct. 14 24	9.10	equal to b.  less than b.  (feen with the greatest difficulty; less than any stars of the
	0 11	ditto.
May 9	9.10	rather less than h.

Dates.	Mag.	
1784 May 21 June 17 July 21 22 27 Aug. 1	8.9 8 6 6 6 5.6 6	rather brighter than b, but not fo bright as b. equal to a, brighter than b. equal to $\chi$ with the naked eye. if any difference the $\chi$ was the brightest. rather brighter than $\chi$ . undoubtedly brighter than $\chi$ . think it decreased, but still rather brighter than $\chi$ .
Sept. 2 12 19 20	6 · 7 6 · 7 7	much decreased, less than $\chi_s$ , but brighter than $d$ .  still brighter than $d$ .  if any difference brighter than $d$ .  rather less than $d$ .
Oct. 5	7.8	less than e, about equal to a.
16 Nov. 11 17	7.8	rather brighter than a. less than b, about equal to f. rather less than f.
1785 May 9 June 21 July 23 Aug. 13 15 27 28 30 Sept. 2 7 11 12 26	9.10 8 7 6.7 6 6	rather brighter than a.  [a little brighter than d and e, much lefs than x; am not fure I could fee it with the naked eye.  [not fo bright as x, much brighter than d; I could fee it with the naked eye, but the x more distinctly.  not quite fo bright as x; naked eye.  ditto  [very difficult to fee with the naked eye, decreased in brightness; air clear.  [though the air was remarkably clear, it was with the utmost
27	} 7	difficulty I could fometimes fee it with the naked eye.



X. An Account of a Subsidence of the Ground near Folkstone, on the Coust of Kent. In a Letter from the Rev. John Lyon, M. A. to Edward King, Esq. F. R. S. and A. S. Communicated by Mr. King in a Letter to Charles Blagden, M. D. Sec. R. S.; with Remarks.

Read February 16, 1786.

TO DR. BLAGDEN, Sec. R. S.

DEAR SIR,

Mansfield-Street, Dec. 22, 1785.

HAVING always thought the account given in the Philosophical Transactions, by Mr. Sackette\*, about the beginning of this century, concerning the motion of the Cliffs, and of the adjacent ground, near Folkstone in Kent, a very curious one, and deserving of much attention; both because of the many positive attestations there were of ancient men with regard to it (who were both mariners, and used to observation); and because of the singular consequences that would follow, from the ascertaining of such a fact, in a philosophical light; I have constantly, whenever I had any opportunity, made repeated enquiries concerning the matter, of such perfons as I thought likely to be able to afford me any satisfactory information.

<sup>\*</sup> See Phil. Trans. vol. XXIX. No 349. or Jones's Abridgment, vol. IV. part II. p. 248.

Amongst

Amongst the rest, I mentioned it last summer to my worthy and very curious friend Mr. Boys, of Sandwich; who seemed surprised at the narration, and had never before heard of any such phænomenon. However, in less than a fortnight after our conversation, I was agreeably surprised by receiving a letter (dated 24th Sept. 1785), in which he said, I am sorry your bealth will not permit you to make the tour you at first proposed; especially as something very curious has happened within these sew days at Folkstone. Part of the cliff, to the westward of the town, a little way from the church, has sunk, and continues sinking into the earth; raising the ground, about the sinking part, in a very extraordinary manner. This corresponds with what you said to me on the subject of Stutfall-Castle, &c.; and certainly deserves your attention. If I could, by going thither, give you any satisfaction, I shall be ready and happy to obey your commands.

Being, through illness, prevented from examining this curious phænomenon myself, I accepted this obliging offer of Mr. Boys, and requested his affistance: and although he also was prevented from going to the spot himself, yet he applied to a friend of his, the reverend Mr. Lyon, of Dover; who has made repeated visits to the place, to obtain all the information possible; and has, at last, sent to me a very accurate drawing, together with an explanatory letter; which I now, with great pleasure, venture to lay before the Royal Society.

I must, however, at the same time, beg leave to observe, that although Mr. Lyon differs from Mr. Sackette, in his conclusion, concerning the motion of the whole adjacent country, and controverts that sact; and has certainly given a more clear and satisfactory account of the present phænomenon, than Mr. Sackette did of that which he wished to record; yet they both agree in imputing a most remarkable effect (only in different

different ways) to the passage of the springs, and drains of water, through the stratum of loose marle, on which the whole country rests: an effect which must needs produce, at different periods of time, various alterations on the surface; and may most probably have ocasioned much greater changes in the face of the country than that made in the present instance.

Whether therefore Mr. SACKETTE was right or wrong, in his great and final conclusion, concerning the motion of the whole coast; what he records, on the testimony of so many aged persons (in which they persisted with great seriousness and on the fullest consideration), does surely still deserve at least to be born in mind, and to be attended to with much circumspection; especially on a coast, where perhaps fixed points may be attempted to be ascertained, at some time or other, in order to complete the most accurate and most curious philosophical mensurations.

And I must further venture to observe, in vindication of Mr. Sackette's account and conclusions, that although Tarlingham-house has indeed been rebuilt, since the time referred to by the old man who conversed with Mr. Lyon; and therefore that old man's remark might be occasioned merely by that circumstance; yet it had not been rebuilt in Mr. Sackette's time; and, therefore, no such circumstance could be the occasion of its coming recently in view, at that period when he wrote, in parts of the coast where it had not been possible to see it at some time before.

And as to the Mooring Rock, so particularly referred to by Mr. Sackette, being now utterly unknown; it ought to be remembered, that Mr. Sackette, in his description of it, says, that it lies surrounded with great numbers of other rocks, and was on this account chiefly a noted one, because at it vessels use to

be moored, while they are loading other rocks, which they take from hence, not only for our own pier-heads, but for those of Dover Pier; and a very great quantity of them were shipped in the time of OLIVER's usurpation. and carried to Dunkirk, for the service of that harbour. Considering, therefore, that the enormous pile of Ramsgate Pier has been built since that time, (which, though it be chiefly composed of Portland stone, had, I apprehend, soundations and interior parts of ruder materials) and that there have been other vast demands for stone, it is not at all unlikely, that this very Mooring Rock, mentioned by Mr. Sackette, has itself been carried away in like manner as the others were that used to surround it; and that this is the sole reason why it is now no longer known, and totally forgotten.

I am, Sir, with much efteem, &c.

### EDWARD KING.

P. S. There is a peculiarity in Mr. Lyon's sketch, Tab. V. (designed to illustrate the grounds of his objections to Mr. Sackette's conclusions) which demands some explanation. After having given a section of the cliff and shore, the lines (instead of being continued in the same plane, and in the direction of the same section) are drawn so, as to be conceived as extended on the surface of the country from the eye of the observer at E. Without attending to this circumstance, what he says is not very easily to be understood; and indeed I must still think, that Mr. Sackette does not deserve so much censure, although Mr. Lyon's be undoubtedly a most accurate account, and most clear solution of the present phænomenon.

#### TO EDWARD KING, ESQ.

SIR,

Dover, Nov. 24, 1785.

AS I have been requested by my friend Mr. Boys, of Sandwich, to examine into the cause of the sinking of some ground near the town of Folkstone, in this neighbourhood, and to send you the results of my inquiries; I have made it my business to attend particularly to the subject. I have been twice to view the place. I have endeavoured to procure the best information, and have compared my remarks with what the reverend Mr. Sackette formerly said upon the same subject to the Royal Society.

That you may have a clearer idea of the place where the ground is finking, I have annexed a drawing of it, taken from a small hill near the foot of the cliff.

AA (Tab. IV.) represents the length of the ground, 130 feet, which is funk 40 feet from the top of the cliff DD.

BB, is a fiffure, in the valley between the finking ground AA and the hill HH, and in which there are many smaller chasms.

C, the tower of Folkstone-Church, not far from the cliff DD.

E, part of the town of Folkstone, as seen between the cliff DD and the hill HH.

F, the high chalk cliffs at a distance, leading towards Dover.

G, a track of pasture land, between a high range of hills and the sea.

I, the beach, at the foot of the hill H.

KK, Rocks, faid to be raifed (and I believe they are) by the finking of the ground AA.

As I intend, in explaining the cause of the sinking of the ground AA to you, to advance an opinion of my own, and to controvert what the reverend Mr. SACKETTE formerly said upon the subject, it may be necessary to explain the nature of the soil, as far as it is open to view, in the neighbourhood of Folkstone.

The chalk cliffs FF, which begin at Dover, form opposite Folkstone town high hills, and leaving the shore, there is a a large track of arable and pasture land between them and the sea.

Part of this ground is shewn in the view at G, and is a kind of marle, which contains pyrites, fragments of the Cornu Ammonis, and many other fossil bodies.

Next to the marle is a loose fandy soil (see the cliff DD) intermixed with a very large, hard, and coarse kind of stone, in which are often found fossil oyster shells.

This fandy foil rests upon a marle, which at the cliss DD is in some places three or sour seet above the beach, and when wet is very slippery. A stratum of this marle extends for many miles on the coast, and where it is not sufficiently covered with sand to bear any weight, it is in many places a quag, and dangerous to pass over.

Through this track of land I have described, there are many drains of water, which may be supplied partly from the falling of the rains in wet seasons, and partly from the springs issuing from the hills; and there is reason to suppose, that in a loose soil these drains form channels in a course of time. At the place where the ground has sunk before, and is now sinking, there is a drain from the marle under the sand; and I am of opinion, that the course of the water is in the same direction

as the valley between the hill H and the finking of the ground AA.

That the finking of the ground is caused by the foundation being undermined (and I think by water) is evident from the appearance of the ground in the valley. The soil is full of fishers, and resembles an arch, which is sunk down, and has left the two abutments, the hill H and the cliff DD, standing.

As the hill H more than counter-balances the pressure of the sinking ground upon the stratum of wet marle, the consequence is, that the rocks KK, at some yards distance, being only thinly covered with sand, are forced upwards, and become visible, and the wet marle in many places is squeezed through the sand with them.

This appears to me to be the true reason of the sinking of the ground at one place, and the rising of the rocks at another.

That the reverend Mr. SACKETTE's account of the finking of the ground at Folkstone, to the Royal Society, is founded in error, I have not the least doubt, from the present appearance of some of the objects he describes. I am rather at a loss to follow him exactly, as the oldest man in the town of Folkstone (I am told) never heard of the Mooring-rock he mentions.

I think by his description the finking of the ground must have been in his time at the same place it is now, as Tarlingham-house is not to be seen on the other side of the town.

Admitting this to be the case, there will still be a difficulty respecting the relative situation of each place in explaining what he calls a sketch of the country. But, to explain my meaning more sully, let B (Tab. V.) represent the

foot

foot of the hill H in the view, which is upwards of 30 feet high.

CD, the valley between the hill B and the cliff.

DE, the cragged cliff, 60 yards high.

EF, a plain, above a mile long.

FG, a hill of steep ascent, Mr. SACKETTE says near half a mile; but this is much higher than it really is.

GH, the land from the top of the hill to the house near a mile.

I, Tarlingham-house, lying two miles and a half N.N.W. from the rock.

EGH, a line of fight (see Mr. SACKETTE's description of the country).

If Mr. Sackette, in the above description of his sketch of the country, had placed each object according to its real situation; and if the effects he has mentioned had been real ones, they would have been truly wonderful, and worthy the attention of the curious investigator of the hidden operations of nature; but I am apprehensive he had but very little better soundation for what he has said than the vague and inconsistent reports of a few ancient sishermen. Tarlingham-house is by Mr. Sackette's account situated full as far beyond the hill FG as the width of the plain EF; but how deep the hill has sunk to render the house visible over the top must depend upon the situation of it, viz. how much higher it was than the top of the hill.

If the hill has funk only ten feet, there must have been some external evidence of it, such as sissures round the base, and a very steep ascent from the top of it, where the separation happened between it and Tarlingham-house; but there are no traces of any such sinking of the hills.

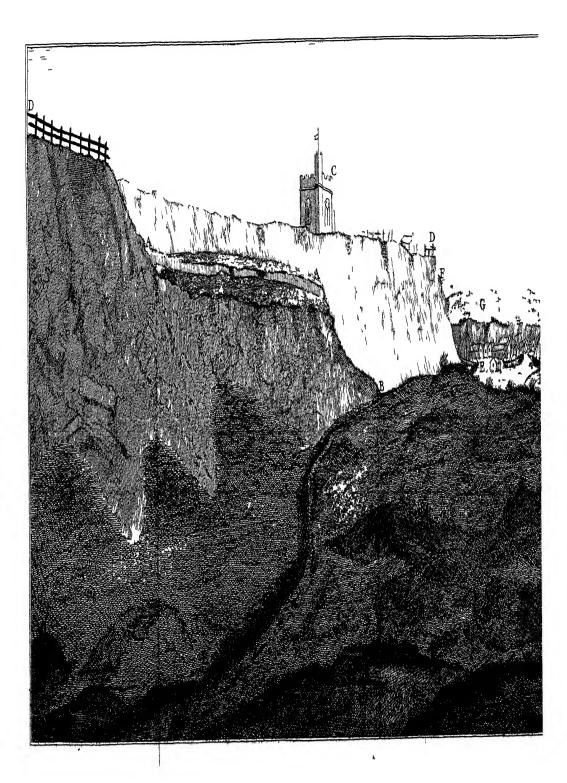
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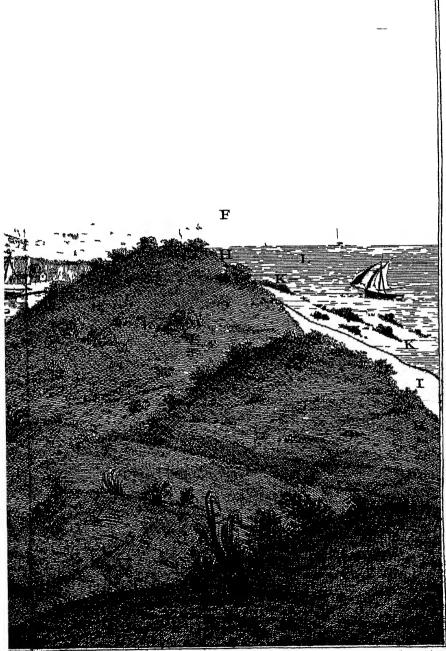
There is farther proof that Mr. SACKETTE did not examine into the matter himself, but rested what he said upon the report of others; and this is, that Tarlingham-house is not seen over the top of the hill in the line of fight EG, but confiderably to the left of it, in the line EI, and clear even of the base of the hill. Besides, a moment's reslection would have told him, that the finking of the hills could not produce the effects he mentions; for if the ground in the plain was pushed forward by it, it could not be a partial flipping; not only the church, and the whole town, must have been removed, but every object between the base of the hills and the cliff must have been removed out of their place; but I may venture to affirm, there is no proof of this having been done. I should have been drawn into the same or similar errors myself, if I had rested satisfied with the first accounts I received from an ancient fisherman. He told me the same story of the hills sinking in his time, and Tarlingham-house appearing higher than it did fince he could remember. In one part of his relation he was right; for I found, upon inquiry, that Tarlingham-house has been taken down, and built upon a much larger scale than formerly, fince it has been in the hands of the present proprietor.

If what I have faid should not prove satisfactory, I shall be happy in giving you any sarther information upon this subject in my power; and am, Sir, &c.

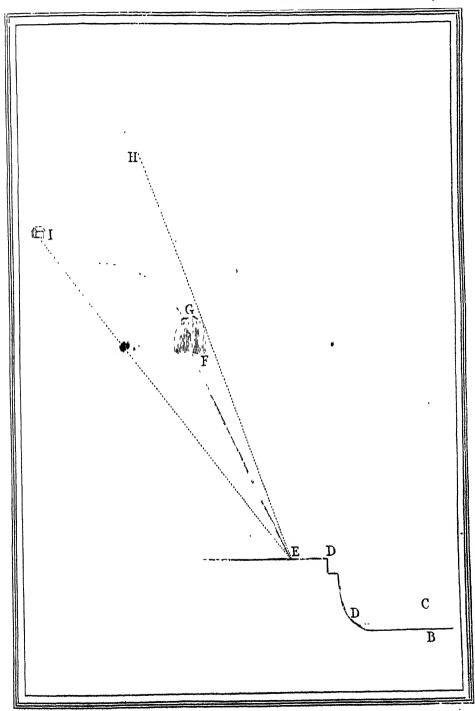
J. LYON.







Bywelc



XI. Particulars relative to the Nature and Customs of the Indians of North-America. By Mr. Richard Mc Causland, Surgeon to the King's or Eighth Regiment of Foot. Communicated by Joseph Planta, Esq. Sec. R. S.

#### Read February 16, 1786.

Thas been advanced by feveral travellers and historians that the Indians of America differed from other males of the human species in the want of one very characteristic mark of the sex, to wit, that of a beard. From this general observation, the Esquimaux have been excepted; and hence it has been supposed, that they had an origin different from that of the other natives of America. Inferences have also been drawn, not only with respect to the origin, but even relative to the conformation of Indians, as if this was in its nature more imperfect than that of the rest of mankind.

It appears somewhat singular that authors, in deducing the origin both of the Esquimaux and of the other Indians of America from the old world, should never have explained to us how the former came to retain their beards, and the latter to lay them aside. To ascertain the authenticity of this point may perhaps prove of little real utility to mankind; but the singularity of the fact certainly claims the attention of the curious: and as it is impossible to fix any limits to the infe-

rences which may at one time or another be drawn from alledged facts, it must always be of consequence to inquire into the authenticity of those facts, how little interesting soever they may at present appear.

I will not by any means take upon me to fay that there are not nations of America destitute of beards; but ten years residence at Niagara, in the midst of the Six-Nations (with frequent opportunities of seeing other nations of Indians) has convinced me, that they do not differ from the rest of men, in this particular, more than one European differs from another: and as this impersection has been attributed to the Indians of North-America, equally with those of the rest of the Continent, I am much inclined to think, that this affertion is as void of foundation in one region as it is in the other.

All the Indians of North-America (except a very fmall number, who, from living among white people, have adopted their customs) pluck out the hairs of the beard; and as they begin this from its first appearance, it must naturally be supposed, that to a superficial observer their faces will feem fmooth and beardless. As further proof that they have beards, we may observe, first, that they all have an instrument for the purpose of plucking them out. Secondly, that when they neglect this for any time, several hairs sprout up, and are seen upon the chin and face. Thirdly, that many Indians allow tufts of hair to grow upon their chins or upper lips, refembling those we see in different nations of the old world. Fourthly, that several of the Mohocks, Delawares, and others, who live amongst white people, sometimes shave with razors, and sometimes pluck their beards out. These are facts which are notorious amongst the Army, Indian-Traders, &c.; and which

are never doubted in that part of the world by any person in the least conversant with Indians: but as it is difficult to transport a matter of belief from one country to another distant one, and as the authors who have maintained the contrary opinion are too respectable to be doubted upon light grounds, I by no means intend to rest the proofs upon what has been said, or upon my single affertion.

I have provided myself with two authorities, which I apprehend may in this case be decisive. One is Colonel BUTLER, Deputy Superintendant of Indian Affairs, well known in the late American war, whose great and extensive influence amongst the Six-Nations could not have been acquired by any thing less than his long and intimate knowledge of them and their language. The other authority is that of THAYENDANEGA, commonly known by the name of Captain JOSEPH BRANT, a Mohock Indian of great influence, and much spoken of in the late war. He was in England in 1775, and writes and speaks the English language with tolerable accuracy. I shall therefore only subjoin their opinions upon this matter, the originals of which I have under their own signatures.

#### Colonel Butler's.

THE men of the Six-Nation Indians have all beards naturally, as have all the other nations of North-America which I have had an opportunity of feeing. Several of the Mohocks shave with razors, as do likewise many of the Panees who are kept as slaves by the Europeans. But in general the Indians pluck out the beard by the roots from its earliest appearance; and as their faces are therefore smooth, it has been supposed that they were destitute of beards. I am even of opinion, that

Mr. Mc CAUSLAND's Observations on the

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f the Indians were to practife shaving from their youth, many of them would have as strong beards as Europeans.

(Signed)

Niagara, April 12, 1784.

JOHN BUTLER.
Agent of Indian Affairs.

## Captain BRANT's.

THE men of the Six-Nations have all beards by nature; as have likewise all other Indian nations of North America which I have seen. Some Indians allow a part of the beard upon the chin and upper lip to grow, and a sew of the Mohocks shave with razors in the same manner as Europeans; but the generality pluck out the hairs of the beard by the roots as soon as they begin to appear; and as they continue this practice all their lives, they appear to have no beard, or at most only a sew straggling hairs which they have neglected to pluck out. I am however of opinion, that if the Indians were to shave they would never have beards altogether so thick as the Europeans; and there are some to be met with who have actually very little beard.

(Signed)

JOS. BRANT THAYENDANEGA.

Niagara, April 19, 1783.

Upon this subject I shall only further observe, that it has been supposed by some, that this appearance of beard on Indians arises only from a mixture of European blood; and that an Indian of pure race is intirely destitute of it. But the nations, amongst whom this circumstance can have any influence, bear so small a proportion to the multitude who are unaffected

by it, that it cannot by any means be considered as the cause; nor is it looked upon as such either by Captain BRANT or Colonel BUTLER.

I shall here subjoin a few particulars relative to the Indians of the Six-Nations, which, as they seem not to be well understood even in America, are probably still less known in Europe. My authorities upon this subject, as well as upon the former, are the Indian Captain BRANT and Colonel BUTLER.

Each nation is divided into three or more tribes; the principal of which are called the Turtle-tribe, the Wolf-tribe, and the Bear-tribe.

Each tribe has two, three, or more chiefs, called Sachems; and this distinction is always hereditary in the samily, but descends along the semale line: for instance, if a chief dies, one of his sister's sons, or one of his own brothers, will be appointed to succeed him. Among these no preference is given to proximity or primogeniture; but the Sachem, during his life-time, pitches upon one whom he supposes to have more abilities than the rest; and in this choice he frequently, though not always, consults the principal men of the tribe. If the successor happens to be a child, the offices of the post are performed by some of his friends until he is of sufficient age to act himself.

Each of these posts of Sachem has a name which is peculiar to it, and which never changes, as it is always adopted by the successor; nor does the order of precedency of each of these names or titles ever vary. Nevertheless, any Sachem, by abilities and activity, may acquire greater power and influence in the nation Vol. LXXVI.

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than those who rank before him in point of precedency; but this is merely temporary, and dies with him.

Each tribe has one or two chief warriors, which dignity is also hereditary, and has a peculiar name attached to it.

These are the only titles of distinction which are fixed and permanent in the nation; for although any Indian may by superior talents, either as a counsellor or as a warrior, acquire influence in the nation, yet it is not in his power to transmit this to his family.

The Indians have also their Great Women as well as their Great Men, to whose opinions they pay great deference; and this distinction is also hereditary in families. They do not sit in council with the Sachems, but have separate ones of their own.

When war is declared, the Sachems and great Women generally give up the management of public affairs into the hands of the warriors. It may however so happen, that a Sachem may at the same time be also a chief warrior.

Friendships seem to have been instituted with a view towards strengthening the union between the several nations of the confederacy; and hence Friends are called the sinews of the Six-Nations. An Indian has therefore generally one or more friends in each nation. Besides the attachment which subsists during the life-time of the two friends, whenever one of them happens to be killed, it is incumbent on the survivor to replace him, by presenting to his samily either a scalp, a prisoner, or a belt consisting of some thousands of wampum; and this ceremony is performed by every friend of the deceased.

The purpose and soundation of war parties therefore, is in general, to procure a prisoner or scalp to replace the friend or relation of the Indian who is the head of the party. An Indian

dian who wishes to replace a friend or relation presents a belt to his acquaintance, and as many as chuse to follow him accept this belt, and become his party. After this, it is of no consequence whether he goes on the expedition or remains at home (as it often happens that he is a child), he is still considered as the head of the party. The belt he presented to his party is returned fixed to the scalp or prisoner, and passes along with them to the friends of the person he replaces. Hence it happens, that a war party, returning with more scalps or prisoners than the original intention of the party required, will often give one of these supernumerary scalps or prisoners to another war party whom they meet going out; upon which this party, having sulfilled the purpose of their expedition, will sometimes return without going to war.



XII. Abstract of a Register of the Barometer, Thermometer, and Rain at Lyndon in Rutland, in 1785. By Thomas Barker, Esq. Asso of the Rain at South Lambeth, in Surrey; and at Selbourn and Fysield, Hampshire. Communicated by Thomas White, Esq. F.R.S.

Read February 23, 1786.

	1	Barometer.			Thermometer.					Rain.				
		Highest	Lowest	, Mean.		Low.			broad Low.		Lyndon	S.Lam- beth,	SeL bourn.	Fyfield.
		Inches.	Inches.	Inches.	0	-	٥	°	٥	0	Inch.	Inch.	Inch.	Inch.
Jan.	Morn. Aftern.	20 82	28,59	29,31	45½ 46	34½ 34½	39 40	45 47 <sup>½</sup>	25½ 27	.35 38 <del>1</del>	1,494	1,78	2,84	2,12 <u>1</u>
Feb.	Morn, Aftern	30,16	28,45	29,34	39 40	29 30½	342		10 23	28 34	0,365	1,20	1,80	1,85
Mar.	Morn. Aftern.	29,84	29,16	29,61	44 45	29½ 31½	36 37₹	43½ 51	17 27½	30 <u>₹</u> 38	0,212	0,35	0,30	0,00 <u>I</u>
Apr.	Morn. Aftern.	30,05	28,88	29,71	56 58	36 37	48 50	52½ 67½	25 37 <sup>1</sup> / <sub>2</sub>	41 54	0,175	0,34	0,17	0,141
May	lurrerm.	30,09	28,95	29,54	61 64	50½ 51½	55 50½ 61	58½ 75½	42 50¥		0,666	0,81	0,60	0,96
June	Aftern.	29,99	29,32	29,71	66½ 69½ 68½	753 55½	63	80½		55 69	1,567	2,04	1,39	1,19
July	Wifein.	29,82	28,97	29,42	73	61	64	64 83	53 <del>1</del> 60½	1	3,403	1,73	3,80	1,69
Aug	Wifelu.	29,72	28,99	29,36	64 <u>1</u> 65	56	61	71	55	64	4,315	3,05	3,21	4,26
Sept	Itaireitt.	29,89	28,51	29,29	63 64½			59 72	36 47	52 63	3,314	15	5,94	5,30
Joa.	tuttern.	29,99	28,95	29,45	58 59½		511	62 2	37 =	42½ 52	1,653	4,04	5,21	2,52
Nov	Attern.	30,02	28,33	29,33	3-2	392	44 <sup>1</sup> / <sub>2</sub> 45	56½	34½		1,125	] " '	2,27	1,463
Dec	Morn. Aftern	29,79	28,76	29,32	43 <sup>1</sup> 44 <sup>1</sup>	32 32	39 40	43 45½	201	33	2,037	1,53	4,02	3,04
									Iı	nches	20,206	19,62	31,55	24,551

The severe frost of December, 1784, broke early in January, cand was all gone before the middle, and the most open part of this sharp winter followed it, being misty or thick and warm very wet air; but the last day of January another frost set in, which, though not so steady as the former, was sometimes very severe, and did not go away till near the middle of March: and this winter, particularly the former frost about December 10, was much severer in the south of England than here, and greater signs of destruction by it were seen among the trees and plants there. From the breaking of the frost till April 4, was chiefly frosty mornings, and sometimes in the shade all day, so that, if you count the number of frosty days, I do not know that any winter had more, though I have known several longer frosts, and more steady, and some few more severe.

From April 5, the weather began to mend, was tolerably pleasant, and things came on gradually; yet not without some frosty mornings, even in May. The feed time began late, but was without hindrance; and there having been very little rain fince the frost, it harrowed remarkably fine, and the lands and roads were uncommonly dufty. The corn came up very well, except the late fown, fome of which, especially in the fouth of England, lay dry till June; for it continued a remarkably dry time all fpring, so that the grass was very short, and hay very scarce; yet the grain continued particularly fine-coloured, and eared very well, though some of the winter corn was rather thin; yet that was much mended by fome refreshing showers in May and June, which were enough to freshen things, though not to make much grass: and during this drought there were great numbers of little whirlwinds, sometimes several in a day. 2. The The weather began to be showery the middle of July, and feveral great rains; and after August 3d it was more frequent, but less at a time. This made plenty of good grass, but was very troublesome for the harvest, which was got in slowly, and with loss, but came out again full as well as could be expected. The wheat was remarkably full-eared. The barley good, except the late fown, which never ripened; and some too liastily carried in harvest. The birds of passage went away rather early this year: almost all the Swifts were gone in July, and most of the Swallows and Martins in September; the last were August 7, and October 12. It continued very showery till near the middle of October; after which the autumn was pretty fine, and less wet than before, yet enough to make it very dirty when the fun lost its power in December; and the winter began for the most part open and pleasant, till a frost and large fnow at Christmas, which grew severer to the end of the year.

## On the Variations of Seasons.

Measuring the rain for a few years will not shew completely the general quantity of rain which falls in any place; for there is a very great difference at different periods of time. If I had measured the rain at Lyndon only in the four years 1740, 1741, 1742, 1743, the mean would have been found to be only 16½ inches in a year; yet they were not all complained of as dry summers. 1740 was cold and dry till July 30. The spring

fpring 1741 was cold and dry, the fummer hot, dry, and burning till the beginning of September; then ten days wet and very warm again, being the finest autumn for grass ever known. 1742 was a showery summer, and 1743 wet in the middle; but then the winters were dry, so that the quantity of rain upon the whole was small. 1741 to 1750 the mean was 18½ inches. 1741 and 1750 were hot, dry, and burning, 1750 being the hottest year I have known. The intermediate years were neither very wet nor very dry; and this was the most plentiful and cheapest time for corn of any ten years I remember; for grain oftener fails in England from too much wet than too little. 1751 to 1760 the mean year was 221. 1760 was hot, dry, and burning; but several of the summers were wet, and the crops not fo plentiful. Three wet fummers together, 1754, 1755, and 1756, were a time of scarcity, and we have had more failing crops fince that time than before it. From 1761 to 1770 there was 231 in a year. 1762 was hot, dry, and burning; and 1765 cold and dry; but several years were wet, 1763 and 1768 remarkably so; and of those ten years several had failing crops, and some had great snows. There was a great change of the seasons at 1763; for I have had more rain fince that time than I had before it in the proportion of 5 to 4. From 1770 to 1780 there was at a mean 26 inches. 1771 was dry, and 1778 and 1779 were hot, yet not without fits of rain; and most of the other years were wet, and some great snows. 1773, 1774, and 1775, were so wet that there came 32 inches in a year, which is nearly double what there was from 1740 to 1743. In twelve months, from October 1773, to September 1774, there came 39,390 inches of rain, which is nearly a Lancashire year. And in

one month, September 1774, there was 8 inches: this was in barley and peafe harvest, and for three weeks together not a load could be carried in. By the above state of the case it appears, that, for four successive periods of ten years, the quantity of rain has been increasing each time.



XIII. An Account of Experiments made by Mr. John Me Nab, at Henley House, Hudson's Bay, relating to freezing Mixtures. By Henry Cavendish, Esq. F. R. S. and A. S.

## Read February 23, 1786.

IN my observations on Mr. Hutchins's Experiments. printed in the LXXIIId volume of the Philosophical Tranfactions. I gave my opinion concerning the cause of the cold produced by mixing fnow with different liquors. As there were fome circumstances, however, which seemed to form a difficulty in the way of this opinion, I was defirous of having further experiments made on the subject; and at the same time I thought that, by proper management, a greater degree of cold might be produced than had hitherto been done. On mentioning the experiments I wished to have made to Mr. Hutchins, he very obligingly defired Mr. Mo NAB; Master at Henley-House, to try them; who was so good as to undertake the bufinefs, and has executed it in the most satisfactory manner; as he has not only taken great pains, but has shewn the utmost attention and accuracy, in observing and relating all the phænomena which occurred, and has manifested great judgement in frequently adapting the manner of trying the experiments to appearances which occurred in former ones, to which we are indebted for great part of the most curious facts in this paper. His endeavours have also been attended with much success, as he has not only shewn many remarkable circumstances relating to the freezing of the nitrous and Vol. LXXVI. I i

and vitriolic acids, and the phænomena of freezing mixtures; but has also produced degrees of cold greatly superior to any before known.

- 1. In the above-mentioned Paper I said, that the cold produced by mixing spirit of nitre with snow, is owing to the melting of the fnow; and that in all probability there is a certain degree of cold, in which spirit of nitre is so far from diffolving fnow, that it will yield out part of its own water, and fuster that to freeze, as is the case with solutions of common falt; fo that if the cold of the materials, before mixing, is equal to this, no additional cold can be produced. A circumstance, however, which at first fight feems repugnant to this opinion, occurred in an experiment of FAHRENHEIT's for producing cold by a mixture of spirit of nitre and ice; namely, that the acid, which had been repeatedly cooled by different frigorific mixtures, was found frozen before it was mixed with the ice; notwithstanding which, cold was produced by the mixture. Professor BRAUN also found, that cold was produced by mixing frozen spirit of nitre with snow. On consideration, however, this appeared by no means inconfistent with the opinion there laid down, as there was great reason to think, that the freezing of the acid was of a different kind from that confidered in the above-mentioned Paper, and that it did not procced from the watery part separating from the rest and freezing: but that the whole acid, or perhaps the more concentrated part, froze; in which cafe it would not be extraordinary that the acid should diffolive more snow, and produce cold.
  - 2. To clear up this point, I fent to Hudson's Bay a bottle of spirit of nitre, of nearly the same strength as FAHRENHEIT's; and desired Mr. M. NAB to expose it to the cold, and, if it froze, to ascertain the temperature, and decant the fluid part into

another bottle, and fend both home to be examined, as it would thereby be known, whether it was the whole acid, or only the watery part, which froze, For the same purpose also I sent some dephlogisticated spirit of nitre of the same strength, and also some strong oil of vitriol. I also sent some spirit of nitre and spirit of wine, both diluted with so much water, that it was expected, that with the cold of Hudson's Bay they would suffer the first kind of congelation; that is, their watery part would freeze, and thereby make the difference between the two kinds of freezing more apparent.

3. In the same Paper I say, "That on adding snow gra-"dually to some of the spirit of nitre used by Mr. HUTCHINS, "I found, that the addition of a fmall quantity produced heat " instead of cold; and it was not until so much was added as to "increase the heat from 28° to 51°, that the addition of more " fnow began to produce cold; the quantity of fnow required " for this purpose being pretty exactly one quarter of the weight of the spirit of nitre, and the heat of the snow and " air of the room, as well as the acid, being 28°. The reason of this is, that a great deal of heat is produced by mixing "water with spirit of nitre, and the stronger the spirit is, the " greater is the heat produced. Now it appears from this experiment, that before the acid was diluted, the heat or produced by its union with the water formed from the melted " fnow was greater than the cold produced by the melting of "the snow; and it was not till it was diluted by the addition. " of one quarter of its weight of that substance, that the cold " generated by the latter cause began to exceed the heat gene-" rated by the former. From what has been faid, it is evi-"dent, that the cold of a freezing mixture, made with the " undiluted acid, cannot be quite fo great as that made with ss the Tiz

"the same acid, diluted with a quarter of its weight of water, "supposing the acid and snow to be both at 28° of heat; and there is no reason to think, that the event will be different if they are colder; for the undiluted acid will not begin to generate cold, until so much snow is dissolved as to increase its heat from 28° to 51°, so that no greater cold will be produced, than would be obtained by mixing the diluted acid heated to 51° with snow of the heat of 28°. This method of adding snow gradually to an acid, is much the best way I know of finding what strength it ought to be of, in order to produce the greatest effect possible."

As it seemed likely that, by following this method, a greater degree of cold might be produced than had been done hitherto, I sent three other bottles of spirit of nitre and oil of vitriol, all three diluted, but not so much so, but that I thought they would require a little further dilution, in order to reduce them to their properest degree of strength. I also sent a bottle of highly reclified spirit of wine, and a mixture of equal quantities of the above-mentioned common spirit of nitre and oil of vitriol; and desired Mr. Mc NAR to find what degree of cold-could be produced by mixing them with snow, after having first reduced them, in the above-mentioned manner, to their best degree of strength \*.

He was also defired to ascertain how much snow he added; for as their strength was determined before they were sent out, it would thereby be known what was the best strength of these liquors for frigorisic mixtures.

<sup>\*</sup> This might have been done at home; but I thought it not unlikely that the firength found this way might differ, in some measure, according to the heat in which the experiment was tried.

All these bottles were numbered with a diamond; and as I shall sometimes distinguish them by these numbers, and as it may be of use to those who may consult the original, I have added the following list of these bottles, with their contents.

N°	Liquors mentioned in Art. 3.	Weight of narble which they diffolve.	gravity at
168 27 103 28 8	Spirit of nitre,  Dephlogisticated spirit of nitre,  Diluted oil of vitriol,  Equal weights of N° 168. and N° 103.  Very highly rectified spirit of wine,	,582 ,53 ,654 	1,4371 1,4040 1,5596 — — ,8195
ŀ	Liquors mentioned in Art. 2.		
151 142 139 141 143	Strong oil of vitriol,  Spirit of nitre,  Some of the fame diluted with twice its weight of water,  Dephlogificated spirit of nitre,  Some of the same spirit of wine as in N° 8. diluted with 1½ its weight of water,	,98 ,525  ,53	1,8437 1,4043  1,4033
72 171	Dilutedoilof vitriol for comparing the thermometers, Oil of vitriol of about the usual strength, but the exact strength not known, intended to refresh the former when too weak.	1	

4. Professor Braun says, that by mixtures of snow and spirit of nitre he sunk thermometers silled with oil of sassars, and some other essential oils, to -100° er -124°; and that, by the same means, he sunk thermometers silled with the highest rectified spirit of wine to -148°. Though there seemed great reason to think, from Mr. Hutchins's experiments, that there must be some mistake in this; yet, as it was possible that the essential oils, and even spirit of wine of a strength much different from that with which Mr. Hutchins's thermometers were salled, might sollow a considerably different progression in their contraction.

contraction by great degrees of cold, I fent a thermometer filled with oil of fassafras, and two others with spirits of wine. One of these last was filled with the highest rectified spirits I could procure, its specific gravity at 60° of heat being ,8185; the other was intended to be filled with common spirits, though from circumstances I am inclined to suspect that also to have been filled with the best spirits. Besides these, there was sent a mercurial thermometer, accurately adjusted, according to the directions of the Committee of the Royal Society, printed in the LXVIIth volume of the Transactions; and also the two spirit thermometers used by Mr. Hutchins, which were filled with spirits whose specific gravity was ,8247.

5. These thermometers were compared together by exposing them to the cold, with their balls immersed in a glass vessel silled with diluted oil of vitriol. They were at times also compared in cold more violent than the natural cold of the climate, by adding snow to the acid in which they were tried, in which case care was taken to keep the mixture frequently stirred. Oil of vitriol was recommended for this purpose, as a fluid which would most likely bear any degree of cold without freezing, and whose natural cold might be much increased by the addition of snow. It seems to have answered the purpose very well, and not to have been attended with any inconvenience.

During the first comparison of these thermometers, a whitish globule, such as those which appear in frozen oil, was observed in the tube of the thermometer filled with oil of sassas. This appearance of congelation did not much increase; but two days after a large air bubble was sound in its ball, which prevented Mr. Mc NAB from making surther observations with it.

It is well known, that spirit of wine expands more by a given number of degrees of a mercurial thermometer in warm temperatures than in cold ones; and this inequality, as might be expected, was less in the stronger spirit than in the weaker, but the difference was inconsiderable. The oil of sassars also had some of this inequality, but much less. It however appears to be by no means a proper sluid for filling thermometers with. No appearance was observed which indicates any considerable irregularity in the contraction of spirits of wine in intense cold, or which renders it probable, that thermometers filled therewith could be sunk by a mixture of snow and spirit of nitre to a degree near approaching to that mentioned by Professor Braun.

6. Mr. Mc Nab in his experiments fometimes used one thermometer and sometimes another; but in the following pages I have reduced all the observations to the same standard; namely, in degrees of cold less than that of freezing mercury I have set down that degree which would have been shewn by the mercurial thermometer in the same circumstances; but as that could not have been done in greater degrees of cold, as the mercurial thermometer then becomes of no use, I sound how much lower the mercurial thermometer stood at its freezing point, than each of the spirit thermometers, and increased the cold shewn by the latter by that difference.

# On the common and dephlogisticated Acids of Nitre.

The following experiments shew, that both these acids are capable of a kind of congelation, in which the whole, and not merely the watery part, freezes. Their freezing point also differs

differs greatly according to the strength, and varies according to a very unexpected law. Like water too they bear being cooled very much below their freezing point before the congelation begins, and as soon as that takes place, immediately rise up to the freezing point.

7. On the morning of Feb. 1. the common and dephlogisticated spirits of nitre, Nº 142 and 141, whose specific gravities were 1,4043 and 1,4033, were found clear and fluid, the cold of the air at that time being -47°. They also bore being shook without any alteration; but on taking out their stoppers, both of them in a few minutes began to freeze, the congelation beginning by a white appearance at top, which gradually spread to the bottom; and they became so thick as not to move on inclining the phial. For want of a thermometer whose ball reached far enough below its scale, Mr. Mo NAB was not able to determine their cold while in the bottle; but in somewhat more than an hour's time, the frozen acid had so much subsided as to admit of his pouring a little fluid matter out of each into a glass with a thermometer in it \*; whereby the cold of the common spirit of nitre was found to be -31°1, and that of the dephlogisticated acid - 30°, the temperature of the air being -41°. Each of these decanted liquors, at the time their temperature was tried, was full of small spicula of ice: they were then put into phials well stopped, and they, as well as the undecanted liquors, fent home to be examined. The decanted part of the common

<sup>\*</sup> It may be asked, why it was more possible to decant any liquor at this time than at first, as the acid was all the while exposed to a cold much below the freezing point? The reason in all probability is, not that any part of the ice first formed dissolved, but that the small filaments into which it shat collected toges wher, and in some measure subsided to the bottom.

fpirit of nitre dissolved ,535 of its weight of marble, and the undecanted part ,523; for which reason I shall call the strength of the former ,535, and that of the latter ,522; which mode of reckoning is observed in the remainder of this Paper. The strength of the decanted part of the dephlogisticated acid was ,56, and that of the undecanted part ,528; so that it appears that in each of these acids the unfrozen part was a little stronger than the frozen part. It is remarkable, that in the common spirit of nitre, the decanted part, though stronger than the other, was paler coloured and less suming.

- 8. On Dec. 21, the temperature of the air being  $-28^{\circ}$ , fome dephlogisticated spirit of nitre (N° 27.) of nearly the same strength as the former acid, was poured into a jar, in order to be diluted with snow, as recommended in Art. 2. Immediately after it was decanted, it began to freeze, in the same manner as before described, except that a less portion of it seems to have congealed: its temperature, tried by dipping a thermometer into it, was  $-19^{\circ}$ , where it remained stationary for many minutes; it was then diluted with snow, as will be mentioned in Art. 14. whereby its strength was reduced to .434.
- 9. On Dec. 29th, this diluted acid was completely melted, and half of it poured into a jar with a ground stopper, and both portions exposed to the air. In the morning they were perfectly sluid; but on taking the stopper out of the jar, and dipping in it a thermometer, the acid immediately froze, beginning by forming a white coat round the ball of the thermometer, which gradually spread through the whole shuid; and at the same time the thermometer rose till it stood stationary at -5°. The cold of the acid before it began to sreeze must have been about -30°½, that being the temperature of a Vol. LXXVI.

glass of vitriolic acid standing near it; but the thermometer which was dipped into it was five or six degrees colder, which seems to be the cause of the congelation beginning round the ball.

In the afternoon a thermometer was dipped into the other half of the acid, where, as the weather had grown less cold, it stood above a minute at  $-25^{\circ}$ , without freezing; then, however, the acid froze, with the same appearance as in the morning, and at the same time the thermometer rose to  $-4^{\circ}$ , and became stationary.

This acid, being left in the air with the thermometer in it, was found in the evening at  $-45^{\circ}$ ; it however was not intirely frozen, being only thick as an unguent, which shews that the unfrozen part must have been of a different strength from the frozen part; but it does not appear whether stronger or weaker. The next morning it was frozen solid, though the cold was only half a degree greater.

On Jan. 16th, this acid was again tried in the same manner; it then suffered a thermometer, whose ball had been previously warmed in the hand, to be dipped into it, and remain there several minutes without freezing, though its temperature was  $-35^{\circ}$ . But on lifting up the thermometer, a drop fell from its ball into the acid, which immediately set it a freezing, and it rose up to  $-4^{\circ}\frac{1}{2}$ .

10. On Dec. 22d, the spirit of nitre (N° 168.) which a few days before had been diluted with snow, so as to be reduced to the strength of ,411, was divided into two equal parts, and exposed to the cold. On Dec. 29th, when the temperature of the air was  $-17^{\circ}\frac{1}{2}$ , one of these parts was found beginning to freeze; the other was sluid, but began to freeze on dipping a thermometer; the thermometer in both kept stationary at

- -1°. The latter was twice re melted and exposed to the cold, and both times the temperature of the frozen acid came out the same as before.
- owing only to its confisting of very slender flaments; for in some cases, where it froze slower, and where, in consequence, it shot into larger solid masses, they were transparent, and of the same colour as the acid itself. By the continuance of a sufficient cold, the acid, which by hasty freezing put on the white appearance, would become hard solid ice, but yet still retained its white appearance, owing perhaps to the silaments first shot consisting of an acid differing in strength from that which froze afterwards, and filled up the interstices.

In all these experiments, whether the ice was formed into minute filaments or solid masses, still, whenever there was a sufficient quantity of sluid matter to admit of it, they constantly subsided to the bottom; a proof that the frozen part was heavier than the unfrozen. The difference indeed is so great, that in one case where it froze into solid crystals on the surface, these crystals, when detached by agitation, fell with force enough to make a tinkling noise against the bottom of the glass.

These acids contract very much on freezing. Whenever the acid is frozen solid, the surface, instead of being elevated in ridges, like frozen water, is depressed and sull of cracks. In one experiment Mr. Mc NAB, after a glass almost sull of acid was nearly frozen, filled it to the brim with fresh acid; and then, after it was completely frozen, the surface was visibly depressed, with suffures one-eighth of an inch broad, extending from top to bottom. It is this contraction of the acid in freezing which makes the frozen part subside in the fluid R k 2

part; as it was found, in the undiluted acid, that the latter contifted of a stronger, and consequently heavier, acid than the former. But still the subsidence of the frozen part shews, that the ice is not mere water, or even a very dilute acid; which indeed was proved by the examination of the liquors sent home.

The ninth and tenth articles shew, that though the acids bear being cooled greatly below the freezing point, without any congelation taking place, yet as soon as they begin to freeze they immediately rise up to their freezing point; and this point is always very nearly, if not exactly, the same in the same acid; for those acids were frozen and melted again three or four times, and were cooled considerably more below the freezing point in one trial than another, and yet as soon as they began to freeze the thermometer immersed in them constantly rose nearly to the same point.

The quantity which these acids will bear being cooled below the freezing point, without freezing, is remarkable. The diluted spirit of nitre, whose freezing point is  $-1^{\circ}\frac{1}{2}$ , once bore being cooled to near  $-39^{\circ}$ , without freezing, that is, near 37 degrees below its freezing point. The diluted dephlogisticated spirit of nitre, whose freezing point is  $-5^{\circ}$ , bore cooling to  $-35^{\circ}$ ; and the dephlogisticated spirit of nitre (141) whose true freezing point is most likely  $-19^{\circ}$  (see next article) bore being cooled to  $-49^{\circ}$ : perhaps too they might have born to be cooled considerably lower without freezing, but how much does not appear. It must be observed, however, that the same diluted spirit which at one time bore being cooled to  $-39^{\circ}$ , at another froze, without any apparent cause, when its cold was certainly less than  $-30^{\circ}$ , and most likely not much below  $-18^{\circ}$ .

12. The freezing point differs remarkably, according to the ftrength of the acid. In the diluted dephlogisticated and common spirit of Art. 7. and 8. the freezing point was  $-5^{\circ}$  and  $-1^{\circ}\frac{1}{2}$ . In the dephlogisticated and common spirit of Art. 5. the decanted parts of which were stronger than the foregoing in scarcely so great a proportion as that of four to three, it feemed to be - 30° and - 31° 1. It may indeed be fufpected, that as this point was determined only by pouring a small quantity of the acid into a glass, at a time when the air and glass were much colder than the acid, these decanted liquors might be cooled by the air and glass, and thereby make the freezing point appear lower than it really was: but I do not think this could be the case; for as the decanted liquors were full of small filaments of ice, they could hardly be cooled fenfibly below their freezing points without freezing; and any cold, communicated to them by the air or glass, would serve only to convert more of them into ice, without fenfibly increafing their cold: fo that I think this experiment determines the true freezing point of their decanted part; but it must be observed, that as the decanted part was rather stronger than the rest, it is very possible that the freezing point of the undecanted part might be considerably less cold.

A circumstance which might incline one to think, that the way by which the freezing point was determined in this experiment is defective is, that the freezing point of the dephlogisticated acid N° 27. though nearly of the same strength as that last mentioned, but rather stronger, was much less low, being only -19°. But I have little doubt that the true reason of this is, that in the former acid the strength of the decayted part, which is the part whose freezing point was tried, was found to be at least  $\frac{1}{20}$  greater than that of the whole mass; where is

in N° 27. the fluid part was in all probability not fensibly stronger than the whole mass; for as N° 27. was cooled only seven degrees below the freezing point, and its temperature was tried soon after its beginning to freeze, not much of the acid could have frozen; whereas the other was cooled 15 degrees below its freezing point, and was exposed for an hour or two to an air not much less cold, in consequence of which a considerable part of the acid must have frozen; so that in all probability the acid, whose freezing point was found to be  $-30^{\circ}$ , was in reality  $\frac{1}{20^{\circ}}$  part stronger than that whose freezing point was  $-19^{\circ}$ .

If this reasoning be just, the freezing point of these acids is as follows:

•		Freezing point.
Dephlogisticated spirit of nitre, whose strength = {  Common spirit of nitre, whose strength = {	,56 ,53	- 30° - 19 - 4\frac{1}{2}
Common spirit of nitre, whose strength = {	,54	$-31\frac{1}{2}$

On the Phænomena objerved on mixing Snow with these Acids.

13. On Dec. 13, snow was added to the spirit of nitre N° 168, as recommended in Art. 2. The snow was put in very gradually, and time was taken to find what effect each addition had on the thermometer and mixture, before more was added. The temperature of the acid before the mixture was -27°, and each addition of snow raised the thermometer a little, till it rose to -1°½; after which the next addition made it sink to -2°, which shewed that sufficient snow had then been added. The quantity

quantity of fnow used was pretty exactly 40 of the weight of the acid, the weight of the acid being 13 oz. so that the strength of the diluted acid was reduced to ,411.

The acid before the addition of snow had no signs of freezing, its temperature being in all probability much above its freezing point; yet the snow did not appear to dissolve, but formed thin white cakes, which however did not float on the surface, but fell to the bottom, and when broke by the spatula formed a gritty sediment; so that it appears, that these cakes are not simply undissolved snow, but that the adjoining acid absorbed so much of the snow in contact with it, as to become diluted sufficiently to freeze with that degree of cold, and then congealed into these cakes. The quantity of congealed matter seems to have kept increasing till the end of the experiment.

14. On Dec. 21, an experiment was made in the same manner with the dephlogisticated spirit of nitre N° 27. The acid began to freeze in pouring it into the jar in which the mixture was to be made, and stood stationary there at -19°, as related in Art. 6.; so that the liquor at the beginning of the experiment was white and thick, which made the effect of the addition of the snow less sensible. However, the congealed matter constantly subsided to the bottom, and the quantity seems to have continued increasing to the end of the experiment. The heat of the mixture rose to -4° before cold began to be produced, and the quantity of snow added was  $\frac{2}{120}$  of that of the acid, so that the strength of the acid was reduced to ,437 by the dilution.

A very remarkable circumstance in this experiment is that the acid, while the snow was adding, first became of a yel-

lowish, and afterwards of a greenish or bluish hue. This colour did not go off by standing, but continued at least ten days, during which time the acid constantly kept that colour, except when by hasty freezing it shot into small silaments, in which case it put on the white appearance which these acids always assumed under those circumstances; but once that by gradual freezing it shot into transparent ice, this ice was of a bluish colour.

It is difficult to conceive what this colour should proceed from. Spirit of nitre is well known to affume this colour when much phlogisticated and properly diluted; but one does not fee why it should become phlogisticated by the addition of the fnow, and still less why the dephlogisticated acid should become more phlogisticated thereby than the common acid did; for though it is not extraordinary, that a process not capable of producing any increase of phlogistication in the common acid, should make this as much phlogisticated as that, yet it is very extraordinary that it should make it more so. No notice is taken of any effervescence or discharge of air while it was affuming this colour, nor was it observed that it became more fmoking thereby, or that the top of the phial in which it was kept became full of red fumes, as might naturally be expected if it was rendered much phlogisticated. These are circumstances which, considering Mr. Ma NAB's great attention to set down all the phænomena that occurred, I should think would hardly have been omitted if they had really happened.

addition of snow produced heat, until it arrived pretty exactly at what was found to be the freezing point of the diluted acid; but that as soon as it arrived at that point, the addition of more snow began to produce cold. This can hardly be owing merely

merely to accident, and to both acids having happened to be of that precise degree of heat before the experiment began, that their heat after dilution should coincide with the freezing point answering to their new strength. The true cause seems to be as follows. It will be shewn in Art. 16. and 17. that the freezing point of these acids, when diluted as in the foregoing experiments, is much less cold than when they are considerably more diluted; and it was before shewn to be much less cold than when not diluted; fo that there must be a certain degree of strength, not very different from that to which these acids were reduced by dilution, at which they freeze with a lefs degree of cold than when they are either stronger or weaker. Now in these experiments, the temperature of the liquors before dilution was below this point of easiest freezing, and a great deal of the acid was in a state of congelation all the time of dilution; the consequence of which is, that when they were diluted to the strength of easiest freezing, they would also be at the heat of easiest freezing; for they could not be below that point, because, if they were, so much of the acid would immediately freeze as would raise them up to it; and they could not be above it, for, if they were, fo much of the congealed acid. would diffolve as would fink them down to it. After they were arrived at this strength of easiest freezing, the addition of more fnow would produce cold, unless this strength be greater than that at which the addition of a small quantity of fnow begins to produce cold; but even were this the case, heat would not be produced, but the temperature of the acids would remain stationary until they were so much diluted that the addition of more fnow should produce cold. So that, in either case, the heat of the acids, at the time that the addition of fresh snow began to produce cold, must be that of easiest freezing; Vol. LXXVI. LI

freezing; and consequently, as this heat was found to coincide very nearly with the freezing point of these acids, after dilution, it follows that their strengths at that time could differ very little from the strength of easiest freezing.

If the temperature of the liquors at the beginning of the experiment had been above the point of easiest freezing, none of the acid would have congealed during the dilution, and nothing could have been learnt from the experiment relating to the point of eafiest freezing; but the heat would have kept increasing, till the acid was diluted to that degree of strength at which the cold produced by the diffolving of the fnow was just equal to the heat produced by the union of the melted fnow with the acid \*; after which the addition of more fnow would begin to produce cold. When I recommended this method of finding the best strength of spirit of nitre for producing cold, by the additions of fnow, I was not aware of any impediment from the freezing of the acid, in which case it would have been a very proper method; but on account of this circumstance it can hardly be considered as such, except when the cold of the acid at setting out is less than that of easiest freezing.

In the dephlogisticated spirit of nitre the freezing points answering to the strength of ,434, ,53, and ,56, were said to be  $-4^{\circ}\frac{1}{2}$ ,  $-19^{\circ}$ , and  $-30^{\circ}$ ; and the differences of  $-30^{\circ}$  and  $-19^{\circ}$  from  $-4^{\circ}\frac{1}{2}$  are to each other very nearly in the duplicate ratio of ,126 and ,096, the differences of the corresponding strengths from ,434; which, as ,434 is the strength of easiest freezing, is the proportion that might naturally be

<sup>\*</sup> In the experiment related in my observations on Mr. Hutchins's Experiments, this strength was rather greater than that of easiest freezing: but whether it is so in degrees of cold exceeding that in which my experiment was tried, does not appear.

A expected,

expected, and confequently serves in some measure to confirm the reasoning in this and the 12th Article.

16. After Mr. Me NAB had diluted these acids as abovementioned, he divided each of them into two parts, and tried what degree of cold could be produced by mixing them with fnow. On January 15th, one of these parts of the common spirit of nitre was tried. It was fluid when the experiment began, though its temperature, as well as that of the fnow, was - 21° 1; but on adding fnow it immediately began to freeze, and grew thick, and its heat increased to  $-2^{\circ}\frac{1}{2}$ ; but by the addition of more fnow it quickly funk again, and at last got to -43° 4. During the addition of the snow, the mixture grew thinner, and by the time it arrived at nearly the greatest degree of cold, confifted vifibly of three parts: the lowest part, which confifted of frozen acid, was white and felt gritty; the upper part, which occupied about an equal space, was also white, but felt soft, and must have consisted of unmelted fnow; the other part, which occupied by much the smallest space, was clear and fluid. The quantity of snow added was about in of the weight of the acid, and confequently its strength was reduced to ,243.

Though snow was added to the acid in this experiment as long as, and even longer than, it produced any increase of cold, yet some days after, on adding more snow to the mixture, while it was sluid, and of the temperature of  $-45^{\circ}$ , the cold was increased to  $-44^{\circ}$ , or 1 degree lower than before. Mr. Me NAB did not perceive the snow to melt, though in all probability some must have done so, or no cold would have been produced.

The cause of this seems to be, that in the preceding experiment the congealed part of the acid was stronger than the

fluid part; fo that, though the fluid part was not strong enough to dissolve snow in a cold greater than - 43°4, yet the whole acid together was strong enough to do it in a cold one degree greater.

A circumstance occurred in the last experiment which I cannot at all see the reason of; namely, a small part of the acid being poured into a saucer, before the addition of the snow, it was in an hour's time changed into solid ice, though the cold of the air, at the time the acid was poured out, was only -41° 4, and does not seem to have increased during the experiment.

- 17. On December 30, the other half of the same acid had been tried in the same manner; at the beginning of the experiment not more than one-ninth part of the acid was stuid, the rest solid clear ice; its temperature was  $-34^{\circ}\frac{\pi}{2}$ , and that of the snow nearly the same; the greatest degree of cold produced was  $-42^{\circ}\frac{\pi}{4}$ ; and the quantity of snow employed was about one-eighteenth of the weight of the acid; so that the strength of the mixture was 38. The streezing point of the acid thus diluted appears to be about  $-45^{\circ}\frac{\pi}{4}$ ; for by the increase of warmth during the day-time, most of the congealed matter dissolved; but in the evening it began to freeze again, so as to become thicker, its temperature being then  $-45^{\circ}\frac{\pi}{4}$ ; and the next morning it was frozen solid, its cold being one degree greater.
- 18. On December 12, the diluted spirit of nitre N° 139. whose strength was ,175, was found frozen, its temperature being -17. The fluid part, which was full of thin flakes of clear ice, and was of the consistence of syrup, was decanted into another bottle, and sent back. Its strength was ,21, and was greater than that of the undecanted part in the proportion of ,21 to ,16; so that, as not much of the undecanted part was

really congealed, the frozen part of the acid must have been much weaker than the rest, if not mere water. Accordingly, during the melting of the undecanted part, the frozen particles swam at top. Mr. Mc NAB added snow to a little of the decanted liquor, but it did not dissolve, and no increase of cold was produced.

19. From these experiments it appears, that spirit of nitre is fubject to two kinds of congelation, which we may call the aqueous and spirituous; as in the first it is chiefly, if not intirely, the watery part which freezes, and in the latter the spirit itself. Accordingly, when the spirit is cooled to the point of aqueous congelation, it has no tendency to dissolve snow and produce cold thereby, but on the contrary is disposed to part with its own water; whereas its tendency to diffolve fnow and produce cold, is by no mean's destroyed by being cooled to the point of spirituous congelation, or even by being actually congealed. When the acid is excessively dilute, the point of aqueous congelation must necessarily be very little below that of freezing water; when the strength is ,21, it is at -17°, and at the strength of ,243, it seems, from Art. 16. to be at .-44°4... Spirit of nitre, of the foregoing degrees of strength, is liable only to the aqueous congelation, and it is only in greater strengths that the spirituous congelation can take place. This seems to be performed with the least degree of cold, when the strength is ,411, in which case the freezing point, is at - 1° 1. When the acid is either stronger or weaker, it requires a greater degree of cold; and in both cases the frozen part seems to approach nearer to the strength of ,411 than the junfrozen part; it certainly does fo, when the strength is greater than ,411, and there is little doubt but what it does so in the other case. At the strength of ,54, the point of spirituous congelation.

. . .

congelation is  $31^{\circ}\frac{1}{2}$ , and at ,33 probably  $-45^{\circ}\frac{1}{4}$ ; at least one kind of congelation takes place at that point, and there is little doubt but that it is of the spirituous kind. In order to present this matter more at one view, I have added the following table of the freezing point of common spirit of nitre answering to different strengths.

Strength,	Freezing point.	
,54 ,411 ,38 ,243	- 3 <sup>1</sup> ½ - 1 ½* - 45 <sup>‡</sup> - 44 <sup>‡</sup>	fpirituous congelation. aqueous congelation.

120. In trying the first half of the dephlogisticated spirit of nitre, the cold produced was  $-44^{\circ}\frac{1}{2}$ . The acid was sluid before the addition of the snow, and of the temperature of  $-30^{\circ}$ , but froze on putting in the thermometer, and rose to  $-5^{\circ}$ , as related in Art. 7.

In trying the second part, the acid was about 0° before the addition of the snow, and therefore had no disposition to freeze. The cold produced was  $-42^{\circ}\frac{1}{2}$ .

As the quantity of snow added in these experiments was not observed, they do not determine any points of aqueous or spirituous congelation in this acid; but there is reason to think, that these points are nearly the same as those of common spirit of nitre of the same strength, as the cold produced in these experiments was nearly the same as that obtained by the common spirit of nitre.

<sup>\*</sup> The point of easiest freezing.

#### On the Vitriolic Acid.

21. On December 12, the strong oil of vitriol N° 151. was found frozen, and was nearly of the colour and consistence of hogs-lard. Its temperature, found by pressing the ball of a thermometer into it, was  $-15^{\circ}$ , and that of the air nearly the same; but in the night it had been exposed to a cold of  $-33^{\circ}$ . It dissolved but slowly on being brought into a warm room, and was not completely melted before it had risen to  $+20^{\circ}$ , and even then was not very fluid, but of a syrupy consistence. During the progress of the melting, the congealed part sunk to the bottom, as in spirit of nitre: and many air bubbles separated from the acid, which, when it was completely melted, formed a little froth on the surface. As soon as it was sufficiently melted to admit of it, which was not till it had risen to the temperature of  $+10^{\circ}$ , the sluid part was decanted, and both were sent home to be examined.

It is remarkable, that the frozen part did not intirely diffolve until the temperature was so much increased. This would incline one to think, that the frozen part must have differed in some respect from the rest, so as to require much less cold to make it freeze; but yet I could not find that the strength of the decanted part differed sensibly from the rest.

It appeared by another bottle of oil of vitriol, which also froze by the natural cold of the air, that this acid, as well as the nitrous, contracts in freezing.

22. On December 21, when the weather was at -30°, the vitriolic acid N° 103, was diluted with snow, as directed in Art. 3. The snow dissolved immediately, and no signs of congelation appeared during any part of the process. The temperature

temperature of the acid rose only one degree before it began to sink, and the weight of the snow added was only  $\frac{r_0}{r_{2}}$  of that of the acid, so that its strength was reduced thereby to ,605; which is therefore the best degree of strength for producing cold by the addition of snow, when the degree of cold set out with is  $-30^{\circ}$ . This strength is one-sisteenth past less than what I sound myself, by a similar experiment, when the temperature of the acid was  $+27^{\circ}$ ; which shews, that the best degree of strength is rather less, when the degree of cold set out with is great than when small, but that it does not differ much.

- 23. The acid thus diluted was divided into two parts, and the next day Mr. M° NAB tried what degree of cold could be produced by adding fnow to one of them. The temperature of the air at the time was  $-39^{\circ}$ , and the mixture funk by the process to  $-55^{\circ}\frac{1}{2}$ . The snow dissolved readily, and the mixture did not lose much of its sluidity until it had acquired nearly its greatest degree of cold, nor did any congealed matter sink to the bottom in any part of the process. The quantity of snow added was about  $\frac{8}{100}$  of the weight of the acid, so that the strength of the mixture was about  $\frac{325}{100}$ .
- 24. On January 1, thin crystals of ice were found disfused all through this mixture, the temperature of the air being  $-51^{\circ}\frac{1}{2}$ , but that of the siquor was not tried. As this congelation must have been of the aqueous kind, and seems to have taken place at the temperature of  $-51^{\circ}\frac{1}{2}$ , it should follow, that this acid had no power of dissolving snow in a cold of  $51^{\circ}\frac{1}{2}$ ; so that it does not at first appear why a cold four degrees greater than that should have been produced in the foregoing experiment. The reason is, that at the time the mixture arrived at  $-55^{\circ}\frac{1}{2}$ , it appeared by the diminution of its sluidity to have contained

contained some undissolved snow, and some more was added to it after that time, which before the first of January dissolved and mixed with the acid; so that the acid in the mixture, at the time it sunk to  $-55^{\circ}\frac{1}{2}$ , was not quite so much diluted as that which froze on January 1. This is the reverse of what happened in the trial of the nitrous acid in Art. 15. as in that experiment the sluid part, at the time of the greatest cold, was weaker than the whole mixture together; but it must be considered, that that mixture contained much congealed acid, as well as undissolved snow, whereas this contained only the latter.

- 25. On January 1, fnow was added to the other half of the acid diluted on December 21. The cold produced was much greater than before, namely - 68° ; this feems to have proceeded, partly from the air and materials having been 12 degrees colder in this than in the former experiment, and partly from the fnow having been added faster, so that the mixture arrived at its greatest degree of cold in 20', whereas it before took up 46'. Another reason is, that the former mixture was made in too small a jar, in consequence of which it was poured into a larger before the experiment was completed, whereby fome cold was loft. The quantity of flow used in this experiment was less than in the former, so that the strength of the acid after the experiment was about ,343. The mixture also grew much thicker, and had a degree of elasticity resembling jelly; but whether this was owing only to more fnow remaining undiffolved, or to any other cause, I cannot tell.
- 26. Great as the foregoing degree of cold is, Mr. Mc NAB, on February 2, produced one much greater. In hopes of tobtaining a greater degree of cold by previously cooling the materials, he cooled about feven ounces of oil of vitriol, whose strength was ,629, that is, rather stronger than the foregoing,

by placing the jar in which it was contained in a freezing mixture of oil of vitriol and fnow; the fnow intended to be used was also cooled by placing it under the vessel in which the freezing mixture was made. As soon as the acid in the jar was cooled to the temperature of  $-57^{\circ}$ ; a little of the snow was added, on which it immediately began to freeze, and rose to  $-36^{\circ}$ ; but in about 40 minutes, as the jar was still kept in the freezing mixture, it sunk to  $-48^{\circ}$ ; by which time it was grown very thick and gritty, especially at bottom. More of the cooled snow was then added, which in a short time made it sink to  $-78^{\circ}$ ; and at the same time the thickness and tenacity of the mixture diminished; so that by the time it arrived at the greatest degree of cold, very little thickness remained.

It is worth inquiring, what was the reason of the greater degree of cold produced in this than in the preceding experiment? It could not be owing to the materials being colder; for at the time of the second addition of snow, at which time the experiment may be confidered to have begun, the acid was not colder than at the beginning of the preceding experiment, and the fnow in all probability not much colder. It could not be owing neither to the jar having been kept in the freezing mixture: for though that mixture was three or four degrees colder than the air in the preceding experiment, yet the acid in the jar, before it acquired much addition of cold, would be robbed of its cold faster by the mixture than it would by air of the same temperature as that in the preceding experiment. Neither could it proceed from any difference in the strength of the acid; for what difference there was must have done more hurt than good. The true reason is, that the acid was in a state of congelation: for as the congealed acid united to the fnow and became fluid by . the union, it is plain, that cold must have been produced both by the melting of the snow and by that of the acid; whereas, if the acid had been in a fluid state, cold would have been produced only by the first cause, and consequently a greater degree of cold should be produced in this experiment than in the former. The only inconvenience attending the acid being in a state of congelation is, that in all probability it does not unite to the snow so readily as when in a sluid state; but the difference seems not material, as the cold was produced, and the materials melted, in 5 minutes.

- 27. The day before, Mr. Mc NAB, by adding fnow to some of the same acid in the usual manner, when the cold of the materials was -46°, produced a cold of only -66°.
- 28. In these four last experiments the acid was reduced, by the addition of the snow, to the strengths of 325, 343, 403, and 334; and the cold produced in them was before said to be  $-55^{\circ}\frac{1}{2}$ ,  $-68^{\circ}\frac{1}{2}$ ,  $-78^{\circ}\frac{1}{2}$ , and  $-66^{\circ}$ ; whence we may conclude, that these are nearly the points of aqueous congelation answering to the foregoing strengths; only it appears, from what was said in Art. 24. that the strengths here set down are all of them rather too small.

Though it is certain that oil of vitriol is capable of the spirituous congelation, and though it appears, both from the foregoing experiments and from some made by the Duc D'AYEN\* and by M. DE MORVEAU; that it freezes with a less degree of cold when strong than when much diluted, it is not certain whether it has any point of easiest freezing, like spirit of nitre, or whether the cold required to freeze it does not continually diminish as the strength increases, without limitation; but the latter opinion is the most probable. For the Duc D'AYEN'S and

<sup>\*</sup> Diction. de Chym. par Macquer, 2de edit.

<sup>†</sup> Nouv. Mém. de l'Académ. de Dijon, 1782, 1er femestre, p. 68.

M. DE MORVEAU's acids, which, as they were concentrated on purpose, were most likely stronger than Mr. Mc NAB's, froze with a cold less than zero of FAHRENHEIT; whereas the freezing point of Mr. Mo NAB's undiluted acid, whose strength was ,98, was - 15°, and that of the diluted acid, whose strength was ,629, was - 36°; and when the acid was more diluted, it was found to bear a much greater cold without freezing. It appears also, both from Art. 21. and from M. DE Morve Au's experiment, that during the congelation of the oil of vitriol, tome separation of its parts takes place, so that the congealed part differs in some respect from the rest, in consequence of which it freezes with a less degree of cold; and as there is reason to think from Art. 21. that these two parts do not differ much in strength, it seems as if the difference between them depended on fome less obvious quality, and probably on that, whatever it is, which forms the difference between glacial and common oil of vitriol. The oil of vitriol prepared from green vitriol, has fometimes been obtained in such a state as to remain constantly congealed, except when exposed to a heat considerably greater than that of the atmosphere, whence it acquired its name of glacial \*. It is not known indeed upon what this property depends, but it is certainly fomething else than its strength; for oil of vitriol of this kind is always fmoking, and the fumes it emits are particularly oppreffive and fuffocating, though very different from those of the volatile fulphureous acid. On rectification likewise it yields, with the gentleft heat, a peculiar concrete substance, in the form of faline crystals; and after this volatile part has been driven off,

<sup>\*</sup> Mem. de l'Academ. des Sc. 1738, p. 288.

the remainder is no longer fmoking, and has lost its glacial quality \*.

### On the Mixture of Oil of Vitriol and Spirit of Nitre.

29. This mixture is not so fit for producing cold by the addition of snow, as oil of vitriol alone; for the cold obtained did not exceed  $-54^{\circ}\frac{1}{2}$ , in either of the experiments tried with it. The point of spirituous congelation of this mixture, when diluted with somewhat more than one-tenth of its weight of water, is about  $-20^{\circ}$ , and is much lower when the acid is confiderably more diluted: but as the Society will most likely have less curiosity about the disposition to freeze of this mixture than of the simple acids, I shall spare the particulars.

### On the Spirit of Wine.

- 30. The rectified spirits N° 8. were diluted with snow, in the same manner as the other liquors; but were found not to want any, as the first and only addition of snow produced cold. The quantity added was about  $\frac{3}{2.6}$  of the weight of the spirit.
- 31. The spirit thus diluted was divided, like the other liquors, into two parts, and each tried separately. The first was at  $-45^{\circ}$ , before the addition of the snow, and was sunk by the process to  $-56^{\circ}$ . The snow, even at the first addition, did not dissolve well, so that the spirit immediately

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<sup>\*</sup> CRELL'S Neu. Entdeck. in der Chemie, Th. 11. p. 100. Th. 12. p. 241, &c. and Annalen, 1785, St. 5. p. 438, &c.

became full of white spots \*, and grew thick by the time it arrived at its greatest degree of cold. After standing some hours, the mixture rose to the temperature of -39°, and was grown clear, but yet was not limpid, but of the consistence of syrup. No cold was produced by adding snow to it in that state, though it appeared that its point of aqueous congelation was at least 6 degrees lower than its temperature at that time †; which seems to shew that spirit of wine has scarce any power of dissolving snow when it wants even 6 degrees of its point of aqueous congelation, and therefore is another instance that snow is dissolved much less readily by spirit of wine than by the nitrous and vitriolic acids.

32. In trying the other part of the diluted spirits, the cold produced was only  $-47^{\circ\frac{1}{2}}$ , the cold set out with being  $-37^{\circ}$ .

33. It appeared by the diluted spirit of wine N° 143. which on December 12 froze by the natural cold of the atmosphere, and was treated in the same manner as the diluted spirit of nitre, that when highly rectified spirit of wine, such as N° 8. is diluted with 1.4 its weight of water, its point of aqueous congelation will be at -21°. The congealed part of the spirit was white like diluted milk, and even the decanted part, which was full of thin silms of ice, had a milky hue. The sluid part was stronger than the rest, and no increase of cold was produced by adding snow to some of it, both of which are marks of aqueous congelation.

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<sup>\*</sup> This was not the case during the above-mentioned dilution of the spirits; but the coldwas 16 degrees less in that experiment than in this.

<sup>†</sup> On account of the dilution which the spirits suffered by the melting of the show which remained undissolved at the time of the greatest cold, its point of aqueous congelation was no longer to low as  $-56^{\circ}$ ; but it till was not less than  $-45\frac{1}{2}$ , as in the evening it was found at that temperature, without much congealed matter in it.

. Though the foregoing experiments confirm the truth of what I faid, in the account of Mr. HUTCHINS's experiments. concerning the cause of the cold produced by mixing snow with different liquors, and intirely clear up the difficulty relating to it which I mentioned in Att. 1. yet feveral questions may naturally occur; fuch as, why the cold produced by the oil of vitriol was fo much greater than that obtained by the fpirit of nitre, notwithstanding that in warmer climates the nitrous acid feems to produce more cold? and why the cold produced by the nitrous acid, notwithstanding its previous dilution, which might naturally be expected to be of fervice, was not greater than has been obtained by other persons without that precaution? But as this would lead me into disquisitions of confiderable length, without my being able to fay any thing very fatisfactory on the subject, I shall forbear entering into it. I will only observe, that in most of the foregoing experiments, Mr. Mº NAB would probably have produced more cold, if he had added the snow faster. We ought not, however, to regret that he did not, as its effects on the acids would then have been less sensible.

The natural cold, when these experiments were made, is remarkable; as there were at least nine mornings in which the cold was not less than that of freezing mercury; four in which it was at least eight degrees below that point, or  $-47^{\circ}$ ; and one in which it was  $-50^{\circ}$ . Whereas out of nine winters, during which Mr. Hutchins observed the thermometer at Albany Fort, there were only twelve days in which the cold was equal to that of freezing mercury, and the greatest cold seems to have been  $-45^{\circ}$ . I cannot learn whether the last winter was more severe than usual at Hudson's Bay; or whether Henley-House is a colder situation than Albany, which

may perhaps be the case; forthough it is only 130 miles distant from it, yet it stands inland, and to the W. or S.W. of it, which is the quarter from which the coldest winds blow.

Mr. Mc NAB's original account of the experiments which furnished the materials of this Paper, having been thought too long to be printed in detail, is deposited in the Archives of the Society.

# PHILOSOPHICAL

# MSACTIONS.

OF THE

# ROYAL SOCIETY

OF

# L O N D O N

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PART II.



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## PHILOSOPHICAL

# TRANSACTIONS

XIV. New Experiments upon Heat. By Colonel Sir Benjamin Thompson, Knt. F. R.'S. In a Letter to Sir Joseph Banks, Bart. P. R. S.

### Read March 9, 1786.

DEAR SIR,

HAVE at length begun the course of experiments upon heat which I have so long had in contemplation; and I have already made a discovery, which, if not new to you, is perfectly so to me, and which I think may lead to a further knowledge respecting the nature of heat.

Vol. LXXVI.

O o

Examining

Examining the conducting power of air, and of various other fluid and folid bodies, with regard to heat, I was led to examine the conducting power of the Torricellian vacuum. From the striking analogy between the electric fluid and heat respecting their conductors and non-conductors (having found that bodies, in general, which are conductors of the electric fluid, are likewise good conductors of heat, and, on the contrary, that electric bodies, or such as are bad conductors of the electric fluid, are likewise bad conductors of heat), I was led to imagine that the Torricellian vacuum, which is known to afford so ready a passage to the electric fluid, would also have afforded a ready passage to heat.

The common experiments of heating and cooling bodies under the receiver of an air-pump I concluded inadequate to determining this question; not only on account of the impossibility of making a perfect void of air by means of the pump; but also on account of the moist vapour, which exhaling from the wet leather and the oil used in the machine, expands under the receiver, and fills it with a watery sluid, which, though extremely rare, is yet capable of conducting a great deal of heat: I had recourse therefore to other contrivances.

I took a thermometer, unfilled, the diameter of whose bulb (which was globular) was just half an inch, Paris measure, and fixed it in the center of a hollow glass ball of the diameter of 12 Paris inch, in such a manner, that the short neck or opening of the ball being soldered fast to the tube of the thermometer 7½ lines above its bulb, the bulb of the thermometer remained fixed in the center of the ball, and consequently was cut off from all communication with the external air. In the bottom of the glass ball was fixed a small hollow tube or point, which projecting outwards was soldered

to the end of a common barometer tube about 32 inches in length, and by means of this opening the space between the internal furface of the glass ball and the bulb of the thermometer was filled with hot mercury, which had been previously freed of air and moisture by boiling. The ball, and also the barometrical tube attached to it, being filled with mercury, the tube was carefully inverted, and its open end placed in a bowl in which there was a quantity of mercury. The instrument now became a barometer, and the mercury descending from the ball (which was now uppermost) left the space surrounding the bulb of the thermometer free of air. The mercury having totally quitted the glass ball, and having sunk in the tube to the height of 28 inches (being the height of the mercury in the common barometer at that time), with a lamp and a blow-pipe I melted the tube together, or fealed it hermetically, about three-quarters of an inch below the ball, and cutting it at this place with a fine file, I separated the ball from the long barometrical tube. The thermometer being afterwards filled with mercury in the common way, I now possessed a thermometer whose bulb was confined in the center of a Torricellian vacuum, and which served at the same time as the body to be heated, and as the instrument for measuring the heat communicated.

## Experiment Nº 1.

With this instrument (see fig. 1. Tab. VI.) I made the following experiment. Having plunged it into a vessel filled with water, warm to the 18th degree of REAUMUR'S scale, and suffered it to remain the retill it had acquired the temperature of the water, that is

to fay, till the mercury in the inclosed thermometer stood at 18°, I took it out of this vessel and plunged it suddenly into a vessel of boiling water, and holding it in the water (which was kept constantly boiling) by the end of the tube, in such a manner that the glass ball, in the center of which was the bulb of the thermometer, was just submerged, I observed the number of degrees to which the mercury in the thermometer had arisen at different periods of time, counted from the moment of its immersion. Thus, after it had remained in the boiling water 1 min. 30 sec. I found the mercury had risen from 18° to 27°. After 4 minutes had elapsed, it had risen to  $48^{\circ}_{10}$ ; and at the end of 5 minutes it had risen to  $48^{\circ}_{10}$ .

#### Experiment Nº 2.

Taking it now out of the boiling water I suffered it to cool gradually in the air, and after it had acquired the temperature of the atmosphere, which was that of 15° R. (the weather being perfectly fine), I broke off a little piece from the point of the small tube which remained at the bottom of the glass ball, where it had been hermetically sealed, and of course the atmospheric air rushed immediately into the ball. The ball furrounding the bulb of the thermometer being now filled with air (instead of being emptied of air, as it was in the beforementioned experiment), I re-fealed the end of the small tube at the bottom of the glass ball hermetically, and by that means cut off all communication between the air confined in the ball and the external air; and with the instrument so prepared I repeated the experiment before-mentioned; that is to fay, I put it into water warmed to 18°, and when it had acquired the temperature perature of the water, I plunged it into boiling water, and observed the times of the ascent of the mercury in the thermometer. They were as follows:

	Time elapfed.	Heat acquired.
Heat at the moment of being plunged into the boiling water,	}	18° R.
	M. S.	e
After having remained in the boiling water	0 45	27
	r c	34-4
	2 10	44-20
	2 40	48-2
	4	56 <sub>7°</sub> 5
	5	0 60 <del>10</del>

From the refult of these experiments it appears evidently, that the Torricellian vacuum, which affords so ready a passage to the electric sluid, so far from being a good conductor of heat, is a much worse one than common air, which of itself is reckoned among the worst: for in the last experiment, when the bulb of the thermometer was surrounded with air, and the instrument was plunged into boiling water, the mercury rose from 18° to 27° in 45 seconds; but in the former experiment, when it was surrounded by a Torricellian vacuum, it required to remain in the boiling water 1 minute 30 seconds = 90 seconds, to acquire that degree of heat. In the vacuum it required 5 minutes to rise to 48 '20; but in air it rose to that height in 2 minutes 40 seconds; and the proportion of the times in the other observations is nearly the same, as will appear by the following table.

The bulb of the thermometer placed in the

60-2-

	The bu	center of the	•	
	furrounded by a Torricellian vacuum.		furrounded by ai	
	(Exp	. N° 1.)	(Exp. N° 2.)	
	Time	Heat	Time	Heat
	elapfed.	acquired.	elapfed.	acquired.
Upon being plunged into boiling water	?}	. 18°		180
Dolling water	M. s.	9	M. S.	•
After remaining in it	1 30	27	0 45	27
_			1 0	30-14-
•	4 0	44-19-	2 10	44-3
	5 0	48,2	2 40	48,20
			4 0	56 <del>.2</del> ~
				-

These experiments were made at Manheim, upon the first day of July last, in the presence of Professor Hemmer, of the Electoral Academy of Sciences of Manheim, and Charles Artaria, Meteorological Instrument-maker to the Academy, by whom I was assisted.

Finding the construction of the instrument made use of in these experiments attended with much trouble and risque, on account of the difficulty of soldering the glass ball to the tube of the thermometer without at the same time either closing up, or otherwise injuring, the bore of the tube, I had recourse to another contrivance much more commodious, and much easier in the execution.

At the end of a glass tube or cylinder ten or eleven inches in length, and near three-quarters of an inch in diameter internally, I caused a hollow globe to be blown 1½ inch in diameter.

meter, with an opening in the bottom of it corresponding with the bore of the tube, and equal to it in diameter, leaving to the opening a neck or short tube, about an inch or threequarters of an inch in length. Having a thermometer prepared, whose bulb was just half an inch in diameter, and whose freezing point fell at about 24 inches above its bulb, I graduated its tube according to REAUMUR's scale, beginning at oo, and marking that point, and also every tenth degree above it to 80°, with threads of fine filk bound round it, which being moistened with lac varnish adhered firmly to the tube. This thermometer I introduced into the glass cylinder and globe just described, by the opening in the bottom of the globe, having first choaked the cylinder at about 2 inches from its junction with the globe by heating it, and crowding its fides inwards towards its axis, leaving only an opening fufficient to admit the tube of the thermometer. The thermometer being introduced into the cylinder in fuch a manner that the center of its bulb coincided with the center of the globe, I marked a place in the cylinder, about three-quarters of an inch above the 80th degree or boiling point upon the tube of the inclosed thermometer, and taking out the thermometer, I choaked the cylinder again in this place. Introducing now the thermometer for the last time, I closed the opening at the bottom of the globe at the lamp, taking care, before I brought it to the fire, to turn the cylinder upfide down, and to let the bulh of the thermometer fall into the cylinder till it refted upon the lower choak in the cylinder. By this means the bulb of the thermometer was removed more than 3 inches from the flame of the lamp. The opening at the bottom of the globe being now closed, and the bulb of the thermometer being suffered to return into the globe, the end of the cylinder was cut off to within 4

within about half an inch of the upper choak. This being done, it is plain, that the tube of the thermometer projected beyond the end of the cylinder. Taking hold of the end of the tube, I placed the bulb of the thermometer as nearly as possible in the center of the globe, and obscrving and marking a point in the tube immediately above the upper choak of the cylinder, I turned the cylinder upfide down, and fuffering the bulb of the thermometer to enter the cylinder, and rest upon the first or lower choak (by which means the end of the tube of the thermometer came further out of the cylinder), the end of the tube was cut off at the mark just mentioned (having first taken care to melt the internal cavity or bore of the tube together at that place), and a small solid ball of glass, a little larger than the internal diameter or opening of the choak, was soldered to the end of the tube, forming a little button or knob, which resting upon the upper choak of the cylinder, served to sufpend the thermometer in fuch a manner that the center of its bulb coincided with the center of the globe in which it was thut up. The end of the cylinder above the upper choak being now heated and drawn out to a point, or rather being formed into the figure of the frustum of a hollow cone, the end of it was foldered to the end of a barometrical tube, by the help of which the cavity of the cylinder and globe containing the thermometer was completely voided of air with mercury; when, the end of the cylinder being hermetically scaled, the barometrical tube was detached from it with a file, and the thermometer was left completely shut up in a Torricellian vacuum, the center of the bulb of the thermometer being confined in the center of the glass globe, without touching it in any part, by means of the two choaks in the cylinder, and the button upon the end of the tube.

Of these instruments I provided myself with two, as nearly as possible of the same dimensions; the one, which I shall call N° 1. being voided of air, in the manner above described; the other, N° 2. being filled with air, and hermetically sealed.

With these two instruments (see fig. 2.) I made the following experiments upon the 11th of July last, at Manheim, between the hours of ten and twelve, the weather being very fine and clear, the mercury in the barometer standing at 27 inches 11 lines, Reaumur's thermometer at 15°, and the quill hygrometer of the Academy of Manheim at 47°.

### Experiments N° 3, 4, 5 and 6.

Putting both the instruments into melting ice, I let them remain there till the mercury in the inclosed thermometers rested at the point o°, that is to say, till they had acquired exactly the temperature of freezing water or melting ice; and then taking them out of the ice I plunged them suddenly into a large vessel of boiling water, and observed the time required for the mercury to rise in the thermometers from ten degrees to ten degrees, from o° to 80°, taking care to keep the water constantly boiling during the whole of this time, and taking care also to keep the instruments immersed to the same depth, that is to say, just so deep that the point o° of the inclosed thermometer was even with the surface of the water.

These experiments I repeated twice, with the utmost care; and the following table gives the result of them.

Its bulb half an inch in diameter, shut up in the center of a hollow glass globe, 1½ inch in diameter, void of air, and hermetically scaled.  Taken out of freezing water, and plunged into boiling water.  Time elapsed.  Exp. N° 3. Exp. N° 4.  Heat acquired.  Time elapsed.  M. S. M. S. O 51 O 51 O 51 O 59 O 59 O 59 O 59 O 59	Thermometer Nº	1 bermoncter N° 2.			
of a hollow glass globe, 1½ inch in diameter, void of air, and hermetically scaled.  Taken out of freezing water, and plunged into boiling water, and plunged into boiling water.  Time elapsed.    Heat   Exp. N° 3.   Exp. N° 4.   Heat   acquired.   Exp. N° 5.   Exp. N° 6.   O° 0° 0° 0° 0° 0° 0° 0° 0° 0° 0° 0° 0° 0°	Its bulb half an incl	Its bulb half an inch in dia-			
inch in diameter, void of air, and hermetically scaled.  Taken out of freezing water, and plunged into boiling water.  Time elapsed.    Heat   Exp. N° 3.   Exp. N° 4.	meter, shut up in the	e center	meter, thu	it up in th	e center
and hermetically scaled.  Taken out of freezing water, and plunged into boiling water.  Time elapsed.  Heat acquired.    Heat Exp. N° 3.   Exp. N° 4.   Heat acquired.   Exp. N° 5.   Exp. N° 6.   O° M. S. M. S. O. O. O. O°	of a hollow glass gl	obe, I ½	of a holl	ow glais g	lobe, $1\frac{1}{2}$
Taken out of freezing water, and plunged into boiling water.  Time elapsed.    Heat   Exp. N° 3.   Exp. N° 4.   Heat   Exp. N° 5.   Exp. N° 6.   Heat   acquired.   Exp. N° 5.   Exp. N° 6.   Heat   acquired.   Exp. N° 5.   Exp. N° 6.   Heat   acquired.   Exp. N° 5.   Exp. N° 6.   O° M. S. M. S. O° SO° O° O° M. S. M. S. O° SO° O° O			inch in d	liameter, fil	led with
Time elapsed.   Heat   Exp. N° 3.   Exp. N° 4.   Heat   Exp. N° 5.   Exp. N° 6.   Acquired.   Exp. N° 5.   Exp. N° 6.   Heat   Exp. N° 5.   Exp. N° 6.					
Time elapsed.    Heat   Exp. N° 3.   Exp. N° 4.	Taken out of freezing	g water,	Taken or	ut of freezin	ig water,
Exp. N° 3. Exp. N° 4.   acquired.   Exp. N° 5. Exp. N° 6.   acquired.      N° 8.   M. S.   O 51   10   O 30   O 30   10	and plunged into boiling	water.	and plunge	d into boiling	g water.
Exp. N° 3.   Exp. N° 4.	Time elapfed.	Heat	Time	elapfed.	
M. S. M. S. O 51 10 O 30 O 30 10  O 59 O 59 20 O 35 O 37 20  I I I I 2 30 O 41 O 41 30  I 18 I 22 40 O 49 O 53 40  I 24 I 23 50 I I O 59 50  2 O I 51 60 I 24 I 20 60  3 30 3 6 70 2 45 2 25 70  II 41 10 27 80 9 10 9 38 60   22 44 21 I = total time of heating from 0° to 80°.  Total time from 0° to 70°:  M. S.  M. S. M. S. O N.	Exp. N° 3. Exp. N° 4.	acquired.	Exp. N' 5.	Exp. N' 6.	acquired.
M. S. M. S. O 51 10 O 30 O 30 10  O 59 O 59 20 O 35 O 37 20  I I I I 2 30 O 41 O 41 30  I 18 I 22 40 O 49 O 53 40  I 24 I 23 50 I I O 59 50  2 O I 51 60 I 24 I 20 60  3 30 3 6 70 2 45 2 25 70  II 41 10 27 80 9 10 9 38 60   22 44 21 I = total time of heating from 0° to 80°.  Total time from 0° to 70°:  M. S.  M. S. M. S. O N.		o°			o°
0 59 0 59 20 0 35 0 37 20  1 1 1 2 30 0 41 0 41 30  1 18 1 22 40 0 49 0 53 40  1 24 1 23 50 1 1 0 59 50  2 0 1 51 60 1 24 1 20 60  3 30 3 6 70 2 45 2 25 70  11 41 10 27 80 9 10 9 38 60  22 44 21 1 = total time of heating from 0° to 80°.  Total time from 0° to 70°:  M. S.  Total time from 0° to 70°:  M. S.	M. S. M. S.		M. S.	M. S.	t t
0 59 0 59 20 0 35 0 37 20  1 1 1 2 30 0 41 0 41 30  1 18 1 22 40 0 49 0 53 40  1 24 1 23 50 1 1 0 59 50  2 0 1 51 60 1 24 1 20 60  3 30 3 6 70 2 45 2 25 70  11 41 10 27 80 9 10 9 38 60  22 44 21 1 = total time of heating from 0° to 80°.  Total time from 0° to 70°:  M. S.  Total time from 0° to 70°:  M. S.	0 51 0 51	10	0 30	0 30	10
1 I I 2 30 0 41 0 41 30 1 18 1 22 40 0 49 0 53 40 1 24 I 23 50 I I 0 59 50 2 0 I 5I 60 I 24 I 20 60 3 30 3 6 70 2 45 2 25 70 11 41 10 27 80 9 10 9 38 co  22 44 21 I = total time of heating from 0° to 80°.  Total time from 0° to 70°: M. S.  Total time from 0° to 70°: M. S.	1	20	0 35	° 37	20
1 24       1 23       50       1 1       0 59       50         2 0 1 51       60       1 24       1 20       60         3 30       3 6       70       2 45       2 25       70         11 41       10 27       80       9 10       9 38       80         22 44       21 1 = total time       16 55       17 3 = total time         of heating from 0° to 80°.       Total time from 0° to 80°.       Total time from 0° to 70°:         M. S.       M. S.	1 I I 2	30	0 41		30
2 0 1 51 60 1 24 1 20 60  3 30 3 6 70 2 45 2 25 70  11 41 10 27 80 9 10 9 38 60  22 44 21 1 = total time of heating from 0° to 80°.  Total time from 0° to 70°:  M. S.  Total time from 0° to 70°:  M. S.	1 18 1 22	40	0 49	0 53	40
3 30 3 6 70 2 45 2 25 70  11 41 10 27 80 9 10 9 38 80  22 44 21 1 = total time of heating from 0° to 80°.  Total time from 0° to 70°:  M. S.  Total time from 0° to 70°:  M. S.	1 24 1 23	₩.	II		
11 41 10 27 80 9 10 9 38 60  22 44 21 1 = total time of heating from 0° to 80°.  Total time from 0° to 70°:  M. S.  Total time from 0° to 70°:  M. S.		65	1		
22 44 21 1=total time 16 55 17 3=total time of heating from 0° to 80°.  Total time from 0° to 70°:  M. S.  Total time from 0° to 70°:  M. S.	3 30 3 6	70		77	
of heating from 0° to 80°.  Total time from 0° to 70°:  M. S.  Total time from 0° to 70°:  M. S.	11 41 10 27	80	9 10	, 9 38	60
of heating from 0° to 80°.  Total time from 0° to 70°:  M. S.  of heating from 0° to 80°.  Total time from 0° to 70°:  M. S.	22 44 21 I=t	16 55	17 3=1	total time	
Total time from 0° to 70°: Total time from 0° to 70°: M. S.			of heatin	g from o° t	0 807.
M. Ś. M. Ś.	Total time from 0° to 70°:				
In Evn N° $a = 11$ 2   In Exn. N° $a = 7.45$	M. S.			j	M. S.
	In Exp. N° $3. = 11$ 3		In Exp. N° $5.=745$		
In Exp. N° 4. = 10, 34 In Exp. N° 6. = 7 25	In Exp. N° 4. = 10, 34		In E	$p. N^{\circ} 6. =$	7 25
Medium = $10  48\frac{1}{2}$ Medium = $7  35$	Medium = I	0 48 =		Medium =	7 35

It appears from these experiments, that the conducting power of air to that of the Torricellian vacuum, under the circumstances described, is as 7 3 5 to 10 485 inversely, or as 1000 to 702 nearly; for the quantities of heat communicated being 4 equal,

equal, the intensity of the communication is as the times inversely.

In these experiments the heat passed through the surrounding medium into the bulb of the thermometer: in order to reverse the experiment, and make the heat pass out of the thermometer, I put the instruments into boiling water, and let them remain therein till they had acquired the temperature of the water, that is to say, till the mercury in the inclosed thermometers stood at 80°; and then, taking them out of the boiling water, I plunged them suddenly into a mixture of water and pounded ice, and moving them about continually in this mixture, I observed the times employed in cooling as follows.

Thermometer N° 1.  Surrounded by a Torricellian vacuum.  Taken out of boiling water, and plunged into freezing water.		Thermonneter N° 2.  Surrounded by air.  Taken out of boiling water, and plunged into freezing water.		
Time elapsed.  Exp. N° 7. Exp. N° 8. Heat lost.		Time elapsed.  Exp. N° 9. Exp. N° 10.		Heat lost.
M. S. M. S.  1 2 0 54 0 58 1 2 1 17 1 18 1 46 1 37 2 5 2 16 3 14 3 10 5 42 5 59 Not observed. Not observe	80° 70 60 50 40 30 20 10	M. S.  0 33  0 39  0 44  0 55  1 17  1 57  3 44  40 10	M. S.  0 33  0 34  0 44  0 55  1 18  1 57  3 40  Not observed.	80° 70 60 50 40 30 20 10
Total time of cooling from  In Exp. N° 7.=1  In Exp. N° 8.=16  Medium=16	In E	of cooling from  Exp. N° 9. = 9  Exp. N° 10. = 9  Medium = 9	49 41	

By these experiments it appears, that the conducting power of air is to that of the Torricellian vacuum as  $9\frac{4}{5}$  to  $16\frac{1}{5}$  inversely, or as 1000 to 603.

To determine whether the same law would hold good when the heated thermometers, instead of being plunged into freezing water, were suffered to cool in the open air, I made the following experiments. The thermometers N° 1. and N° 2. being again heated in boiling water, as in the last experiments, I took them out of the water, and suspended them in the middle of a large room, where the air (which appeared to be perfectly at rest, the windows and doors being all shut) was warm to the 16th degree of REAUMUR's thermometer, and the times of cooling were observed as follows.

(Exp. N° 11.)  Thermometer N° 1.  Surrounded by a Torricellian vacuum.  Heated to 80°, and suspended in the open arr warm to 16°.	(Exp. N° 12.)  Thermometer N° 2.  Surrounded by air.  Heated to 80°, and suspended in the openair warm to 16°.
Time clapfed. Heat loft.	Time elapsed. Heat lost.  80°  M. S. 0  Not observed. 70  0 51 60  1 5 50  1 34 40  2 41 30
10 12=total time employed n cooling from 70' to 30'.	6 11=total time employed in cooling from 70° to 30°.

Here the difference in the conducting powers of air and of the Torricellian vacuum appears to be nearly the same as in the foregoing experiments, being as  $6\frac{17}{60}$  to  $10\frac{12}{60}$  inversely, or 15 1000 to 605. I could not observe the time of cooling from

80° to 70°, being at that time busied in suspending the instruments.

As it might possibly be objected to the conclusions drawn from these experiments that, notwithstanding all the care that was taken in the constructing of the two instruments made use of that they should be perfectly alike, yet they might in reality be so far different, either in shape or size, as to occasion a very sensible error in the result of the experiments; to remove these doubts I made the following experiments.

In the morning towards eleven o'clock, the weather being remarkably fine, the mercury in the barometer standing at 27 inches 11 lines, Reaumur's thermometer at 15°, and the hygrometer at 47°, I repeated the experiment N° 3. (of heating the thermometer N° 1. in boiling water, &c.) and immediately afterwards opening the cylinder containing the thermometer at its upper end, where it had been sealed, and letting the air into it, I re-sealed it hermetically, and repeated the experiment again with the same instrument, the thermometer being now surrounded with air, like the thermometer N° 2.

The refult of these experiments, which may be seen in the following table, shews evidently, that the error arising from the difference of the shapes or dimensions of the two instruments in question was inconsiderable, if not totally imperceptible.

(Exp.	Nº	13.)	
Thermon	<i>ieter</i>	N	

Its bulb half an inch in diameter shut up in the center of a glass globe 1½ inch in diameter, voided of air, and hermetically sealed.

Taken out of freezing water, and plunged into boiling water.

Time elapsed. Heat acquired.

C	o° :
S. ,	•
5 10	)
7 3°	)
5 40	<b>)</b>
50 50	)
2 6	၁
21 7	0
14 E	)
0 4.4.1	ina of
$\mu_{\Omega} = total$	time of
om oo to 8c	)°•
e from o°	to 70°=
	5. 10 5. 20 7. 30 5. 40 9. 50 2. 60 2.1 7.

(Exp. N° 14.)
The fame Thermometer (N° 1.)
The glass globe, containing the bulb of the thermometer, being now filled with air, and hermetically scaled.

Taken out of freezing water, and plunged into boiling water.

Time elapfed.	Heat acquired.
M. S.	0
0 32	10
0 32	20
0 43	30
0 50	30 40 50 60
1 1,	50
I 24	60
2 38	
10 25	70 * 80
0	Askal dimes a

18 5 = total time of heating from 0° to 80°.

Total time from 0° to 70° = 7′ 40″.

It appears, therefore, from these experiments, that the conducting power of common atmospheric air is to that of the Torricellian vacuum as 7000 to 1140 inversely, or as 1000 to 602; which differs but very little from the result of all the foregoing experiments.

Notwithstanding that it appeared, from the result of these last experiments, that any difference there might possibly have been in the proportions or dimensions of the instruments N° 1. and N° 2. could hardly have produced any sensible error

in the refult of the experiments in question; I was willing, however, to see how far any considerable alterations of size in the instrument would affect the experiment: I therefore provided myself with another instrument, which I shall call Thermometer N° 3. different from those already described in size, and a little different in its construction.

The bulb of the thermometer was of the fame form and fize as in the inftruments  $N^{\circ}$  1. and  $N^{\circ}$  2. that is to fay, it was globular, and half an inch in diameter; but the glass globe, in the center of which it was confined, was much larger, being 3 inches 7½ lines in diameter; and the bore of the tube of the thermometer was much finer, and consequently its length, and the divisions of its scale, were greater. The divisions were marked upon the tube with threads of filk of different colours at every tenth degree, from oo to 800, as in the before-mentioned instruments. The tube or cylinder belonging to the glass globe was 8 lines in diameter, a little longer than the tube of the thermometer, and perfectly cylindrical from its upper end to its junction with the globe, being without any choak; the thermometer being confined in the center of the globe by a different contrivance, which was as follows. To the opening of the cylinder was fitted a stopple of dry wood, covered with a coat of hard varnish, through the center or axis of which passed the end of the tube of the thermometer: this confined the tube in the axis of the cylinder at its upper end. To confine it at its lower end, there was fitted to it a fmall fteel fpring, a little below the point oo; which, being confined round the tube of the thermometer, had three elastic points projecting outwards, which preffing against the infide of the cylinder, confined the thermometer in its place. The total length of this instrument, from the bottom of the globe

to the upper end of the cylinder, was 18 inches, and the freezing point upon the thermometer fell about 3 inches above the bulb; consequently it lay about 11 inch above the junction of the cylinder with the globe, when the thermometer was confined in its place, the center of its bulb coinciding with the center of the globe. Through the stopple which closed the end of the cylinder passed two finall glass tubes, about a line in diameter, which being about a line longer than the stopple were stopped up occasionally with small stopples sitted to their These tubes (which were fitted exactly in the holes bored in the great stopple of the cylinder to receive them, and fixed in their places with cement) ferved to convey air, or any other fluid, into the glass ball, without being under a necessity of removing the stopple closing the end of the cylinder; which, in order to prevent the position of the thermometer from being eafily deranged, was cemented in its place.

I have been the more particular in the description of these instruments, as I conceive it absolutely necessary to have a perfect idea of them in order to judge of the experiments made with them.

With the inftrument last described (which I have called Thermometer N° 3.) I made the following experiment. It was upon the 18th of July last, in the afternoon, the weather variable, alternate clouds and sun-shine; wind strong at S.E. with now and then a sprinkling of rain; barometer at 27 inches 10½ lines, thermometer at 18°¼, and hygrometer variable from 44° to extreme moisture.

In order to compare the refult of the experiment made with this thermometer with those made with the thermometer N° 2. I have, in the following table, placed these experiments by the side of each other.

(Exp.

meter, shut up a glass tube, 3 in diameter, an air.	an inch in dia- in the center of inches $7\frac{1}{2}$ lines d furrounded by	Its bulb he the center meter, and	Exp. N 4. a Thermomete alf an inch is of a glass gl surrounded b f freezing av boiling av	r $N^{\circ}$ 2.  In diameter,  lobe, $I^{\perp}_{2}$ income y air.  Nater, and p	h in dia-
plunged into be	eezing water, and orling water.		Time elapfed	*	Heat
Time elapsed.	Heat acquired.	Exp. N° 4.	Exp. N- 5.	Medium.	acquired.
	ဝ°		,		೦
M. S.	0	M. S.	M. S.	M. S.	•
0 33	10	0 30	0 30	0 30	10
0 38	20	0 35	o 37	O 36	20
0 54	30	0 41	0 41	0 41	30
0 51	40	0 49	0 53	0 51	40
I 7	50	II	0 59	1 0	50
1 28	60	I 24	1 20	I 22	60
2 28	70	2 45	2 25	2 35	70
90	8o	9 10	938	9 24	80
16 59 =	total time of or to 80° to 70° = 7′ 59″.	16 55 time of her	17 3 ating from 0° me from 0° t	' to 80°.	= total

If the agreement of these experiments with the thermometers N° 2. and N° 3. surprised me, I was not less surprised with their disagreement in the experiment which follows.

### Experiment Nº 16.

Taking the thermometer N° 3. out of the boiling water, I immediately suspended it in the middle of a large room, where the air, which was quiet, had the temperature of 18° IR. and observed the times of cooling as follows:

Time	elapíed.	Heat lost.
	<del></del>	8၀°
M.	S.	
I	5 <i>5</i>	70
٥	I 2	60
0	33	50
2	15	40
4	0	30

9 55 = total time of cooling from 80° to 30°.

Time from 70° to  $30^{\circ} = 8'$  o"; but in the experiment N° 12. with the thermometer N° 2. the time employed in cooling from 70° to 30° was only 6' 11". In this experiment, with the thermometer N° 3. the time employed in cooling from 60° to 30° was 7' 48"; but in the above-mentioned experiment, with the thermometer N° 2. it was only 5' 20". It is true, the air of the room was somewhat cooler when the former experiment was made than when this latter was made with the thermometer N° 3.; but this difference of temperature, which was only  $2^{\circ}\frac{1}{4}$  (in the former case the thermometer in the room standing at 16°, and in the latter at  $18^{\circ}\frac{1}{4}$ ) certainly could not have occasioned the whole of the apparent difference in the results of the experiments.

Does air receive heat more readily than it parts with it? This is a question highly deserving of further investigation, and I shall not fail to give it a full examination in the course of my projected inquiries; but leaving it for the present, I shall proceed to give an account of the experiments which I have already made \*.

It

<sup>\*</sup> Conceiving it to be a step of considerable importance towards coming at a further

It having been my intention from the beginning to examine the conducting powers of the artificial airs or gaffes, the thermometer

further knowledge of the nature of heat, to ascertain, by indisputable evidence, its passage through the Torricellian vacuum, and to determine, with as much precision as possible, the law of its motions in that medium; and being apprehensive that doubts might arise with respect to the experiments before described, on account of the contact of the tubes of the inclosed thermometers in the instruments made use of with the containing glass globes, or rather with their cylinders; by which means it might be suspected, that a certain quantity, if not all the heat acquired, might possibly be communicated: to put this matter beyond all doubt, I made the following experiment.

In the middle of a glass body, of a pear-like form, about 8 inches long, and  $2\frac{1}{2}$  inches in its greatest diameter, I suspended a small mercurial thermometer,  $5\frac{1}{2}$ inches long, by a fine thread of filk, in fuch a manner that neither the bulb of the thermometer, nor its tube, touched the containing glass body in any part. The tube of the thermometer was graduated, and marked with fine threads of filk of different colours bound round it, as in the thermometers belonging to the other instruments already described; and the thermometer was suspended in its place by means of a small steel spring, to which the end of the thread of silk which held the thermometer being attached, it (the fpring) was forced into a fmall globular protuberance or cavity, blown in the upper extremity of the glass body, about half an inch in diameter, where the spring remaining, the thermometer necessarily remained suspended in the axis of the glass body. There was an opening at the bottom of the glass body, through which the thermometer was introduced; and a barometrical tube being foldered to this opening, the infide of the glass body was voided of air by means of mercury; and this opening being afterwards sealed hermetically, and the barometrical tube being taken away, the thermometer was left suspended in a Torricellian vacuum.

In this infimument, as the inclosed thermometer did not touch the containing glass body in any part, on the contrary, being distant from its internal surface an inch or more in every part, it is clear, that whatever heat passed into or out of the thermometer must have passed through the surrounding Torricellian vacuum: for it cannot be supposed, that the fine thread of filk, by which the thermometer was suspended, was capable of conducting any heat at all, or at least any sensible quantity. I therefore flattered myself with hopes of being able, with the

thermometer N° 3. was constructed with a view to those expetiments; and having now provided myself with a stock of those different kinds of airs, I began with fixed air, with which, by

affishance of this instrument, to determine positively with regard to the passage of heat in the Torricellian vacuum: and this, I think, I have done, notwithstanding that an unfortunate accident put it out of my power to pursue the experiments so far as I intended.

This inftrument being fitted to a small stand or foot of wood, in such a manner that the glass body remained in a perpendicular situation, I placed it in my room, by the side of another inclosed thermometer (N° 2.), which was surrounded by air, and observed the effect of the variation of heat in the atmosphere. I soon discovered, by the motion of the mercury in the inclosed thermometer, that the heat passed through the Torricellian vacuum; but it appeared plainly from the sluggishness or great insensibility of the thermometer, that the heat passed with much greater difficulty in this medium than in common air. I now plunged both the thermometers into a bucket of cold water; and I observed that the mercury in the thermometer surrounded by air descended much faster than that in the thermometer surrounded by the Torricellian vacuum. I took them out of the cold water, and plunged them into a vessel of hot water (having no conveniencies at hand to repeat the experiment in form with the freezing and with the boiling water); and the thermometer surrounded by the Torricellian vacuum appeared still to be much more insensible or sluggish than that surrounded by air.

These trials were quite sufficient to convince me of the passage of heat in the Torricellian vacuum, and also of the greater difficulty of its passage in that medium than in common air; but, not satisfied to rest my inquiries here, I took the first opportunity that offered, and set myself to repeat the experiments which I had before made with the instruments N° 1. and N° 2. I plunged this instrument into freezing water, where I let it remain till the mercury in the inclosed thermometer had descended to 0°; when, taking it out of the freezing water, I plunged it suddenly into a vessel of boiling water, and prepared myself to observe the ascent of the mercury in the inclosed thermometer as in the foregoing experiments; but unfortunately the moment the end of the glass body touched the boiling water, it cracked with the heat at the point where it had been hermetically sealed, and the water rushing into the body, spoiled the experiment: and I have not since had an opportunity of providing myself with another instrument to repeat it.

means of water, I filled the globe and cylinder containing the thermometer; and stopping up the two holes in the great stopple closing the end of the cylinder, I exposed the instrument in freezing water till the mercury in the inclosed thermometer had descended to oo; when, taking it out of the freezing water, I plunged it into a large vessel of boiling water, and prepared myself to observe the times of heating, as in the former cases; but an accident happened, which fuddenly put a stop to the experiment. Immediately upon plunging the instrument into the boiling water, the mercury began to rife in the thermometer with fuch uncommon celerity, that it had paffed the first divifion upon the tube (which marked the 10th degree, according to REAUMUR's scale) before I was aware of its being yet in motion; and having thus missed the opportunity of observing the time elapsed when the mercury arrived at that point, I was preparing to observe its passage of the next, when all of a fudden the stopple closing the end of the cylinder was blown up the chimney with a great explosion, and the thermometer, which, being cemented to it by its tube, was taken along with it. and was broken to pieces, and destroyed in its fall.

This unfortunate experiment, though it put a stop for the time to the inquiries proposed, opened the way to other refearches not less interesting. Suspecting that the explosion was occasioned by the rarefaction of the water which remained attached to the inside of the globe and cylinder after the operation of filling them with fixed air; and thinking it more than probable, that the uncommon celerity, with which the mercury rose in the thermometer, was principally owing to the same cause; I was led to examine the conducting power of moist air, or air saturated with water.

For this experiment, I provided myself with a new thermometer N° 4. the bulb of which, being of the same form as those already described (viz. globular) was also of the same size. or half an inch in diameter. To receive this thermometer a glass cylinder was provided, 8 lines in diameter, and about 14 inches long, and terminated at one end by a globe 11 inch in diameter. In the center of this globe the bulb of the thermometer was confined, by means of the stopple which closed the end of the cylinder; which stopple, being near 2 inches long, received the end of the tube of the thermometer into a hole bored through its center or axis, and confined the thermometer in its place, without the affistance of any other apparatus. Through this stopple two other small holes were bored, and lined with thin glass tubes, as in the thermometer N° 3. opening a pasfage into the cylinder, which holes were occasionally stopped up with some stopples of cork; but to prevent accidents, such as I had before experienced from an explosion, great care was taken not to press these stopples into their places with any confiderable force, that they might the more eafily be blown out by any confiderable effort of the confined air.

Though in this instrument the thermometer was not altogether so steady in its place as in the thermometers N° 1. N° 2. and N° 3. the elasticity of the tube, and the weight of the mercury in the bulb of the thermometer, occasioning a small vibration or trembling of the thermometer upon any sudden motion or jar; yet I preferred this method to the others, on account of the lower part of this thermometer being intirely free, or suspended in such a manner as not to touch, or have any communication with, the lower part of the cylinder or the globe: for though the quantity of heat received by the tube of the thermometer at its contact with the cylinder at its choaks.

choaks, in the inftruments N° 1. and N° 2. or with the branches of the fteel spring in N° 3. and from thence communicated to the bulb, must have been exceedingly small; yet I was desirous to prevent even that, and every other possible error or inaccuracy, however small, that might arise.

Does humidity augment the conducting power of air?

To determine this question I made the following experiments, the weather being clear and fine, the mercury in the barometer standing at 27 inches 8 lines, the thermometer at 19°, and the hygrometer at 44°.

(Exp. N° 17.)  Thermometer N° 4.  Surrounded by air dry to the 44th degree of the quill hygrometer of the Manheim Academy.  Taken out of freezing water, and plunged into boiling water.	(Exp. N° 18.) The fume thermometer (N° 4.) Surrounded by air rendered as moist as possible by wetting the inside of the cylinder and globe with water. Taken out of freezing water, and plunged into boiling water.
Time elapsed. Heat acquired.	Time elapsed. Heat acquired.  O  M. S. O  O  O  O  O  O  O  O  O  O  O  O  O

From these experiments it appears, that the conducting power of air is very much increased by humidity. To see if the same result would obtain when the experiment was reversed, I now took the thermometer with the moist air out of the boiling water, and plunged it into freezing water; and moving it about continually from place to place in the freezing water, I observed the times of cooling, as set down in the following table. N. B. To compare the result of this experiment with those made with dry air, I have placed on one side in the following table the experiment in question, and on the other side the experiment N° 19. made with the thermometer N° 2.

(Exp. N° 19.)  Thermometer N° 4.  Surrounded by moist air.  Taken out of boiling water,  and plunged into freezing water.	(Exp. N° 10.)  Thermometer N° 2.  Surrounded by dry air.  Taken out of boiling water, and plunged into freezing water.
Time elapsed. Heat lost.	Time elapfed. Heat loft.
M. S. 70	o 33 7°
0 14 60 0 31 50	0 44 50
0 52 40 1 22 30	0 55 40 1 18 30
2 3 20 4 2 10	1 57 20 3 40 10
$\frac{1}{9.8}$ = total time of	$\frac{3}{9} \frac{12}{12} = \text{total time of}$
cooling from 80- to 10°.	cooling from 80° to 10°.

Though the difference of the whole times of cooling from 80° to 10° in these two experiments appears to have been very

small, yet the difference of the times taken up by the first twenty or thirty degrees from the boiling point is very remarkable, and shows with how much greater facility heat passes in moist air than in dry air. Even the slowness with which the mercury in the thermometer N° 4. descended in this experiment from the 30th to the 20th, and from the 20th to the 10th degree, I attribute in some measure to the great conducting power of the moist air with which it was furrounded; for the cylinder containing the thermometer and the moist air, being not wholly submerged in the freezing water, that part of it which remained out of the water was necessarily furrounded by the air of the atmosphere; which being much warmer than the water, communicated of its heat to the glass; which, passing from thence into the contained moist air as foon as that air became colder than the external air, was, through that medium, communicated to the bulb of the inclosed thermometer, which prevented its cooling so fast as it would otherwife have done. But when the weather becomes cold, I propose to repeat this experiment with variations, in fuch a manner as to put the matter beyond all doubt. In the mean time I cannot help observing, with what infinite wisdom and goodness Divine Providence appears to have guarded us against the evil effects of excessive heat and cold in the atmofphere; for if it were possible for the air to be equally damp during the severe cold of the winter months as it sometimes is in summer, its conducting power, and consequently its apparent coldness, when applied to our bodies, would be so much increased, by such an additional degree of moisture, that it would become quite intolerable; but, happily for us, its power to hold water in solution is diminished, and with it its power to rob us of our animal heat, in proportion as its coldness Rr VOL. LXXVI.

coldness is increased. Every body knows how very disagreeable a very moderate degree of cold is when the air is very damp; and from hence it appears, why the thermometer is not always a just measure of the apparent or sensible heat of the atmosphere. If colds or catarrhs are occasioned by our bodies being robbed of our animal heat, the reason is plain why those diforders prevail most during the cold autumnal rains, and upon the breaking up of the frost in the spring. It is likewise plain from whence it is that fleeping in damp beds, and inhabiting damp houses, is so very dangerous; and why the evening air is fo pernicious in fummer and in autumn, and why it is not fo during the hard frosts of winter. It has puzzled many very able philosophers and physicians to account for the manner in which the extraordinary degree or rather quantity of heat is generated which an animal body is supposed to lose, when exposed to the cold of winter, above what it communicates to the furrounding atmosphere in warm fummer weather; but is it not more than probable, that the difference of the quantities of heat, actually lost or communicated, is infinitely less than what they have imagined? These inquiries are certainly very interesting; and they are undoubtedly within the reach of well contrived and well conducted experiments. But taking my leave for the present of this curious subject of investigation. I hasten to the sequel of my experiments.

Finding so great a difference in the conducting powers of common air and of the Torricellian vacuum, I was led to examine the conducting powers of common air of different degrees of density. For this experiment I prepared the thermometer N° 4. by stopping up one of the small glass tubes passing through the stopple, and opening a passage into the cylinder, and by sitting a valve to the external overture of the other.

other. The instrument, thus prepared, being put under the receiver of an air-pump, the air passed freely out of the globe and cylinder upon working the machine, but the valve above described prevented its return upon letting air into the receiver. The gage of the air-pump showed the degree of rarity of the air under the receiver, and consequently of that filling the globe and cylinder, and immediately surrounding the thermometer.

With this instrument, the weather being clear and fine, the mercury in the barometer standing at 27 inches 9 lines, the thermometer at 15°, and the hygrometer at 47°, I made the following experiments.

Surrounded by common air, barometer standing at 27 inches 9 lines.  Taken out of freezing wa-	fied by pumping till the barometer-gage stood at 6 inches 11½ lines.	Surrounded by air rare- fied by pumping till the barometer-gage stood at t inch 2 lines.  Taken out of freezing wa
Time Heat elapsed. acquired.  O° M. S. o 0 31 10 0 40 20 0 41 30 0 47 40 1 4 50 1 25 60 2 28 70 10 17 80  7 36 = total time of heating from 0° to 70°.	Time Heat elapsed. acquired.  O°  M. S.  0 31 10 0 38 20 0 44 30 0 51 40 1 7 50 1 19 60 2 27 70 10 21 80  7 37 = total time of heating from 0° to 70°.	Time Heat elapsed. acquired.  O° M. S.  0 29 10 0 36 20 0 49 30 1 1 40 1 1 50 1 24 60 2 31 70 not observed. 80  7 51 = total time of heating from 0° to 70°.

The refult of these experiments, I confess, surprised me not a little; but the discovery of truth being the sole object of my inquiries (having no favourite theory to defend) it brings no disappointment along with it, under whatever unexpected shape it may appear. I hope that further experiments may lead to the discovery of the cause why there is so little difference in the conducting powers of air of such very different degrees of rarity, while there is so great a difference in the conducting powers of air, and of the Torricellian vacuum. At present, I shall not venture any conjectures upon the subject; but in the mean time I dare to affert, that the experiments I have made may be depended on.

The time of my stay at Manheim being expired (having had the honour to attend thither his most Serene Highness the Elector Palatine Duke of Bavaria, my most Gracious Master, in his late journey), I was prevented from pursuing these inquiries further at that time; but I shall not fail to recommence them the first leisure time I can find, which I fancy will be about the beginning of the month of November. In the mean time, to enable myself to pursue them with effect, I am sparing neither labour nor expence to provide a complete apparatus necessary for my purpose; and his Electoral Highness has been graciously pleased to order M. ARTARIA (who is in his fervice) to come to Munich to affift me. With fuch a Patron as his most Serene Highness, and with such an affistant as ARTARIA, I shall go on in my pursuits with chearfulness. Would to God that my labours might be as ufeful to others as they will be pleafant to me!

I shall conclude this letter with a short account of some experiments I have made to determine the conducting powers

of water and of mercury; and with a table, showing at one view the conducting powers of all the different mediums which I have examined.

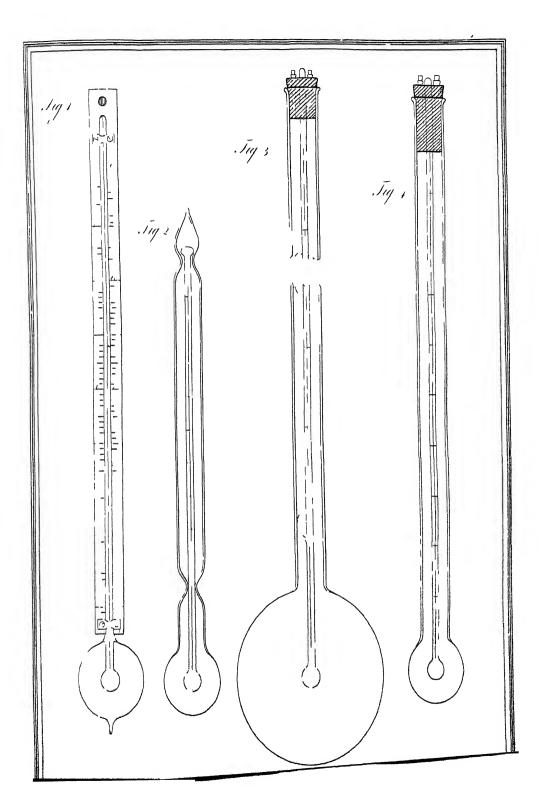
Having filled the glass globe inclosing the bulb of the thermometer N° 4. first with water, and then with mercury, I made the following experiments, to ascertain the conducting powers of those two fluids.

	ter N <sup>o</sup> 4. I by water. Exing water, and	Taken		<i>The</i> Surrou <i>f freez</i>	<i>rmometa</i> .nded b	25, and er N° 4 sy merci vater, a vater.	cry.	inged i	into
50:	Triat				elapfed			Heat	
Time erapied.	Heat acquired.	Exp.	N°24.	Exp.	N°25.	Exp.	N°26.	acquire	ed.
-	၀		-	-				C	ວ°
' M. S.	•	M.	S.	M.	S.	$\mathbf{M}_{\bullet}$			
0 19	10	0	5	0	5	0	5	10	
08	20	0	4		2	0	5	20	
0 9	30		2		2	0	4	39	
0 11	40	0	4	a	5	0	5	40	
0 15	50	0	4	0	4	0	7 8	5°	ر م
0 21	60	*	7	O	4		14		
0 34 2 13	70 80		15 obferve	ed. o	9 58	Not	obferve	d. 8	
4 - 3		_				-			
I 57=to	tal time of heat-			0			48=	total ti	me
ing from o° to				from (		o°.			

The total times of heating from 0° to 70° in the three experiments with mercury being 41 feconds, 31 feconds, and 48 feconds, the mean of these times is 36½ feconds; and as in the experiment with water the time employed in acquiring the same degree of heat was 1' 57"=117 feconds, it appears from

from these experiments, that the conducting power of mercury to that of water, under the circumstances described, is as  $36\frac{2}{3}$  to 117 inversely, or as 1000 to 313. And hence it is plain, why mercury appears so much hotter, and so much colder, to the touch than water, when in fact it is of the same temperature: for the force or violence of the sensation of bot or cold depends not intirely upon the temperature of the body exciting in us those sensations, or upon the degree of heat it actually possesses, but upon the quantity of heat it is capable of communicating to us, or receiving from us, in any given short period of time, or as the intensity of the communication; and this depends in a great measure upon the conducting powers of the bodies in question.

The sensation of *bot* is the entrance of heat into our bodies; that of *cold* is its exit; and whatever contributes to facilitate or accelerate this communication adds to the violence of the sensation. And this is another proof that the thermometer cannot be a just measure of the sensible heat, or cold, existing in bodies; or rather, that the touch does not afford us a just indication of their *real* temperatures.



A Table of the conducting Powers of the under-mentioned Mediums, as determined by the foregoing experiments.

Thermom. N° 1.								
	Taken ou		g water, an	d plunsed in	to barling w	ater.		
		Tin	ne elapfed.					
Torricellian Vacuum (Exp. N° 3. 4. and 13.)	Common air, denfity = 1, (Exp. N° 20.)	Rarefied air, denfity = \frac{1}{4} (Exp. N° 21.)	Rarefied air, denfity $= \frac{1}{24}$ (Exp. N° 22.)	Moift air (Exp. N° 18.)	Water (Exp. Nº 23.)	Mercury (Exp. N° 24, 25, and 26.)	Heat acquired,	
M. S. 0 52 0 58 1 18 1 25 1 58 3 19 11 57	M. S. 0 31 0 40 0 41 0 47 1 25 2 28 10 17	M. S. 0 31 0 38 0 44 0 51 1 7 1 19 2 27 10 21	M. S. 0 29 0 36 0 49 1 1 1 1 24 2 31	M. S. 0 6 0 4 0 5 0 9 0 18 0 26 0 43 7 45	M. S 0 19 0 8 0 9 0 11 0 15 0 21 0 34 2 13	M. S. 0 5 2 3 2 3 0 2 2 3 0 0 4 2 3 0 0 1 2 2 3 0 5 8	0° 10 20 30 40 50 60 70 80	
10 53 tal times o	7 36 of heating	7 37 from 0° to	7 51 70°.	1 51	1 57	o 36 <del>2</del>	= to	

In determining the relative conducting powers of these mediums, I have compared the times of the heating of the thermometers from 0° to 70° instead of taking the whole times from 0° to 80°, on account of the small variation in the heat of the boiling water arising from the variation of the weight of the atmosphere, and also on account of the very slow motion of the mercury between the 70th and the 80th degrees, and the difficulty of determining the precise moment when the mercury arrives at the 80th degree.

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Taking now the conducting power of mercury = 1000, the conducting powers of the other mediums, as determined by these experiments, will be as follows, viz.

Mercury	٠	•	1000
Moist air	•	•	330
Warer,	•	•	313
Common			
Rarefied ai	r, densit	$y = \frac{1}{4}$	. $80^{\frac{2}{100}}$
Rarefied a	ir, densit	$ty = \frac{1}{24}$	78
The Torri	cellian v	acuum	1 55

And in these proportions are the quantities of heat which these different mediums are capable of transmitting in any given time; and consequently these numbers express the relative sensible temperatures of the mediums, as well as their conducting powers. How far these decisions will hold good under a variation of circumstances experiment only can determine. This is certainly a subject of investigation not less curious in itself than it is interesting to mankind; and I wish that what I have done may induce others to turn their attention to this long neglected field of experimental inquiry. For my own part, I am determined not to quit it.

In the future profecution of these inquiries, I do not mean to confine myself solely to the determining of the conducting powers of sluids; on the contrary, solids, and particularly such bodies as are made use of for cloathing, will be principal subjects of my suture experiments. I have indeed already begun these researches, and have made some progress in them; but I sorbear to anticipate a matter which I propose for the subject of a suture communication.

XV. History and Dissection of an extraordinary Introsusception.

By John Coakley Lettsom, M. D. F. R. S. and A. S.

## Read March 16, 1786.

B. a child four years old, was first indisposed about the middle of September, 1784. When I was consulted, which was on the 7th of October, the symptoms resembled those of a cholera morbus. At this period, however, the diarrhoea had ceased; but the patient continued frequently to vomit, especially after taking nourishment.

On the 20th a dysentery succeeded, with mucous and bloody stools, which ceased after a few days continuance, when she nearly recovered her former state of health, without even reaching after her usual food. She was now removed into the country; and I did not hear of her again till December, when she was brought to town, on account of the return of the dysentery, which was, at this period, accompanied with a troublesome tenesmus, and a considerable degree of sever.

By anodyne medicines, and the use of opiate clysters, these complaints were occasionally moderated, and sometimes they totally ceased for a sew days, but seldom longer, and the intervals of relief gradually shortened; the attacks became also more violent, commencing with violent rigors, and sever succeeding; the pulse grew weaker and weaker, and the patient became extremely extenuated in siesh; and towards the conclusion of this Vol. LXXVI.

S f

month,

month, after repeated vomitings of a dark-coloured fluid, like coffee grounds, it finished its painful existence.

Bleeding, before the debility was become alarming, afforded no material respite. Fomentations to the abdomen, and tepid bathing of the whole body, were equally ineffectual. Anodyne starch clysters afforded some truce, but it could not be durable; the nature of the mischief was too momentous to afford any hope of permanent relief, as the dissection after death will evince.

# Examination of the Body after Death, by Mr. THOMAS WHATELY, Surgeon.

Upon exposing the cavity of the abdomen, the sigmoid flexure of the colon immediately presented itself to view, enlarged to the size of that of an adult, as also a large distended intestine appearing to be at first view a continuation of the transverse arch of this gut; and at the place where this seeming arch joined the sigmoid slexure, there appeared a firm or tight band, as if surrounding the intestine, and here it was strongly bound down.

On a nicer inspection this arch was found to be a portion of the ileum, which passing within the band was inclosed in the sigmoid slexure of the colon.

All the parts between this portion of the small intestincs and the sigmoid slexure, amongst which were the caput coli, cæcum with its appendix, and the whole of the great arch of the colon, could no where be seen. The want of these parts, the enlarged size of the sigmoid slexure, and the hard feel evidently shewing that it contained some substance, left no room to doubt, but that all the missing portion of the intestines

was contained within the figmoid flexure. A finger introduced into the anus felt a round substance in the rectum. with an opening in the middle, not unlike the os tincæ. This fubstance did not adhere, the finger passing round it freely, between it and the internal coat of the rectum. The liver, the urinary bladder, and small intestines, were the remaining parts which first appeared when the parietes of the abdomen were turned back.

Upon looking for the omentum, a portion of it only was found attached to the stomach, the remaining part evidently passed within the band into the sigmoid slexure.

The stomach was tied much closer to the spine than natural. by the displacing of the omentum and great arch of the colon. The gall bladder was as large as that of an adult, and was full of thin bile, but without obstruction to its passage into the duodenum.

. The general external appearance of all the intestines was natural, except flight inflammation in fome places.

The cavity of the abdomen also contained more than half an ounce of thin pus; and on the right fide were two ligamentous peritoneal substances, very much on the stretch; one formed by an extension of that part of the peritoneum called ligamentum \* coli dextrum; the other at the place where the colon is connected to the peritoneum over the right kidney.

As the further investigation of this uncommon disease required particular attention, I cut out all the parts connected with it, bringing away the whole figmoid flexure of the colon,

<sup>\*</sup> I have observed, that in some children the caput coli is naturally connected much more loosely than in others. It is probable, that the present case was one with of those.

with the rectum, anus, uterus, and bladder; also a part of the arch of the ileum with the omentum, and a portion of the stomach and drodenum.

The Drawing \* (Tab. VII.) was taken by Mr. Pole, Surgeon, of the natural fize, and the small intestines added from a sketch I made before the parts were removed from the body.

I then made a longitudinal incision through the coats of the sigmoid flexure of the colon, from the anus to the band at its upper part. Within the cavity, which was lined with mucus, appeared a large intestine, taking on the form of the sigmoid flexure, which on examination proved to be the great arch of the colon and the cæcum inverted; so that the villous coat was external, and in contact with the villous coat of the sigmoid flexure, through the whole extent of both; at the extremity of which inverted intestine were two apertures, viz. the large one felt by the singer per anum, and a smaller one.

It now plainly appeared, that the band was formed by the upper part of the figmoid flexure being drawn tight by the inverfion of the part of the colon immediately above it, the further progress of which was prevented by the peritoneal connections at that place not giving way; which caused it to appear as a band tying the intestine down.

This inclosed intestine was very much diseased, the upper part next the band being highly inflamed, and as it approached the caput coli in the rectum gradually terminated in mortification, so that for three inches from its extremity it was perfectly black.

No adhesion whatever appeared between the coats of these intestines, as this inverted colon might be lifted out of the sigmoid slexure to the band.

Upon

<sup>\*</sup> Mr. Basine very accurately reduced the scale under my own inspection from which the engravings are taken,

Upon cutting through the coats of this inverted intestine it was observed, that they were very much thickened and diseased; the enlargement of the gut, which was fully equal to that of an adult, confisting chiefly in a thickening of its various muscular fibres \*. The peritoneal coat, now become its internal furface, was every where highly inflamed, but not black as on the outfide, the inflammation gradually increasing from the band to the extremity of the cæcum. Through the whole length of its cavity was included a portion of the ileum uninverted, with its connecting mesentery, which communicated with the larger aperture above described at the extremity of the cæcum, and with the arch of the ileum above the band. It was contracted in fize, but was nearly free from thickening or inflammation; fome adhesions only connected it with the coats of the colon; but the portion above the band was at least four times as large, thus resembling in magnitude as well as occupying the place of the great arch of the colon. Besides this intestine, this cavity contained a portion of the omentum continued from that above, paffing within the band, and extending half-way to the rectum; an enlarged cluster of mesenteric glands, of the size of a pigeon's egg, which just emerged from under the band, and were connected with a portion of the mesentery above; and, at the lower part, the appendix vermiformis larger and longer than natural, but likewife uninverted, the mouth of the cavity of which formed the fmaller opening in the cæcum before mentioned. It was at this point of the diffection that the same ingenious Surgeon drew the figure, tab. VIII.

<sup>\*</sup> The increased action of these muscles, necessarily attendant on their inverted state, would increase the size of their muscular sibres, as happens in the bladder, when it acts frequently.

As

As long as the parts had been in this very uncommon fituation, the fæces must have passed through the valve of the colon, directly into the very lowest part of the rectum, without ever coming in contact with any portion of the large intestines.

And in the last week of the child's life, when a prolapsus frequently happened, the fæces passed directly from the ileum into the night-stool.

The arch of the ileum, in default of that of the colon, formed the reservoir for the fæces; which, with the partial interruption to their passage by the stricture occasioned by the band, probably caused its enlargement. But the fæces contained in it were of a thinner consistence, and wanted the fætor usually met with in the colon.

#### EXPLANATION OF THE PLATES.

#### TAB. VII.

A general view of the intestines, in the situation in which they appeared on first opening the body,

- aa. The enlarged ileum, putting on the appearance of the great arch of the colon.
  - b. The fudden enlargement of the ileum.
  - c. The ileum passing within the band into the colon.
  - d. Part of the omentum passing within the band.
- e. The intestinal band, formed by the inversion of the great arch of the colon immediately above it ceasing at this place.

- ff. The figmoid flexure of the colon, containing the introfuscepted portion of the alimentary canal.
  - g. The rectum distended with the same.
  - b. The anus.
  - 11. Small intestines of the natural fize and healthy appearance.

#### T A B. VIII.

The fame view, with the figmoid flexure laid open, and the edges turned back, to shew the contained parts; and likewise the introsuscepted colon laid open, to display the uninverted ileum and appendix vermisormis contained within it.

a a a a. Internal furface of the figmoid flexure of the colon foread open.

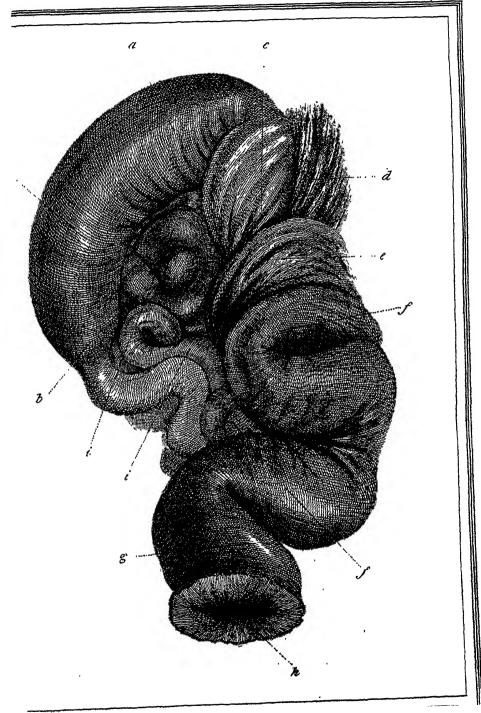
bbb. The external furface (by the inversion now become internal) of the great arch of the colon within the sigmoid flexure spread open.

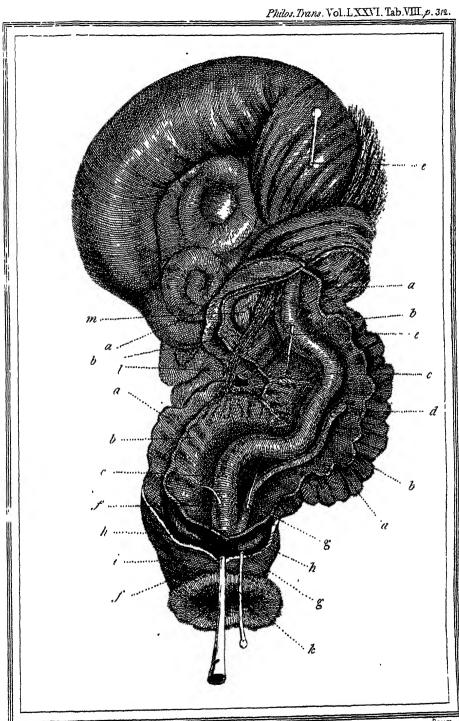
- cc. Part of the ileum uninverted.
- d. Appendix cæci uninverted.
- ee. A probe piercing the distended ileum, passed within the band, and brought out in another portion of the ileum, contained within the inverted colon below the band.
- ff. A blow-pipe passed through the valve of the colon, where it opened into the rectum, and brought out through the coats of the ileum above.
- gg. A probe passed into the natural opening of the appendix exci, and brought out above.
  - bb. The cæcum inverted.

ž.

- i. Part of the rectum.
- k. The anus.
- 1. Part of the omentum, attached to the peritoneal furface of the great arch of the colon, and continued from the portion above.
  - m. The cluster of enlarged mesenteric glands.







XVI. New Experiments on the Ocular Spectra of Light and Colours. By Robert Waring Darwin, M. D.; communicated by Erasmus Darwin, M. D. F. R. S.

## Read March 23, 1786.

WHEN any one has long and attentively looked at a bright object, as at the fetting sun, on closing his eyes, or removing them, an image, which resembles in form the object he was attending to, continues some time to be visible: this appearance in the eye we shall call the ocular spectrum of that object.

These ocular spectra are of sour kinds: 1st, Such as are owing to a less sensibility of a defined part of the retina; or spectra from defect of sensibility. 2d, Such as are owing to a greater sensibility of a defined part of the retina; or spectra from excess of sensibility. 3d, Such as resemble their object in its colour as well as form; which may be termed direct ocular spectra. 4th, Such as are of a colour contrary to that of their object; which may be termed reverse ocular spectra.

The laws of light have been most successfully explained by the great Newton, and the perception of visible objects has been ably investigated by the ingenious Dr. Berkeley and M. Malebranche; but these minute phænomena of vision have yet been thought reducible to no theory, though many philosophers have employed a considerable degree of attention upon them: among these are Dr. Jurin, at the end of Dr. Smith's Optics; M.

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ÆPINUS, in the Nov. Com. Petropol. V. 10.; M. BEGUELIN, in the Berlin Memoires, V. II. 1771; M. D'ARCY, in the Histoire de l'Acad. des Scienc. 1765; M. DE LA HIRE; and, lastly, the celebrated M. DE BUFFON, in the Memoires de l'Acad. des Scien. who has termed them accidental colours, as if subjected to no established laws, Ac. Par. 1743. M. p. 215.

I must here apprize the reader, that it is very difficult for different people to give the same names to various shades of colours; whence, in the following pages, something must be allowed if, on repeating the experiments, the colours here mentioned should not accurately correspond with his own names of them.

#### I. ACTIVITY OF THE RETINA IN VISION.

From the subsequent experiments it appears, that the retina is in an active not in a passive state during the existence of these ocular spectra; and it is thence to be concluded, that all vision is owing to the activity of this organ.

- 1. Place a piece of red silk, about an inch in diameter, as in fig. 1. (Tab. IX.) on a sheet of white paper, in a strong light; look steadily upon it from about the distance of half a yard for a minute; then closing your eyelids cover them with your hands, and a green spectrum will be seen in your eyes, resembling in form the piece of red silk: after some time, this spectrum will disappear and shortly re-appear; and this alternately three or four times, if the experiment is well made, till at length it vanishes entirely.
- 2. Place on a sheet of white paper a circular piece of blue silk, about four inches in diameter, in the sunshine; cover the center of this with a circular piece of yellow silk, about three

three inches in diameter; and the center of the yellow filk with a circle of pink filk, about two inches in diameter; and the center of the pink filk with a circle of green filk, about one inch in diameter; and the center of this with a circle of indigo, about half an inch in diameter; make a small speck with ink in the very center of the whole, as in fig. 2.; look steadily for a minute on this central spot, and then closing your eyes, and applying your hand at about an inch distance before them, fo as to prevent too much or too little light from passing through the eyelids, you will fee the most beautiful circles of colours that imagination can conceive, which are most resembled by the colours occasioned by pouring a drop or two of oil on a still lake in a bright day; but these circular irises of colours are not only different from the colours of the filks abovementioned, but are at the same time perpetually changing as long as they exist.

- 3. When any one in the dark presses either corner of his eye with his finger, and turns his eye away from his finger, he will fee a circle of colours like those in a peacock's tail: and a fudden flash of light is excited in the eye by a stroke on it. (Newton's Opt. Qu. 16.)
- 4. When any one turns round rapidly on one foot, till he becomes dizzy and falls upon the ground, the spectra of the ambient objects continue to present themselves in rotation, or appear to librate, and he feems to behold them for some time fill in motion.

From all these experiments it appears, that the spectra in the eye are not owing to the mechanical impulse of light impressed on the retina, nor to its chemical combination with that organ, nor to the absorption and emission of light, as is observed in many bodies: for in all these cases the spectra must either either remain uniformly, or gradually diminish; and neither their alternate presence and evanescence as in the first experiment, nor the perpetual changes of their colours as in the second, nor the stash of light or colours in the pressed eye as in the third, nor the rotation or libration of the spectra as in the fourth, could exist.

It is not abfurd to conceive, that the retina may be stimulated into motion, as well as the red and white muscles which form our limbs and veffels; fince it confifts of fibres, like those, intermixed with its medullary substance. To evince this structure, the retina of an ox's eye was suspended in a glass of warm water, and forcibly torn in a few places; the edges of these parts appeared jagged and hairy, and did not contract, and become smooth like simple mucus, when it is distended till it breaks: which shews that it consists of fibres: and this its fibrous construction became still more distinct to the fight, by adding some caustic alkali to the water, as the adhering mucus was first eroded, and the hair-like fibres remained floating in the veffel. Nor does the degree of transparency of the retina invalidate the evidence of its fibrous structure, since LEEUWENHOEK has shewn that the crystalline humour itself confifts of fibres. (Arcana Naturæ, V. 1. p. 70.)

Hence it appears, that as the muscles have larger fibres intermixed with a smaller quantity of nervous medulla, the organ of vision has a greater quantity of nervous medulla intermixed with smaller fibres; and it is probable, that the locomotive muscles, as well as the vascular ones, of microscopic animals have much greater tenuity than these of the retina.

And besides the similar laws, which will be shewn in this Paper to govern alike the actions of the retina and of the muscles.

muscles, there are many other analogies which exist between them. They are both originally excited into action by irritations, both act nearly in the same quantity of time, are alike strengthened or same by exertion, are alike painful if excited into action when they are in an instamed state, are alike liable to paralysis, and to the torpor of old age.

#### II. OF SPECTRA FROM DEFECT OF SENSIBILITY.

The retina is not so easily excited into action by less irritation after having been lately subjected to greater.

- I. When any one passes from the bright daylight into a darkened room, the irises of his eyes expand themselves to their utmost extent in a sew seconds of time; but it is very long before the optic nerve, after having been stimulated by the greater light of the day, becomes sensible of the less degree of it in the room; and, if the room is not too obscure, the irises will again contract themselves in some degree, as the sensibility of the retina returns.
- 2. Place about half an inch square of white paper on a black hat, and looking steadily on the center of it for a minute, remove your eyes to a sheet of white paper; and after a second or two a dark square will be seen on the white paper, which will continue some time. A similar dark square will be seen in the closed eye, if light be admitted through the eye-lids.

So after looking at any luminous object of a small size, as at the sun, for a short time, so as not much to fatigue the eyes, this part of the retina becomes less sensible to smaller quantities of light; hence, when the eyes are turned on other less luminous parts of the sky, a dark spot is seen resembling.

the shape of the sun, or other luminous object which we last beheld. This is the source of one kind of the dark-coloured musca volitantes. If this dark spot lies above the center of the eye, we turn our eyes that way, expecting to bring it into the center of the eye, that we may view it more distinctly; and in this case the dark spectrum seems to move upwards. If the dark spectrum is found beneath the center of the eye, we purfue it from the same motive, and it seems to move downwards. This has given rife to various conjectures of fomething floating in the aqueous humours of the eyes; but whoever, in attending to these spots, keeps his eyes unmoved by looking steadily at the corner of a cloud, at the same time that he observes the dark spectra, will be thoroughly convinced, that they have no motion but what is given to them by the movement of our eyes in purfuit of them. Sometimes the form of the spectrum, when it has been received from a circular luminous body, will become oblong; and fometimes it will be divided into two circular spectra, which is owing to our changing the angle made by the two optic axises, according to the distance of the clouds or other bodies to which the spectrum is supposed to be contiguous. The apparent fize of it will also be variable according to its supposed distance; but when such a spectrum is received with only one eye, the other being covered, its form and number are invariable.

As these spectra are more easily observable when our eyes are a little weakened by fatigue, it has frequently happened, that people of delicate constitutions have been much alarmed at them, fearing a beginning decay of their sight, and have thence fallen into the hands of ignorant oculists; but I believe they never are a prelude to any other disease of the eye, and that it is from habit alone, and our want of attention to them,

that we do not see them on all objects every hour of our lives. But as the nerves of very weak people lose their sensibility, in the same manner as their muscles lose their activity, by a small time of exertion, it frequently happens, that fick people in the extreme debility of fevers are perpetually employed in picking fomething from the bed-cloaths, occasioned by their mistaking the appearance of these musica volitantes in their eyes. Benve-NUTO CELINI, an Italian artist, a man of strong abilities, relates, that having passed the whole night on a distant mountain with some companions and a conjurer, and performed many ceremonies to raise the devil, on their return in the morning to Rome, and looking up when the fun began to rife, they faw numerous devils run on the tops of the houses, as they passed along; fo much were the spectra of their weakened eyes magnified by fear, and made subservient to the purposes of fraud or fuperstition. (Life of BEN. CELINI.)

3. Place a square inch of white paper on a large piece of straw-coloured silk; look steadily some time on the white paper, and then move the center of your eyes on the silk, and a spectrum of the form of the paper will appear on the silk, of a deeper yellow than the other part of it: for the central part of the retina, having been some time exposed to the stimulus of a greater quantity of white light, is become less sensible to a smaller quantity of it, and therefore sees only the yellow rays in that part of the straw-coloured silk.

Facts fimilar to these are observable in other parts of our system: thus, if one hand be made warm, and the other exposed to the cold, and then both of them immersed in subtepid water, the water is perceived warm to one hand, and cold to the other; and we are not able to hear weak sounds for some time after we have been exposed to loud ones; and we feel a chilliness

chilline's on coming into an atmosphere of temperate warmth, after having been some time confined in a very warm room: and hence the stomach, and other organs of digestion, of those who have been habituated to the greater stimulus of spirituous liquor, are not excited into their due action by the less stimulus of common food alone; of which the immediate confequence is indigestion and hypochondriacism.

### III. OF SPECTRA FROM EXCESS OF SENSIBILITY.

The retina is more easily excited into action by greater irritation after having been lately subjected to less.

- for a minute or two, in a bright day; on removing the hat a red or crimfon light is feen through the eye-lids. In this experiment the retina, after being fome time kept in the dark, becomes so sensible to a small quantity of light, as to perceive distinctly the greater quantity of red rays than of others which pass through the eye-lids. A similar coloured light is seen to pass through the edges of the singers, when the open hand is opposed to the slame of a candle.
- 2. If you look for some minutes steadily on a window in the beginning of the evening twilight, or in a dark day, and then move your eyes a little, so that those parts of the retina, on which the dark frame-work of the window was delineated, may now fall on the glass part of it, many luminous lines, representing the frame-work, will appear to lie across the glass panes: for those parts of the retina, which were before least stimulated by the dark frame-work, are now more sensible to

light than the other parts of the retina which were exposed to the more luminous parts of the window.

- 3. Make with ink on white paper a very black spot, about half an inch in diameter, with a tail about an inch in length, so as to represent a tadpole; look steadily for a minute on this spot, and, on moving the eye a little, the sigure of the tadpole will be seen on the white part of the paper, which sigure of the tadpole will appear whiter or more luminous than the other parts of the white paper; for the part of the retina on which the tadpole was delineated, is now more sensible to light than the other parts of it, which were exposed to the white paper. This experiment is mentioned by Dr. IRWIN, but is not by him ascribed to the true cause, namely, the greater sensibility of that part of the retina which has been exposed to the black spot, than of the other parts which had received the white field of paper, which is put beyond a doubt by the next experiment.
- 4. On closing the eyes after viewing the black spot on the white paper, as in the foregoing experiment, a red spot is seen of the form of the black spot: for that part of the retina, on which the black spot was delineated, being now more sensible to light than the other parts of it, which were exposed to the white paper, is capable of perceiving the red rays which penetrate the eyelids. If this experiment be made by the light of a tallow candle, the spot will be yellow instead of red; for tallow candles abound much with yellow light, which passes in greater quantity and force through the eyelids than blue light; hence the difficulty of distinguishing blue and green by this kind of candle light. The colour of the spectrum may possibly vary in the day light, according to the different colour of the meridian or the morning or evening light.

M. BEGUELIN, in the Berlin Memoires, V. II. 1771, observes, that, when he held a book so that the sun shone upon his half-closed eyelids, the black letters, which he had long inspected, became red, which must have been thus occasioned. Those parts of the retina which had received for some time the black letters, were so much more sensible than those parts which had been opposed to the white paper, that to the former the red light, which passed through the eyelids, was perceptible. There is a fimilar flory told, I think, in M. DE VOLTAIRE'S Historical Works, of a Duke of Tuscany, who was playing at dice with the general of a foreign army, and, believing he faw bloody spots upon the dice, portended dreadful events, and retired in confusion. The observer, after looking for a minute on the black spots of a die, and carelessly closing his eyes, on a bright day, would fee the image of a die with red spots upon it, as above explained.

5. On emerging from a dark cavern, where we have long continued, the light of a bright day becomes intolerable to the eye for a confiderable time, owing to the excess of sensibility existing in the eye, after having been long exposed to little or no stimulus. This occasions us immediately to contract the iris to its smallest aperture, which becomes again gradually dilated, as the retina becomes accustomed to the greater stimulus of the daylight.

The twinkling of a bright star, or of a distant candle in the night, is perhaps owing to the same cause. While we continue to look upon these luminous objects, their central parts gradually appear paler, owing to the decreasing sensibility of the part of the retina exposed to their light; whilst, at the same time, by the unsteadiness of the eye, the edges of them are perpetually falling on parts of the retina that were just before

before exposed to the darkness of the night, and therefore tenfold more sensible to light than the part on which the star or candle had been for some time delineated. This pains the eye in a similar manner as when we come suddenly from a dark room into bright daylight, and gives the appearance of bright scintillations. Hence the stars twinkle most when the night is darkest, and do not twinkle through telescopes, as observed by Musschenbroeck; and it will afterwards be seen why this twinkling is sometimes of different colours when the object is very bright, as Mr. Melvill observed in looking at Sirius. For the opinions of others on this subject, see Dr. Priestley's valuable History of Light and Colours, p. 494.

Many facts observable in the animal system are similar to these; as the hot glow occasioned by the usual warmth of the air, or our cloaths, on coming out of a cold bath; the pain of the singers on approaching the sire after having handled snow; and the inslamed heels from walking in snow. Hence those who have been exposed to much cold have died on being brought to a sire, or their limbs have become so much inslamed as to mortify. Hence much food or wine given suddenly to those who have almost perished by hunger has destroyed them; for all the organs of the samished body are now become so much more irritable to the stimulus of sood and wine, which they have long been deprived of, that inslammation is excited, which terminates in gangrene or fever.

## IV. OF DIRECT OCULAR SPECTRA.

A quantity of stimulus somewhat greater than natural excites the retina into spasinodic action, which ceases in a few seconds.

A certain duration and energy of the slimulus of light and colours excites the perfect action of the retina in vision; for very quick motions are imperceptible to us, as well as very slow ones, as the whirling of a top, or the shadow on a sundial. So perfect darkness does not affect the eye at all; and excess of light produces pain, not vision.

- 1. When a fire-coal is whirled round in the dark, a lucid circle remains a confiderable time in the eye; and that with fo much vivacity of light, that it is mistaken for a continuance of the irritation of the object. In the same manner, when a fiery meteor shoots across the night, it appears to leave a long lucid train behind it, part of which, and perhaps sometimes the whole, is owing to the continuance of the action of the retina after having been thus vividly excited. This is beautifully illustrated by the following experiment: fix a paper sail, three or four inches in diameter, and made like that of a smoke jack, in a tube of pasteboard; on looking through the tube at a distant prospect, some disjointed parts of it will be seen through the narrow intervals between the fails; but as the fly begins to revolve, these intervals appear larger; and when it revolves quicker, the whole prospect is seen quite as distinct as if nothing intervened, though less luminous.
- 2. Look through a dark tube, about half a yard long, at the area of a yellow circle of half an inch diameter, lying upon a blue area of double that diameter, for half a minute;

and on closing your eyes the colours of the spectrum will appear similar to the two areas, as in sig. 3.; but if the eye is kept too long upon them, the colours of the spectrum will be the reverse of those upon the paper, that is, the internal circle will become blue, and the external area yellow; hence some attention is required in making this experiment.

- 3. Place the bright flame of a spermaceti candle before a black object in the night; look steadily at it for a short time, till it is observed to become somewhat paler; and on closing the eyes, and covering them carefully, but not so as to compress them, the image of the blazing candle will continue distinctly to be visible.
- 4. Look steadily, for a short time, at a window in a dark day, as in Exp. 2. S. III. and then closing your eyes, and covering them with your hands, an exact delineation of the window remains for some time visible in the eye. This experiment requires a little practice to make it succeed well; since, if the eyes are satigued by looking too long on the window, or the day be too bright, the luminous parts of the window will appear dark in the spectrum, and the dark parts of the framework will; appear luminous, as in Exp. 2. S. III. And it is even difficult for many, who first try this experiment, to perceive the spectrum at all; for any hurry of mind, or even too great attention to the spectrum itself, will disappoint them, till they have had a little experience in attending to such small.

The spectra described in this section, termed direct ocular spectra, are produced without much satigue of the eye; the irritation of the luminous object being soon withdrawn, or its quantity of light being not so great as to produce any degree of uneasiness in the organ of vision; which distinguishes them

from the next class of ocular spectra, which are the consequence of fatigue. These direct spectra are best observed in such circumstances that no light, but what comes from the object, can fall upon the eye; as in looking through a tube, of half a yard long, and an inch wide, at a yellow paper on the side of a room, the direct spectrum was easily produced on closing the eye without taking it from the tube: but if the lateral light is admitted through the eye-lids, or by throwing the spectrum on white paper, it becomes a reverse spectrum, as will be explained below.

The other senses also retain for a time the impressions that have been made upon them, or the actions they have been excited into. So if a hard body is pressed upon the palm of the hand, as is practised in tricks of legerdemain, it is not easy to distinguish for a few seconds whether it remains or is removed; and tastes continue long to exist vividly in the mouth, as the smoke of tobacco, or the taste of gentian, after the sapid material is withdrawn.

- v. A quantity of stimulus somewhat greater than the last mentioned excites the retina into spasmodic action, which ceases and recurs alternately.
- 1. On looking for a time on the fetting fun, so as not greatly to satigue the sight, a yellow spectrum is seen when the eyes are closed and covered, which continues for a time, and then disappears, and recurs repeatedly before it intirely vanishes. This yellow spectrum of the sun when the eyelids are opened becomes blue; and if it is made to fall on the green grass, or on other coloured objects, it varies its own colour

colour by an intermixture of theirs, as will be explained in another place.

2. Place a lighted spermaceti candle in the night about one foot from your eye, and look steadily on the center of the slame, till your eye becomes much more fatigued than in S. IV. Exp. 3.; and on closing your eyes a reddish spectrum will be perceived, which will cease and return alternately.

The action of vomiting in like manner ceases, and is renewed by intervals, although the emetic drug is thrown up with the first effort: so after-pains continue some time after parturition; and the alternate pulsations of the heart of a viper are renewed for some time after it is cleared from its blood.

#### VI. OF REVERSE OCULAR SPECTRA.

The retina after having been excited into action by a stimulus somewhat greater than the last mentioned falls into opposite spasmodic action.

The actions of every part of animal bodies may be advantageously compared with each other. This strict analogy contributes much to the investigation of truth; while those looser analogies, which compare the phænomena of animal life with those of chemistry or mechanics, only serve to mislead our inquiries.

When any of our larger muscles have been in long or in violent action, and their antagonists have been at the same time extended, as soon as the action of the former ceases, the limb is stretched the contrary way for our ease, and a pandiculation or yawning takes place.

By the following observations it appears, that a similar circumstance obtains in the organ of vision; after it has been fatigued by one kind of action, it spontaneously falls into the opposite kind.

1. Place a piece of coloured filk, about an inch in diameter, on a sheet of white paper, about half a yard from your eyes; took steadily upon it for a minute; then remove your eyes upon another part of the white paper, and a spectrum will be seen of the form of the filk thus inspected, but of a colour opposite to it. A spectrum nearly similar will appear if the eyes are closed, and the eyelids shaded by approaching the hand near them, so as to permit some but to prevent too much light falling on them.

Red filk produced a green spectrum.

Green produced a red one.

Orange produced blue.

Blue produced orange.

Yellow produced violet.

Violet produced yellow.

That in these experiments the colours of the spectra are the reverse of the colours which occasioned them, may be seen by examining the third sigure in Sir Isaac Newton's Optics, L. II. p. 1. where those thin laminæ of air, which reslected yellow, transmitted violet; those which reslected red, transmitted a blue-green; and so of the rest, agreeing with the experiments above related.

2. These reverse spectra are similar to a colour, formed by a combination of all the primary colours except that with which the eye has been fatigued in making the experiment: thus the reverse spectrum of red must be such a green as would be produced by a combination of all the other prismatic colours.

To evince this fact the following satisfactory experiment was made. The prismatic colours were laid on a circular pasteboard wheel, about four inches in diameter, in the proportions defcribed in Dr. PRIESTLEY'S History of Light and Colours, pl. 12. fig. 33. except that the red compartment was intirely left out, and the others proportionably extended fo as to complete the circle. Then, as the orange is a mixture of red and yellow, and as the violet is a mixture of red and indigo, it became necessary to put yellow on the wheel instead of orange, and indigo instead of violet, that the experiment might more exactly quadrate with the theory it was defigned to establish or confute; because in gaining a green spectrum from a red object, the eye is supposed to have become insensible to red light. This wheel, by means of an axis, was made to whirl like a top; and on its being put in motion, a green colour was produced, corresponding with great exactness to the reverse spectrum of red.

3. In contemplating any one of these reverse spectra in the closed and covered eye, it disappears and re-appears several times successively, till at length it intirely vanishes, like the direct spectra in sect. v.; but with this additional circumstance, that when the spectrum becomes faint or evanescent, it is instantly revived by removing the hand from before the eyelids, so as to admit more light: because then not only the satigued part of the retina is inclined spontaneously to fall into motions of a contrary direction, but being still sensible to all other rays of light, except that with which it was lately satigued, is by these rays at the same time stimulated into those motions which form the reverse spectrum.

From these experiments there is reason to conclude, that the satisfied part of the retina throws itself into a contrary mode Vol. LXXVI. X x of

of action, like ofcitation or pandiculation, as foon as the stimulus, which has satigued it is withdrawn; and that it still remains sensible, that is, liable to be excited into action by any other colours at the same time, except the colour with which it has been satigued.

- VII. The retina after having been excited into action by a stimulus fomewhat greater than the last mentioned falls into various successive spasmodic actions.
- vell bear its brightness, the disc first becomes pale, with a luminous crescent, which seems to librate from one edge of it to the other, owing to the unsteadiness of the eye; then the whole phasis of the sun becomes blue, surrounded with a white halo; and on closing the eyes, and covering them with the hands, a yellow spectrum is seen, which in a little time changes into a blue one.

M. DE LA HIRE observed, after looking at the bright sun, that the impression in his eye first assumed a yellow appearance, and then blue; and wishes to ascribe these appearances to some affection of the nerves. (Porterfield on the Eye, Vol. I. p. 343.)

2. After looking steadily on about an inch square of pink filk, placed on white paper, in a bright sunshine, at the distance of a foot from my eyes, and closing and covering my eyelids, the spectrum of the silk was at first a dark green, and the spectrum of the white paper became of a pink. The spectra then both disappeared; and then the internal spectrum was blue; and then, after a second disappearance, became yellow,

and lastly pink, whilst the spectrum of the field varied into red and green.

These successions of different coloured spectra were not exactly the same in the different experiments, though observed, as near as could be, with the same quantity of light, and other similar circumstances; owing, I suppose, to trying too many experiments at a time; so that the eye was not quite free from the spectra of the colours which were previously attended to.

The alternate exertions of the retina in the preceding section resembled the oscitation or pandiculation of the muscles, as they were performed in directions contrary to each other, and were the consequence of fatigue rather than of pain. And in this they differ from the successive dissimilar exertions of the retina, mentioned in this section, which resemble in miniature the more violent agitations of the limbs in convulsive diseases, as epilepsy, chorea S. Viti, and opishotonos; all which diseases are perhaps, at first, the consequence of pain, and have their periods afterwards established by habit.

- VIII. The retina, after having been excited into action by a stimulus fomewhat greater than the last mentioned, falls into a fixed spasmodic action, which continues for some days.
- 1. After having looked long at the meridian sun, in making some of the preceding experiments, till the discs saded into a pale blue, I frequently observed a bright blue spectrum of the sun on other objects all the next and the succeeding day, which constantly occurred when I attended to it, and frequently when I did not previously attend to it. When I closed and covered

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my eyes, this appeared of a dull yellow; and at other times mixed with the colours of other objects on which it was thrown. It may be imagined, that this part of the retina was become infenfible to white light, and thence a bluish spectrum became visible on all luminous objects; but as a yellowish spectrum was also seen in the closed and covered eye, there can remain no doubt of this being the spectrum of the sun. A similar appearance was observed by M. ÆPINUS, which he acknowledges he could give no account of. (Nov. Com. Petrop. V. 10, p. 2. and 6.)

The locked jaw, and some cataleptic spasms, are resembled by this phænomenon; and from hence we may learn the danger to the eye by inspecting very luminous objects too long a time.

- 1x. A quantity of stimulus greater than the preceding induces a temporary paralysis of the organ of vision.
- 1. Place a circular piece of bright red filk, about half an inch in diameter, on the middle of a sheet of white paper; lay them on the floor in a bright sunshine, and fixing your eyes steadily on the center of the red circle, for three or sour minutes, at the distance of sour or six feet from the object, the red silk will gradually become paler, and finally cease to appear red at all.
- 2. Similar to these are many other animal facts; as purges, opiates, and even poisons, and contagious matter, cease to stimulate our system, after we have been habituated to their use. So some people sleep undisturbed by a clock, or even by a forge hammer in their neighbourhood: and not only continued irritations, but violent exertions of any kind, are succeeded

by temporary paralysis. The arm drops down after violent action, and continues for a time useless; and it is probable, that those who have perished suddenly in swimming, or in scating on the ice, have owed their deaths to the paralysis, or extreme satigue, which succeeds every violent and continued exertion.

### X. MISCELLANEOUS REMARKS.

There were some circumstances occurred in making these experiments, which were liable to alter the results of them, and which I shall here mention for the assistance of others, who may wish to repeat them.

- 1. Of direct and inverse spectra existing at the same time; of reciprocal direct spectra; of a combination of direct and inverse spectra; of a spectral halo; rules to pre-determine the colours of spectra.
- a. When an area, about fix inches fquare, of bright pink Indian paper, had been viewed on an area, about a foot fquare, of white writing paper, the internal spectrum in the closed eye was green, being the reverse spectrum of the pink paper; and the external spectrum was pink, being the direct spectrum of the pink paper. The same circumstance happened when the internal area was white, and external one pink; that is, the internal spectrum was pink, and the external one green. All the same appearances occurred when the pink paper was laid on a black hat.
- b. When fix inches fquare of deep violet polished paper was viewed on a foot square of white writing paper, the internal spectrum.

fpectrum was yellow, being the reverse spectrum of the violet paper, and the external one was violet, being the direct spectrum of the violet paper.

- c. When fix inches square of pink paper was viewed on a foot square of blue paper, the internal spectrum was blue, and the external spectrum was pink; that is, the internal one was the direct spectrum of the external object, and the external one was the direct spectrum of the internal object, instead of their being each the reverse spectrum of the objects they belonged to.
- d. When fix inches square of blue paper were viewed on a foot square of yellow paper, the interior spectrum became a brilliant yellow, and the exterior one a brilliant blue. The vivacity of the spectra was owing to their being excited both by the stimulus of the interior and exterior objects; so that the interior yellow spectrum was both the reverse spectrum of the blue paper, and the direct one of the yellow paper; and the exterior blue spectrum was both the reverse spectrum of the yellow paper, and the direct one of the blue paper.
- e. When the internal area was only a square half-inch of red paper, laid on a square foot of dark violet paper, the internal spectrum was green, with a reddish-blue halo. When the red internal paper was two inches square, the internal spectrum was a deeper green, and the external one redder. When the internal paper was six inches square, the spectrum of it became blue, and the spectrum of the external paper was red.
- f. When a square half-inch of blue paper was laid on a sixinch square of yellow paper, the spectrum of the central paper in the closed eye was yellow, incircled with a blue halo. On looking long on the meridian sun, the disc sades into a pale blue surrounded with a whitish halo.

These circumstances, though they very much perplexed the experiments till they were investigated, admit of a satisfactory explanation; for while the rays from the bright internal object in exp. a. fall with their full force on the center of the retina, and, by fatiguing that part of it, induce the reverse spectrum, many icattered rays, from the same internal pink paper, fall on the more external parts of the retina, but not in fuch quantity as to occasion much fatigue, and hence induce the direct spectrum of the pink colour in those parts of the eye. The same reverse and direct spectra occur from the violet paper in exp b: and in exp. c. the scattered rays from the central pink paper produce a direct spectrum of this colour on the external parts of the eve, while the scattered rays from the external blue paper produce a direct spectrum of that colour on the central part of the eye, instead of these parts of the retina falling reciprocally into their reverse spectra. In exp. d. the colours being the reverse of each other, the scattered rays from the exterior object falling on the central parts of the eye, and there exciting their direct spectrum, at the same time that the retina was excited into a reverse spectrum by the central object, and this direct and reverse spectrum being of similar colour, the fuperior brilliancy of this spectrum was produced. In exp. e. the effect of various quantities of stimulus on the retina, from the different respective fizes of the internal and external areas, induced a spectrum of the internal area in the center of the eye, combined of the reverse spectrum of that internal area and the direct one of the external area, in various shades of colour, from a pale green to a deep blue, with similar changes in the spectrum of the external area. For the same reasons, when an internal bright object was small, as in exp. f. instead of the whole of the spectrum of the external object being

being reverse to the colour of the internal object, only a kind of halo, or radiation of colour, similar to that of the internal object, was spread a little way on the external spectrum. For this internal blue area being so small, the scattered rays from it extended but a little way on the image of the external area of yellow paper, and could therefore produce only a blue halo round the yellow spectrum in the center.

If any one should suspect that the scattered rays from the exterior coloured object do not intermix with the rays from the interior coloured object, and thus affect the central part of the eye, let him look through an opake tube, about two feet in length, and an inch in diameter, at a coloured wall of a room with one eye, and with the other eye naked; and he will find, that by shutting out the lateral light, the area of the wall seen through a tube appears as if illuminated by the sunshine, compared with the other parts of it; from whence arises the advantage of looking through a dark tube at distant paintings.

Hence we may fafely deduce the following rules to determine before-hand the colours of all spectra. 1. The direct spectrum without any lateral light is an evanescent representation of its object in the unsatigued eye. 2. With some lateral light it becomes of a colour combined of the direct spectrum of the central object, and of the circumjacent objects, in proportion to their respective quantity and brilliancy. 3. The reverse spectrum without lateral light is a representation in the satigued eye of the form of its objects, with such a colour as would be produced by all the primary colours, except that of the object. 4. With lateral light the colour is compounded of the reverse spectrum of the central object, and the direct spectrum of the circumjacent objects, in proportion to their respective quantity and brilliancy.

# 11. Variation and vivacity of the spectra occasioned by extraneous light.

The reverse spectrum, as has been before explained, is similar to a colour, formed by a combination of all the primary colours, except that with which the eye has been fatigued in making the experiment: so the reverse spectrum of red is such a green as would be produced by a combination of all the other prismatic colours. Now it must be observed, that this reverse spectrum of red is therefore the direct spectrum of a combination of all the other prismatic colours, except the red; whence, on removing the eye from a piece of red filk to a sheet of white paper, the green spectrum, which is perceived, may either be called the reverse spectrum of the red silk, or the direct spectrum of all the rays from the white paper, except the red; for in truth it is both. Hence we sec the reason why it is not easy to gain a direct spectrum of any coloured object in the day-time, where there is much lateral light, except of very bright objects, as of the fetting fun, or by looking through an opake tube; because the lateral external light falling also on the central part of the retina, contributes to induce the reverse spectrum, which is at the same time the direct spectrum of that lateral light, deducting only the colour of the central object which we have been viewing. And for the fame reason, it is difficult to gain the reverse spectrum, where there is no lateral light to contribute to its formation. Thus, in looking through an opake tube on a yellow wall, and clofing my eye, without admitting any lateral light, the spectra were all at first yellow; but at length changed into blue. And on looking in the same manner on red paper, I did at length get a grecia Vol. LXXVI. Yv

green spectrum; but they were all at first red ones: and the same after looking at a candle in the night.

The reverse spectrum was formed with greater facility when the eye was thrown from the object on a sheet of white paper, or when light was admitted through the closed eyelids; because not only the fatigued part of the retina was inclined spontaneously to fall into motions of a contrary direction; but being still sensible to all other rays of light except that with which it was lately fatigued, was by these rays slimulated at the same time into those motions which form the reverse spectrum. Hence, when the reverse spectrum of any colour became faint, it was wonderfully revived by admitting more light through the eyelids, by removing the hand from before them: and hence, on covering the closed eyelids, the spectrum would often cease for a time, till the retina became sensible to the stimulus of the smaller quantity of light, and then it recurred. Nor was the spectrum only changed in vivacity, or in degree, by this admission of light through the eyelids; but it frequently happened, after having viewed bright objects, that the spectrum in the closed and covered eye was changed into a third spectrum, when light was admitted through the eyelids: which third spectrum was composed of such colours as could pass through the eyelids, except those of the object. Thus, when an area of half an inch diameter of pink paper was viewed on a sheet of white paper in the sunshine, the spectrum with closed and covered eyes was green; but on removing the hands from before the closed eyelids, the spectrum became yellow, and returned instantly again to green, as often as the hands were applied to cover the eyelids, or removed from them: for the retina being now infensible to red light, the yellow rays passing through the eyelids in greater quantity than the other colours, induced a yellow spectrum; whereas if the spectrum was thrown on white paper, with the eyes open, it became only a lighter green.

Though a certain quantity of light facilitates the formation of the reverse spectrum, a greater quantity prevents its formation, as the more powerful stimulus excites even the satigued parts of the eye into action; otherwise we should see the spectrum of the last viewed object as often as we turn our eyes. Hence the reverse spectra are best seen by gradually approaching the hand near the closed eyelids to a certain distance only, which must be varied with the brightness of the day, or the energy of the spectrum. Add to this, that all dark spectra, as black, blue, or green, if light be admitted through the eyelids, after they have been some time covered, give reddish spectra, for the reasons given in sect. III. exp. 1.

From these circumstances of the extraneous light coinciding with the spontaneous efforts of the fatigued retina to produce a reverse spectrum, as was observed before, it is not easy to gain a direct spectrum, except of objects brighter than the ambient light; fuch as a candle in the night, the fetting fun, or viewing a bright object through an opake tube; and then the reverfe spectrum is instantaneously produced by the admission of some external light; and is as instantly converted again to the direct fpectrum by the exclusion of it. Thus, on looking at the fetting fun, on closing the eyes, and covering them, a yellow fpectrum is feen, which is the direct spectrum of the setting fun; but on opening the eyes on the sky, the yellow spectrum is immediately changed into a blue one, which is the reverse spectrum of the yellow sun, or the direct spectrum of the blue sky, or a combination of both. And this is again transformed into a yellow one on closing the eyes, and fo reciprocally, as quick as the motions of the opening and closing eyelids. Hence, when Mr. MELWILL observed the Y v 2

the scintillations of the star Sirius to be sometimes coloured, these were probably the direct spectrum of the blue sky on the parts of the retina satigued by the white light of the star. (Essays Physical and Literary, p. 81. V. 2.)

When a direct spectrum is thrown on colours darker than itself, it mixes with them; as the yellow spectrum of the fetting fun, thrown on the green grass, becomes a greener yellow. But when a direct spectrum is thrown on colours brighter than itself, it becomes instantly changed into the reverse spectrum, which mixes with those brighter colours. So the yellow spectrum of the setting sun thrown on the luminous sky becomes blue, and changes with the colour or brightness of the clouds on which it appears. But the reverse spectrum mixes with every kind of colour on which it is thrown, whether brighter than itself or not: thus the reverse spectrum, obtained by viewing a piece of yellow filk, when thrown on white paper was a lucid blue green; when thrown on black Turkey leather becomes a deep violet. And the spectrum of blue filk, thrown on white paper, was a light yellow; on black filk was an obscure orange; and the blue spectrum, obtained from orange-coloured filk, thrown on yellow, became a green.

In these cases the retina is thrown into activity or sensation by the stimulus of external colours, at the same time that it continues the activity or sensation which forms the spectra; in the same manner as the prismatic colours, painted on a whirling top, are seen to mix together. When these colours of external objects are brighter than the direct spectrum which is thrown upon them, they change it into the reverse spectrum, like the admission of external light on a direct spectrum, as explained above. When they are darker than the direct spec-

trum, they mix with it, their weaker stimulus being insufficient to induce the reverse spectrum.

# 111. Variation of spectra in respect to number and figure and remission.

When we look long and attentively at any object, the eye cannot always be kept intirely motionless; hence, on inspecting a circular area of red filk placed on white paper, a lucid crescent or edge is seen to librate on one side or other of the red circle: for the exterior parts of the retina fometimes falling on the edge of the central filk, and fometimes on the white paper, are less fatigued with red light than the central part of the retina, which is constantly exposed to it; and therefore, when they fall on the edge of the red filk, they perceive it more vividly. Afterwards, when the eye becomes fatigued, a green spectrum in the form of a crescent is seen to librate on one side or other of the central circle, as by the unsteadiness of the eye a part of the fatigued retina falls on the white paper; and as by the increasing fatigue of the eye the central part of the filk appears paler, the edge on which the unfatigued part of the retina occasionally falls will appear of a deeper red than the original filk, because it is compared with the pale internal part of it. M. DE Buffon in making this experiment observed, that the red edge of the filk was not only deeper coloured than the original filk; but, on his retreating a little from it, it became oblong, and at length divided into two, which must have heen owing to a change of the angle of the two optic axifes with the new distance he observed it at. Thus, if a pen is held up before a distant candle, when we look intensely at the pen two candles are seen behind it; when we look intensely at

the candle two pens are feen. If the fight be unsteady at the time of beholding the fun, even though one eye only be used, many images of the fun will appear, or luminous lines, when the eye is closed. And as some parts of these will be more vivid than others, and some parts of them will be produced nearer the center of the eye than others, these will disappear sooner than the others; and hence the number and shape of these spectra of the fun will continually vary, as long as they exist. The cause of some being more vivid than others, is the unsteadiness of the eye of the beholder, so that some parts of the retina have been longer exposed to the funbeams. That some parts of a complicated spectrum fade and return before other parts of it, the following experiment evinces. Draw three concentric circles; the external one an inch and a half in diameter, the middle one an inch, and the internal one half an inch; colour the external and internal areas blue, and the remaining one yellow, as in fig. 4.; after having looked about a minute on the center of these circles, in a bright light, the spectrum of the external area appears first in the closed eye, then the middle area, and lastly the central one; and then the central one difappears, and the others in inverted order. If concentric circles of more colours are added, it produces the beautiful ever changing spectrum in sect. I. exp. 2.

From hence it would seem, that the center of the eye produces quicker remissions of spectra, owing perhaps to its greater sensibility; that is, to its more energetic exertions. These remissions of spectra bear some analogy to the tremors of the hands, and palpitations of the heart, of weak people; and perhaps a criterion of the strength of any muscle or nerve may be taken from the time it can be continued in exertion.

- IV. Variation of spectra in respect to brilliancy; the visibility of the circulation of the blood in the eye..
- 1. The meridian or evening light makes a difference in the colours of some spectra; for as the sun descends, the red rays, which are less refrangible by the convex atmosphere, abound in great quantity. Whence the spectrum of the light parts of a window at this time, or early in the morning, is red; and becomes blue either a little later or earlier; and white in the meridian day; and is also variable from the colour of the clouds or sky which are opposed to the window.
- 2. All these experiments are liable to be confounded, if they are made too foon after each other, as the remaining spectrum will mix with the new ones. This is a very troublesome circumstance to painters, who are obliged to look long upon the same colour; and in particular to those whose eyes, from natural debility, cannot long continue the fame kind of exertion. For the fame reason, in making these experiments, the result becomes much varied if the eyes, after viewing any object, are removed on other objects for but an instant of time, before we close them to view the spectrum; for the light from the object, of which we had only a transient view, in the very time of closing our eyes acts as a stimulus on the satigued retina; and for a time prevents the defired spectrum from appearing, or mixes its own spectrum with it. Whence, after the cyclids are closed, either a dark field, or some unexpected colours, are beheld for a few feconds, before the defired spectrum becomes distinctly visible.
- 3. The length of time taken up in viewing an object, of which we are to observe the spectrum, makes a great difference

in the appearance of the spectrum, not only in its vivacity, but in its colour; as the direct spectrum of the central object, or of the circumjacent ones, and also the reverse spectra of both, with their various combinations, as well as the time of their duration in the eye, and of their remissions or alternations, depend upon the degree of fatigue the retina is subjected to. The Chevalier D'ARCY constructed a machine by which a coal of fire was whirled round in the dark, and found, that when a luminous body made a revolution in eight thirds of time, it presented to the eye a complete circle of fire; from whence he concludes, that the impression continues on the organ about the feventh part of a fecond. (Mém. de l'Acad. des Sc. 1765.) This, however, is only to be confidered as the shortest time of the duration of these direct spectra; since in the fatigued eye both the direct and reverse spectra, with their intermissions, appear to take up many seconds of time, and feem very variable in proportion to the circumstances of fatigue or energy.

4. It sometimes happens, if the eyeballs have been rubbed hard with the singers, that lucid sparks are seen in quick motion amidst the spectrum we are attending to. This is similar to the slashes of sire from a stroke on the eye in sighting, and is resembled by the warmth and glow which appear upon the skin after friction, and is probably owing to an acceleration of the arterial blood into the vessels emptied by the previous pressure. By being accustomed to observe such small sensations in the eye, it is easy to see the circulation of the blood in this organ. I have attended to this frequently, when I have observed my eyes more than commonly sensible to other spectra. The circulation may be seen either in both eyes at a time, or only in one of them; for as a certain quantity of light is necessary

to produce this curious phænomenon, if one hand be brought nearer the closed eyelids than the other, the circulation in that eye will for a time disappear. For the easier viewing the circulation, it is fometimes necessary to rub the eyes with a certain degree of force after they are closed, and to hold the breath rather longer than is agreeable, which, by accumulating more blood in the eye, facilitates the experiment; but in general it may be feen distinctly after having examined other spectra with your back to the light, till the eyes become weary; then having covered your closed eyelids for half a minute, till the spectrum is faded away which you were examining, turn your face to the light, and removing your hands from the eyelids, by and by again shade them a little, and the circulation becomes curiously distinct. The streams of blood are however generally feen to unite, which shews it to be the venous circulation, owing, I suppose, to the greater opacity of the colour of the blood in these vessels; for this venous circulation is also much more easily seen by the microscope in the tail of a tadpole.

- v. Variation of spectra in respect to distinctness and size; with a new way of magnifying objects.
- together were opposite to each other, as yellow and blue, red and green, &c. according to the table of resections and transmissions of light in Sir Isaac Newton's Optics, B. II. fig. 3. the spectra of those colours were of all others the most brilliant, and best defined; because they were combined of the reverse spectrum of one colour, and of the direct spectrum of the other. Hence, in books printed with small types, or in Vol. LXXVI.

the minute graduation of thermometers, or of clock-faces, which are to be seen at a distance, if the letters or figures are coloured with orange, and the ground with indigo; or the letters with red, and the ground with green; or any other lucid colour is used for the letters, the spectrum of which is fimilar to the colour of the ground; fuch letters will be feen much more diffinctly, and with less confusion, than in black or white: for as the spectrum of the letter is the same colour with the ground on which they are feen, the unsteadiness of the eye in long attending to them will not produce coloured lines by the edges of the letters, which is the principal cause of their confusion. The beauty of colours lying in vicinity to each other, whose spectra are thus reciprocally similar to each colour, is owing to this greater ease that the eye experiences in beholding them distinctly; and it is probable, in the organ of hearing a fimilar circumstance may constitute the pleasure of melody. Sir Isaac Newton observes, that gold and indigo were agreeable when viewed together; and thinks there may be fome analogy between the fensations of light and sound. (Optics, Qu. 14.)

In viewing the spectra of bright objects, as of an area of red silk of half an inch diameter on white paper, it is easy to magnify it to tenfold its size: for if, when the spectrum is formed, you still keep your eye fixed on the silk area, and remove it a few inches further from you, a green circle is seen round the red silk: for the angle now subtended by the silk is less than it was when the spectrum was formed, but that of the spectrum continues the same, and our imagination places them at the same distance. Thus when you view a spectrum on a sheet of white paper, if you approach the paper to the eye, you may diminish it to a point; and if the paper is made to recede from

the eye, the spectrum will appear magnified in proportion to the distance.

I was furprised, and agreeably amused, with the following experiment. I covered a paper about four inches square with yellow, and with a pen silled with a blue colour wrote upon the middle of it the word BANKS in capitals, as in sig. 5, and, sitting with my back to the sun, sixed my eyes for a minute exactly on the center of the letter N in the middle of the word; after closing my eyes, and shading them somewhat with my hand, the word was distinctly seen in the spectrum in yellow letters on a blue field; and then, on opening my eyes on a yellowish wall at twenty feet distance, the magnified name of BANKS appeared written on the wall in golden characters.

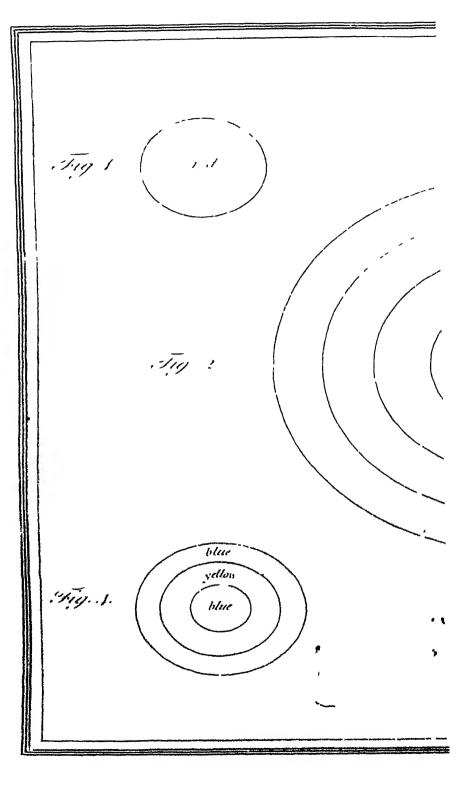
#### CONCLUSION.

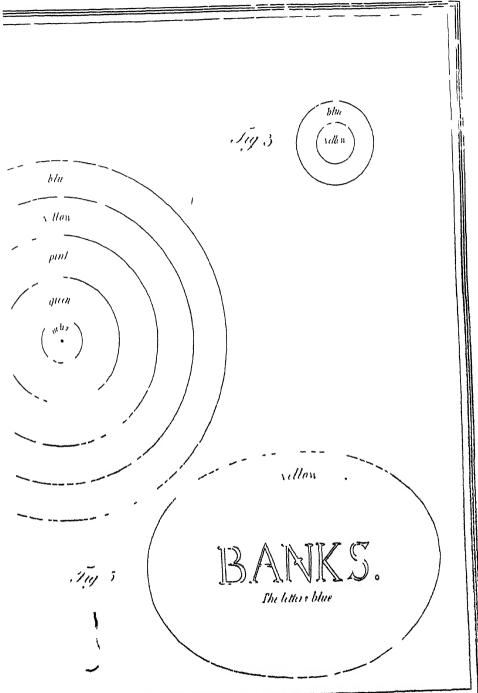
It was observed by the learned M. Sauvages (Nosol. method. Cl. VIII. Ord. 1.) that the pulsations of the optic artery might be perceived by looking attentively on a white wall well illuminated. A kind of net-work, darker than the other parts of the wall, appears and vanishes alternately with every pulsation. This change of the colour of the wall he well ascribes to the compression of the retina by the diastole of the artery. The various colours produced in the eye by the pressure of the singer, or by a stroke on it, as mentioned by Sir Isaac Newton, seem likewise to originate from the unequal pressure on various parts of the retina. Now as Sir Isaac Newton has shewn, that all the different colours are reslected or transmitted by the laminæ of soap bubbles, or of air, according to their different thickness or thinness, is it not probable, that the

effect of the activity of the retina may be to alter its thickness or thinness, so as better to adapt it to reflect or transmit the colours which stimulate it into action? May not muscular sibres exist in the retina for this purpose, which may be less minute than the locomotive muscles of microscopic animals? May not these muscular actions of the retina constitute the sensation of lights and colours; and the voluntary repetitions of them, when the object is withdrawn, constitute our memory of them? And lastly, may not the laws of the sensations of light, here investigated, be applicable to all our other senses, and much contribute to elucidate many phænomena of animal bodies both in their healthy and diseased state; and thus render this investigation well worthy the attention of the physician, the metaphysician, and the natural philosopher?

Derby, November 1, 1785.







XVII. Observations on some Causes of the Excess of the Mortality of Males above that of Females. By Joseph Clarke, M. D. Physician to the Lying-in Hospital at Dublin. Communicated by the Rev. Richard Price, D. D. F. R. S. in a Letter to Charles Blagden, M. D. Sec. R. S.

## Read March 30, 1786.

SIR,

4

Newington-Green, February 6, 1786.

I RECEIVED fome time ago the inclosed letters and registry from Dr. CLARKE, Physician to the Lying-in Hospital at Dublin. They contain some accounts that seem to me not improper to be communicated to the Royal Society.

The observations which have been made on the laws that govern human mortality prove, that the mortality of males exceeds that of females in almost all the stages of life, and particularly in the earliest stages; and that this excess prevails most in great towns, and all the less natural situations of human life. The facts in these papers throw some light on this fubject. Male fætus's requiring more nutrition than female fætus's, because larger, and being also for this reason more liable to injury in delivery, are brought into the world less perfect: and this happening more or less in proportion to the vigour and just formation of the mother, it must happen most in those situations where the greatest tenderness of frame and deviations from nature take place. The truth, in short,

short, seems to be, that any debility in either parent must affect most the production of that sex which requires the largest and strongest stamina; and that such debilities prevailing most in great towns and polished Societies, the excess of the mortality of males must also be greatest in such situations. And this I reckon the principal reason of a circumstance in human mortality which, before I received these communications from Dr. CLARKE, I did not so well understand.

With much respect I am, &c.

RICH. PRICE.

Dr. CLARKE's first Letter to the Rev. Dr. PRICE.

SIR, Dublin.

IN your very useful Treatise on Life Annuities, &c. you remark \*, that "it has been observed, that the Author of "nature has provided, that more males should be born than seemales, on account of the particular waste of males, occa- fioned by wars and other causes. That perhaps it might have been observed, with more reason, that this provision had in view that particular weakness or delicacy in the constitution of males which makes them more subject to more tality; and which, consequently, renders it necessary that more of them should be produced, in order to preserve

"in the world a due proportion between the fexes." And further, you elsewhere remark \*, that "the facts recited at "the end of your fourth Essay prove, that there is a difference between the mortality of males and semales; but that you must however observe, that it may be doubted, whether this difference, so unfavourable to males, be natural; and that there are facts which prove that you have reason for such a doubt." After stating a number of very satisfactory facts of this kind you remark, that "the inference from them is very obvious; that they seem to shew sufficiently, that human slife in males is more brittle than in semales, only in consequence of adventitious causes, or of some particular debility which takes place in polished and luxurious societies, and "especially in great towns."

What those adventitious causes are, or how this particular debility is produced and operates, are questions which appear to me highly interesting and curious. I have therefore been at considerable pains to examine and arrange a very accurate and extensive registry in such a manner as I hope will throw some light on these questions. As it is to the accuracy of modern registers that we are originally indebted for our knowledge of the facts in question, I apprehend, it is from the same source only that we shall be enabled satisfactorily to explain them.

Of the registry inclosed, I beg leave to observe to you, Sir, that it has been kept from its commencement by a man of uncommon accuracy (one of the under-clerks of our House of Commons); and that as the poor women and their children are obliged to pass through his office, before leaving the Hospital, his situation is such that there is no likelihood of his being deceived. It exhibits to our view the occurrences of 28 years

in above 20,000 instances: a number which I am inclined to think can hardly appear insufficient for establishing some general inferences and conclusions on a tolerably sure soundation. Although my reasoning on these matters should not appear very conclusive, or my calculations perfectly accurate, yet I flatter myself, that the sacts will neither be unacceptable nor useless to you.

I believe it may be fafely afferted, that anatomy has not hitherto detected any internal difference between the animal economy of the male and female, which can be supposed to account for their difference of mortality, more especially in early Infancy; and this (it deserves to be particularly remarked) is the period during which the chances are much the greatest against male life. It is a matter of common observation that males, cæteris paribus, grow to a greater fize than females, both in utero and every subsequent period of their growth. Consequently, they must meet with more difficulty, and endure more hardship and fatigue, in the hour of birth. Accordingly, practitioners in midwifry, taught by experience, know, that when any confiderable difficulty occurs in the birth of a child (for example, in all the different kinds of preternatural labours) they stand a much better chance of faving the life of a female than of a male. It is on this principle we can explain what our registry concurs with others in proving, viz. that near one-half more males than females are still-born. Naturalists are agreed, that the head of the human fœtus is larger in proportion to its body than that of any other animal; and I believe it is certain, that no animal whatever brings forth its young with fo much difficulty, pain, and danger, as a woman. Now as we know that the head contains one of the most important organs of the body to life, it is highly reasonable to suppose, that any additional material effects on the whole system. These effects though often may not be always immediate. They may operate in weakening the male constitution so as to render it more apt to be affected by any exciting cause of disease soon after birth, and less able to struggle against it. It may be asked, how this will apply to the difference of mortality in great towns and country situations? The answer evidently is, that in great towns rickets, scrophula, and other diseases assecting the bones, and producing consequent mal-conformation of the semale sex, are more frequent than in healthy country situations.

There is another circumstance, Sir, which may have some influence in producing that particular debility which you mention. It is this: as the stamina of the male are naturally constituted to grow to a greater fize, a greater supply of nourishment in utero will be necessary to his growth than to that of a female. Defects in this particular, proceeding from delicacy of constitution or diseases of the mother, must of course be more injurious to the male fex. And although the male children may be so lucky as to escape abortion and the perils of delivery, it is probable, that they will be more apt to languish under disease, or die at some future period, from the application of noxious causes to an originally half-starved frame. To a person little accustomed to consider physiological subjects, this reasoning may appear somewhat obscure. It may, perhaps, be somewhat illustrated by considering that nourishment of the fœtus after birth which nature has provided for. Suppose every mother in a great city obliged to suckle and nurse her own child, without the affiftance of spoon-meat; and every mother in the adjacent country to do the same. Of the former there would not perhaps be one good nurse in five; and of the Aaa latter. Vol. LXXVI.

latter, perhaps, not one bad in ten. The difference of mortality that would ensue both to mothers and children thus situated, and the greater sufferings of the male than semale sex, may be easily conceived, but not easily calculated. We see that, when a woman conceives twins, and has two sectuses in utero to nourish instead of one, it becomes peculiarly satal both to her and her offspring. The chances are above four to one greater against her than against a woman bringing forth one child, and about two to one against her issue\*.

Give me leave, Sir, to call your attention a little further to the facts relating to twins. They are fingular and curious, at the fame time that they serve to confirm some of the preceding reasoning. Near one-half more twins die, and near one-third more are still-born, than of single children. And why?—It is not because they meet with greater difficulties in the birth. On the contrary, it is a known fact, that, being much less than other children, women bring them forth with more ease. Does it not then proceed from a scanty nutrition, by which they are oftener blighted in utero than single children; and, when born alive, have less strength to support life through the first stages of its existence.

It is farther worthy of observation, that though double the numbers of twins die and are still-born, compared to single children, yet the proportion of male twins lost to females is lefs. Only one-fifth more of the male sex die than of the female, and only one-third more is still-born. Whereas of single children, whose proportional mortality is one-half less, one-fourth more of the male sex die, and near double the number is still-born. To what then are we to attribute this lessened mortality in favour of male twins? Probably to their brain and

<sup>\*</sup> Compare the 7th and 14th, 6th and 13th inferences in the annexed extracts.

nervous system suffering less during delivery, on account of their heads being much finaller than those of fingle children. Were I disposed to be prolix, I could offer many more plausible arguments on this subject; but to you, Sir, I am sure they would be unnecessary. There is only one circumstance remaining, relative to the proportion of the fexes, which I cannot pass over in silence. We see evident wisdom in the creation of a greater number of males than females; but why the proportion they bear to each other differs in different countries and fituations, and why there should be a seventeenth more males born of fingle children than twins, are questions which I leave to be decided by those philosophers who understand the theory of generation better than I do. Be this as it may, I am convinced that the majority in favour of the male fex is fooner destroyed than the generality of writers seem to be aware of. Did the limits of this letter permit, I think, I could prove from Dr. Short's own data\*, that the majority of males is destroyed long before the common marriagcable period; but I shall content myself with an observation or two on the registry before us. If one-half of the whole born in this hospital die before three years, which is the established computation for great cities; and if, on the lofs of fomewhat more than a third of this half, a majority of 1177 be reduced to 483 by a loss of 694, as appears from the registry, it is pretty evident, that by the death of the two remaining thirds, a majority will be left in favour of the female fex. It is obvious, that the statement with regard to twins corroborates this supposition; for of them, instead of a fifth, there is near one balf dead and still-born, the consequence of which is, that we send out a majority of females. It may be objected, that their males do not bear so great a proportion to the females; and that, therefore, it is not to be expected they should keep up their majority
so long. But there is only a seventeenth sewer males produced; whereas it has been already shewn, that there is a much
greater proportion between the deaths of single and twin males
against the former and in savour of the latter.

Such are the outlines, Sir, of my fentiments on this subject. I have assumed the liberty of addressing them to you without ceremony, as a well-wisher to every member of the republic of letters. I shall be happy, should your fentiments happen to coincide with mine, or if I can be of any farther fervice in promoting your very laudable inquiries.

I am, Sir, with great respect, &c.

JOSEPH CLARKE.

Lying in Hospital, June 9, 1785.

# Dr. CLARKE's fecend Letter to the Rev. Dr. PRICE.

5 I R,

Dublin, Oct. 22, 1785.

ENCOURAGED by your approbation of my former letter, I will take the liberty of stating to you a few more facts and observations, which I hope you will judge an Appendix to it of some importance.

With the view of ascertaining how far some of the foregoing conjectures are well founded, and of determining with greater greater precision the more obvious differences between the male and semale sex in infancy, I began in the month of July last by weighing forty children, twenty of each sex, and by taking the dimensions of their heads. In the months of August and September I repeated the same experiment twice, taking such children as appeared to have arrived at the sull period of gestation promiscuously as they happened to be born.

I weighed them all a few hours after birth, before they had taken food, and before purgative medicines had time to operate. For this purpose, I made use of a small spring or pocket steelyard, which weighs anything (not heavier than a few pounds, appended to it with sufficient accuracy. To this was attached a slannel bag, into which the children were put, at suff, naked; but this I soon sound very troublesome. The number often wanted time sufficient to assist me, and timid mothers were assaud of their infants catching cold; I was therefore obliged to weigh them with their cloaths on, and to subtract a certain quantity from the gross weight of each child, according as it was full, middling, or light cloathed. Whatever inaccuracy this may have introduced, as to the real weight of the children, it can but little influence their comparative weights, or the differences between the two sexes, which it was my object to assertain.

For measuring their heads, I made use of a piece of painted or varnished linen tape, divided into inches, halves, and quarters. The varnish has the good effect of preventing the length of such a measure being readily affected by variations in the humidity of the atmosphere, &c.; and it has little or no elasticity. In this part of the experiment then I can pretend to considerable accuracy. I took first the greatest circumference of the head from the most prominent part of the occiputational dimensions.

dimension from the superior and anterior part of one ear, across the fontanelle, to a fimilar part of the opposite ear. These dimensions appeared to me the most likely to afford data for determining the respective sizes of the brain in the different sexes. The refult was as tollows:

r	wenty male	es.	Tw	Twenty females.					
	Circum erence		Weight.	Circumf.	Dimen.from				
lbs. &c.	of heads.	from ear to ear.	lbs. &c.	of heads.					
	Inches.	Inches.		Inches.	Inches.				
		Experim	ent I.						
149½	282	152	137 <del>4</del>	272	143				
		Experime	ent 2.						
144 <u>1</u>	277	146 <del>1</del>	135	272	147				
		Experim	ent 3.		_				
148	280	147 <u>±</u>	132	273	143∓				
		Tota	als.		_				
442	839	445≩	404₹	817	433 <sup>‡</sup>				
		Average we	_						
7 lbs. 5 oz.	7 dr. 14	7 <del> </del>	6 lbs. 11 oz. 6	ir. 13\f	75				

Having found the relative proportions between the fexes to turn out thrice with fo much uniformity, and observing them to correspond pretty nearly with some experiments, made for very different purposes by the late Professor Roederer, of Gottingen, I did not think it necessary to prosecute the subject farther.

Upon the whole, it may be observed, that the difference of weight between the male and female at birth may be rated at about nine ounces, or nearly a twelfth part of the original weight. In the circumference of their heads there is a difference of near half an inch, or about a 28th or 30th part; and the same proportion of a 28th is pretty nearly preserved in the transverse dimension. It is evident, as the bony passage through

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through which infants pass is of a certain determined capacity, that, were their heads equally incompressible with those of adults, the difference of half an inch in their size would often prove fatal to them. By the compressibility of their heads, however, in well formed women, this difficulty is by time surmounted. The effects which such a compression on the brain may produce, have not hitherto been well attended to.

In reckoning children, weighing from 5½ to 6½, 6 pounds weight, and from 6½ to 7½, 7, and so forth, in order to avoid fractions, I find the numbers of males and females, arranged according to their weight, to stand as follow.

${f M}$ ales.						Females.								
lbs.	4	5	6	7	8	9	10 lbs.	4	5	6	7	8	9	10
							I Nº							

Hence it appears, that the majority of males runs thus: feven, eight, fix, five; whilft that of the females is feven, fix, five, eight. Hence also appears the merciful dispensations of Providence towards the female sex; for when deviations from the medium standard occur, it is remarkable, that they are much more frequently below than above this standard. In 120 instances there are only five children exceeding eight pounds and a half in weight. The same may be observed with regard to the size of their heads. Only six measured above 14½ inches in circumference, and these all of the male sex; sive measured 14½, and one 15. In transverse dimensions only four exceeded 7½, the largest of which was 8½; whereas deviations under the standard in these particulars were very numerous, never however under 12 around and 6½ across.

In the year 1753, Dr. Roederer published a Paper, De pondere et longitudine Insantum recens natorum, in the Commentaries of the Royal Society of Gottingen, of which the celebrated HALLER was the principal institutor, and long the prefident. In this Paper he proves, in the clearest manner, by incontestible experiments, the absurdity of the ideas of obstetric writers with regard to the progress of the ovum during gestation, and the weight of the fœtus after birth. He shews, although they state the weight of the fætus, come to the full time, to be from 12 to 14 or 16 pounds, that it is more generally 6 or 7, and very rarely exceeds eight. This deferves particular notice for two reasons; first, because it serves to shew how little dependence is to be placed on the affertions of authors who copy each other fervilely, without having recourse to experiment even in the most obvious cases; and, secondly, because this paper has been overlooked by some of the most celebrated writers and teachers of midwifry now living. What idea are we to form of the accuracy of one of our latest fystematic writers, who (telling us that he has been a practitioner of midwifry, in a capital city, for twenty years, and a teacher for more than twelve) states, in one page of his work, that the weight of a fœtus at eight months is about feven pounds; and on the opposite page, that at full time it weighs from twelve to fourteen pounds \*?

Of 27 children, carried to the full period of gestation, weighed and measured in length by ROEDERER, without any attention to the difference of sex, I find, that 18 were of the male and 9 of the semale sex; and that the average weight of

<sup>\*</sup> See a Treatife of Midwifry (p. 88. and 89.) diverted of technical terms and abstruct theories, by A. Hamilton, M. D. 8° edit. London, 1781.

the former was about 6 lbs. 9 oz., that of the latter about 6 lbs. 2 oz. 2 dr. Whether he and I used the same weights, I cannot exactly say. He observes, that he used the civil pound of Gottingen, which I can easily perceive consisted of 16 ounces, as mine did; but whether a German ounce be the same with ours, I have not daia to determine. The average length of the males measured by him is about 20½ inches, and of the semales about 19½. He weighed also the placentæ of 21 lying-in women, 16 of whom had borne male children, and sive semale. The average weight of the former was 1 lb. 2½ oz.; that of the latter 1 lb. 2 oz. Hence it appears, that in other circumstances, besides those I have taken notice of, the male and semale sex differ. So far I thought it necessary to take extracts from Dr. Roederer's paper, as his observations and mine throw light on each other, and add confirmation to both.

The limits of this letter will not permit me, Sir, to trespass much farther on your patience. There is one circumstance or two fo intimately connected with my former letter, that I cannot pass them over in silence. Having found that males suffer more in the birth than females, I was desirous of knowing whether the chance of the mother's recovery was thereby in any degree affected; and to determine this I was once more at the pains of turning over our registry with care. I found, that of 214 women, dead of fingle children, 50 were delivered of still-born males, and 15 of still-born females; 76 of living males, and 73 of living females. Of the 15 dead of twins, 6 had twins one of each fex; 6 others had twins both of the male fex; and three had twins both of the female fex. All of which twins (two or three excepted), it is very remarkable, furvived the death of their mothers. It would appear then, that the life of the mother is principally endangered Vol. LXXVI. Bbb

gered in those cases where the bulk of the male's head precludes the possibility of his being brought into the world alive, either by the efforts of nature or art. The conception of twins we have observed to be more fatal to the mother than that of single children. The average weight of 12 twins, which have occurred to me of late, I find to be 11 lbs. a pair. The largest pair weighed 13 lbs. and the least  $8\frac{1}{2}$ . From some rude attempts made to ascertain the weight of the contents of the gravid uterus in cases of twin and single children, I am inclined to think, that they are to each other as about 15 to 10, or perhaps  $14\frac{1}{2}$  to  $9\frac{1}{4}$ .

Believe me, Sir, with great respect, &c.

J. CLARKE.

Totals														Year ending 31 of December,	
	1784	1783	1782	1781	1785	1779	1778	1777	1776	1775	1774	1773	1772	1771	1770
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20625	- 1317	- 1230	1021	1079	967	1064	96 I	872	883	752	709	727	725	724	705
	<u> </u>	ı	1	1	ı	1	ı	J	ı	1	ı	ı	ı	ı	i
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	1	1	1	1	ı	j	i	1	I	I	ı	ı	ı	1	1
10647	642	632	549	598	499	550	476	452	418	364	357	367	368	370	372
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9470	640	553	458	447	143	475	450	375	407	378	33+	<u>د</u> به ۱	34.4	341	325
ış	1	l	ı	ı	7	1	ı	1	ı	ı	ı	1	1	)	ì
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3111	76	91	127	121	115	146	127	145	132	122	154	3	116	102	107
	1	ì	ı	1	ı	ı	ı	ı	ı	ı	ı	ı	1	ı	1
9001	68	72	57	38	41	59	39	35	_39	27	29	31	ಜ	4	37
	ı	ī	ī	ı	1	i	1	ı	ı	ı	ı	I	ı	ı	ı
229	11	Sı	6	6	٠	00	10	7	~T ·	(r	21	13	4	Un	တ

Proportion of males and females born, about nine males to eight females. women having twins, as one to about fixty. children still-born, as one to about twenty. children dying under fixteen days old, as one to about fix and a baff. women dying in child-bed, as one to about eighty-feven.

An Abstract of the Registry kept at the Lying in Hospital, in Dublin, from the 8th of December 31st of December, 1-84. By B. H. Register. 7:7 the

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ı		1766	1765	1764	1763	1762	1761	1760	1759	1758	From 8th to 31st of December, 1757	
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## Extracts from the Registry kept at the Lying-in Hospital, Dublin, from the year 1757 to 1784.

		U	niparo	18.	•		• •	1		ultiparous.	Twins, 7	riplets.	&c.		
Women.		•		Childr	en.			Women. Children.							
				Cimai	VIII			Delivered							
Delivered in Dead.		Sex.		De	ad.	Still-	born.	in	Dead,	Se	Χ.	Dead	i,	Still	botti.
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19455 214	10	305	9150	1656	1247	602	351	331	15	342	320	116	91	29	73
	91	50		1247		351				320		91		20	
	194	155		2903		953				662		207		49	
				953								49			
			Total	3856 d	ead and fti	l born.					Total	256 dead	and still	born.	
Inferences.				•				Inferences.		• • . • .	6 1 1				
1. Proportion					•	17 to 1	· .		portion of		o females borr under 16 days		•	17 to 16	
2. —— children dying under 16 days  children full-born				1 to 1 to 2	•	10		twins still-bo	•	, '		1 to 1	· _		
3. ——— children still-born  4. ——— males dying to femiles				4 to	•		-		lying to female			5 to 2	-		
5			to citto			12 to	7				fill-born to di			3 to 2	2
6	_ ftill-bo	n and d	ead of e	ach fex to	the whole	I to	5				dead of each	fex to the	whole	I to 2,	
7. —	- women	dying i	n child-b	ed	٠,	1 to 9	12	14. —		women dying	•	•	•	I to 2:	2
<b>.</b>	otals of dea	and G	:11 korn			Totale	of doad an	d flill-born when	ther		Totals of tw	ins. &c. d	ead and	ftill-born	
1	otals of qua Males.	n and it Fema						multiparous.	11104		4 0 4 10 10	Males.	Fema		•
	1656	124				-	Males.	Females.				116	91		
	602	35					1656	1247				29	20		
	2258	159	8				116	91				145	111		
	4434	-37	•				602	351			Born		41.4		
Born in hospital	10305	915					29	20		"hed	Born and fill-born		320 111		
Dead and still-box	n 2258	159	)8 				2403	1709				-	-	7	
Sent out living	8047	75	52			7	***	0.180	1	Se	nt out living	197	209		
	7552					Born 10647 2403		9470 1709					197		
Balance	495 in	favour	of the m	ale fex.			-	-	,	Balance	in favour of t	he female	sex 12		
							8244	7761							
							7761								

Of 20117 children born, at the end of a fortnight, there is only a balance of 483 in favour of the male fex, although originally 1177; greater loss of males 694.

XVIII. Some Particulars of the present State of Mount Vesuvius; with the Account of a Journey into the Province of Abruzzo, and a Voyage to the Island of Ponza. In a Letter from Sir William Hamilton, K. B. F. R. S. and A. S. to Sir Joseph Banks, Bart. P. R. S.

### Read May 4, 1786.

SIR.

Naples, January 24, 1786.

HE eruption of Mount Vesuvius, which began in the month of November 1784, nearly at the moment of my return from England to this Capital, and which continued in some degree till about the 20th of last month, has afforded much amusement to travellers unacquainted with this wonderful operation of nature, but no new circumstance that could justify my troubling you with a letter on the subject. The lava either overflowed the rim of the crater, or iffued from fmall fiffures on its borders, on that fide which faces the mountain of Somma, and ran more or less in one, and at times in three or four channels, regularly formed, down the flanks of the conical part of the volcano; fometimes descending and fpreading itself in the valley between the two mountains; and once, when the eruption was in its greatest force, in the month of November last, the lava descended still lower, and did some damage to the vineyards, and cultivated parts at the foot of Vesuvius, towards the village of St. Sebastiano; but generally the Bbb2

the lava, not being abundant, stopped and cooled before it was able to reach the valley. By the accumulation of these lava's on the flanks of Vesuvius, its form has been greatly altered; and by the frequent explosion of scorize and ashes, a considerable mountain has been formed within the crater, which now rifing much above its rim has likewise given that part of the mountain a new appearance. Just before I lest Naples, in May 1783, I was at the top of Vesuvius. The crater was certainly then more than 250 feet deep, and was impracticable, its fides being nearly perpendicular. This eruption, however, has been as fatisfactory as could be defired by the inhabitants of this city, a prodigious quantity of lava having been difgorged; which matter, confined within the bowels of the earth, would probably have occasioned tremors; and even slight ones might prove fatal to Naples, whose houses are, in general, very high, ill built, and a great number in almost every street already supported by props, having either suffered by former earthquakes, or from the loofe volcanic foil's having been washed from under their foundations by the torrents of rain water from the high grounds which furround Naples, and on which a great part of the town itself is built.

From the time of the last formidable eruption of Mount Vesuvius, in August 1779 (described in one of my former communications to the Royal Society) to this day, I have, with the affistance of the Father Antonio Piaggi\*, kept an exact diary of the operations of Vesuvius, with drawings, shewing, by the quantity of smoke, the degrees of fermenta-

<sup>\*</sup> This Padre Antonio Piaggi is the ingenious Monk who invented the method of unfolding and recovering the burnt ancient manuscripts of Herculaneum, and who resides constantly at Resina, at the foot, and in sull view, of Mount Vesuvius.

tion of the volcano; also the course of the lava's during this last eruption, and the changes that have been made in the form of the mountain itself by the lava's and scorize that have been ejected. This journal is becoming very curious and interesting; it is remarkably so with respect to the pointing out a variety of fingular effects that different currents of air have upon the smoke that issues from the crater of Vesuvius, elevated (as you. know, Sir) more than 3600 feet above the level of the fea; but, except the fmoke increasing considerably and constantly when the sea is agitated, and the wind blows from that quarter, the operations of Vesuvius appear to be very capricious and uncertain. One day there will be the appearance of a violent fermentation, and the next all is calmed again: but whenever the smoke has been attended with considerable ejections of scoriæ and cinders, I have constantly observed, that the lava has foon after made its appearance, either by boiling over the crater, or forcing its passage through crevices in the conical part of the volcano. As long as I remain in this country, and: have the necessary assistance of the above-mentioned ingenious Monk (who is as excellent a draughtsman as he is an accurate and diligent observer) the Vesuvian diary shall be continued; and I hope one day to have the honour of presenting these curious manuscripts (which begin now to be voluminous) to the Royal Society, if it should think them worthy of a place in the Library of the Society.

Having never had an opportunity of examining the islands of Ponza, Palmarole, Zannone, and other small islands, or rather rocks, situated between the island of Ventotiene and Monte Circello, near Terracina, on the Continent; and thinking that by a tour of these islands I should be enabled to render my former observations more complete, and to communicate

to you, Sir, some account of the only volcanic parts of this neighbourhood hitherto undescribed, I determined to take advantage of the absence of their Sicilian Majesties (who were then making the tour of Italy) and visit these islands. But before I put this plan in execution, I made a long excursion in the province of Abruzzo, as far as the Lake of Celano, anciently called Fucinus, and where the famous Emissary of the Emperor CLAUDIUS (a most stupendous work \* for draining that lake) remains nearly entire, though filled up with rubbish and earth in many parts, and of course useless. The water of this lake, which is more than 30 miles in circumference, increases daily, and is destroying the rich and cultivated plains on its borders. It is furrounded by very high mountains, many of them covered with fnow, and at the foot of them are many villages, and rich and well cultivated farms. Upon the whole it is the most beautiful lake I ever saw, and would be complete, if the neighbouring mountains were better wooded. This lake furnishes abundance of fish, but not of the best quality: a few large trout, but mostly tench, barbel, and dace. In the shallow water on the borders of the lake, I saw thousands of water fnakes, pursuing and preying upon a little fish like our thornbacks, but much better armed, though their defensive weapons seemed to avail them but little against such ravenous foes.

I went with torches into the emissary of CLAUDIUS as far as I could. It is a covered under-ground canal, three miles long, and great part of it cut through a hard rock; the other parts supported by masonry, with wells sunk to give air and light.

<sup>\*</sup> A description of this emissary of CLAUDIUS, with plans (though not very exact) has been published by Fabretti, in the same book in which he has given an account of Trajan's column.

According to Suetonius, Claudius employed thirty thoufand men eleven years on this great work, intended to convey the superfluous water of the lake into the bed of the river Liris, now called Garigliano; and I make no doubt, but that if it was cleared and repaired, it would again answer that purpose.

In its present state it is a most magnificent monument of antiquity.

The whole country from Arpino, the native place of MARIUS\*, by Isola, Sora, Civitella, and Capistrello, to the lake of Celano, is, in my opinion, infinitely more beautiful and picturesque than any spot I have yet seen on the Alps, in Savoy, Switzerland, or the Tyrol. The road is not passable for carriages, and indeed is scarcely so, even in summer, for horses or mules, and is often insested with banditti; a party of which, consisting of twenty-two, had quartered themselves in a village which I passed through, and left it but a week before my arrival. There are many wolves and some bears in the adjacent mountains, which also commit their depredations in the winter. The tyger-cat, gatto pardo, or lynx, is sometimes found in the woods of this part of Abruzzo.

The road follows the windings of the Garigliano, which is here a beautiful clear trout stream, with a great variety of cascades and water-falls, particularly a double one at Isola, near which place Cicero had a villa, and there are still some remains of it, though converted to a chapel. The valley is extensive, and rich with fruit trees, corn, vines, and olives. Large tracts of land are here and there covered with woods of

<sup>\*</sup> Marius had a large villa, about twelve miles distant from Arpino. I went to visit the spot, on which now stands the only convent of the austere order of La Trappe in Italy. It is in the Pope's state, and has been evidently built of the ruins of Marius's house, and its present name is Casa Mari.

oak and chestnut, all timber trees of the largest size. The mountains nearest the valley rise gently, and are adorned with either modern castles, towns, and villages, or the ruins of ancient The next range of mountains, rifing behind these, are covered with pines, larches, and fuch trees and shrubs as usually abound in a like situation: and above them a third range of mountains and rocks, being the most elevated part of the Apennine, rise much higher, and, being covered with eternal fnow, make a beautiful contrast with the rich valley above-mentioned; and the fnow is at fo great a distance, as not to give that uncomfortable chill to the air, which I have always found in the narrow vallies of the Alps and the Tyrol. Excuse me, Sir, if from the impression which this enchanting and little frequented country has left on my mind, I have been led to depart from the subject of this letter, to which I will return directly.

On the 15th of August last I went in a felucca to the island of Ischia. I have nothing to add to my former observations on this island, already communicated to the Royal Society; except that about fixty yards from the shore, at a place called St. Angelo, fituated between the towns of Ischia and Furia, a column of boiling water bubbles upon the furface of the fea with great force, and communicates its heat to the water of the sea near it; but as the wind was very high, and the furf confiderable, I was not able then to examine this curious fpot as I could have wished, but will return there on purpose some other time. The inhabitants of the neighbourhood told me, that it always boiled up in the fame manner, winter and fummer; and that it was of great use to them in bending their planks for ship-building; and that the fishermen also frequently made use of this natural cauldron to boil their fish. Though I have

have passed at different times many weeks in the island of Ischia, I never before heard of this phænomenon; but in my description of this island mention is made of several spots where, near the shore, I had found, when bathing in the fea, the fand under my feet so hot as to oblige me to retire hastily. This boiling fpring reminds me of one near Viterbo in the Roman State, which I have feen, and is called the Bulicame. It is a circular pool of about fixty feet in diameter, and exceedingly deep, the water of which is conftantly boiling. It is fituated in a plain furrounded by volcanic mountains. stony concretion floats on the furface of the pool, which being carried off by the superfluous water is deposited, and is constantly forming a labes or tuffa, of which all the soil around the pool is composed. You have seen, Sir, the like operation in greater perfection in Iceland, at the famous boiling spring of Geyfer. I am convinced, that many of the finer fort and most compact tuffa's we meet with, in countries formed by volcanoes, have been produced in the same manner.

The 18th of August I arrived at the island of Ventotiene, about twenty-five miles from Ischia. It is greatly improved fince my former visit, seven or eight years ago, when his Sicilian Majesty first planted a little colony there. It then produced neither corn nor wine; now it furnishes annually at least feventy butts of wine and two thousand tomoli of corn. The foil is remarkably fertile, from whence it probably took its ancient Greek name of Pandataria. This island contains at present more than three hundred inhabitants. The island of Ventotiene, and the smaller one called St. Stefano, within a mile of it, having been described in my Campi Phlegræi, as being both entirely composed of volcanic matter, I need not trouble you further on their fubject; I will only mention a curious Ccc Vol. LXXVI.

curious circumstance in the natural history of birds, of which I was informed by an officer of the garrison of Ventotiene, who is a great sportsman, and shoots often in the island of St. Stefano, inhabited only by hawks, and a large kind of feagulls; but is occasionally visited, as a resting place, by divers forts of birds of passage. In the month of May great slights of quails arrive there from Africa, spent with fatigue; and many of them fall an eafy prey for the hawks and fea-gulls; but, as their arrival depends upon one prevailing wind, there is often an interval of many days between one flight and another. My informer affured me, that the hawks constantly, during the flights, make a provision of each day's prey, laying them up in separate heaps of fix or seven near their haunts, always feeding first upon those of the oldest date. The sea-gulls have not the same foresight, but greedily fall upon their unhappy yictims in their languid state before they reach the shore, and, having beat them down into the fea, swallow numbers of them whole. Extraordinary as this may appear, yet as facts related by persons of credibility in any branch of natural history are always pleafing, I thought you would excuse this digreffion. Give me leave likewise to add, for the information of the curious in antiquities, that, during my stay in the island of Ventotiene, I got out of the ruins of an elegant ancient bath (supposed to have been built for the use of Julia, daughter of Augustus, whilst she was in exile here) a fragment of a tile, on which are stamped the following characters in basso relievo,

> HACINI IVLIAI AVGVS. F

which, according to the interpretation of a celebrated antiquary at Naples, mean Opus HACINI ad commodum Balnei Julia Augusta factum. I was informed, that several entire tiles. tiles, with a like inscription, had been dug up on the same spot, and had been made use of in building the church and barracks newly erected in this island. Another fragment of a tile was likewise found here, and given to me, with the following inscription:

#### SAB. A PI.

which the same antiquary explains, SABINAE AVGVSTAE, Pize Imperatrici dicatum Balneum; but, I believe, there is no mention in ancient authors of SABINA having been at Pandataria: of Julia's banishment to this island there can be no doubt.

Between Ventotiene and the island of Ponza, and from the latter at the distance of about twelve miles, a group of rocks rise several feet above the surface of the sea. They are called the *Botte*, and are composed of a compact lava; probably they are the small remains of another volcanic island, the softer parts of which may have been carried off and levelled by the action of the sea, which is open and violent here.

The 20th of August I arrived at the island of Ponza, about thirty miles from Ventotiene, and the next day I went round it in my boat. It is near five miles long: its greatest breadth not more than half a mile, and in some parts not more than five hundred feet. It is furrounded by innumerable detached rocks, some of them very high, and most of which are of lava; in many are regularly formed basaltes, but none in large columns. In some parts the basaltes have a reddish tint of iron ochre, are very small, and irregularly laid one over another. Some masses of them are in a perpendicular, others in an horizontal, and others again in an inclined position: and the rocks themselves, in which these masses are found, are lava of the same nature as the basaltes. At first sight these rocks have very much the appearance of the ruins of ancient Roman brick Ccc2

brick or rather tile buildings, as may be feen in the drawing (fee Tab. XI. fig. 1.) taken on the spot. One rock, as appears in the drawing (see Tab. XII fig. 4.) is composed of large fpherical basaltes; and in many parts of the island I found the lava had inclined to take the like ipherical form, though on a much smaller scale, some of the first mentioned round basaltes being near two feet in diameter. All these rocks have certainly been detached by the action of the fea from the island, which is intirely composed of volcanic matter, lava's, and tuffa's, of various qualities and tints, green, yellow, black, and white. Some of the tuffa's, as well as the lava's, are of a texture more compact than others; and in some parts of the island great tracts feem to have undergone the same operation as is mentioned in one of my former communications to be in full force at a fpot called the Pifciarelli, on the outfide of the Solfaterra, near Puzzole, and where a hot fulphureous vitriolic acid vapour converts all which it penetrates, whether lava's, tuffa's, volcanic ashes, or pumice stones, into a pure clay, mostly white, or with a light tint of red, blue, green, or yellow. The appearance of a tract of volcanic country, which has undergone this operation, is well expressed in the view of the infide of the harbour of Ponza (Tab. XI. fig. 2.). But I was fo struck with the beautiful and uncommon appearance of one of these high volcanic grounds converted to a pure lightcoloured clay (Tab. XII. fig. 1.) in contrast with a neighbouring dark basaltic rock, that I caused the drawing, which accompanies this letter (see Tab. XII.) to be made on the spot. You, Sir, who have feen fuch a variety of countries, will still think this view fingular and beautiful. I can affure you, it is very exact, except the rock of round basaltes (fig. 4.) which, in nature, is at a distance from this spot, and only placed here

to illustrate what I have written on its subject. In one part of the island there is a fort of tuffa, remarkably good for the purpose of building. It is as hard as our Bath stone, and nearly of the same colour, without any mixture of fragments of lava or pumice stone, which usually abound in the tuffa's in the neighbourhood of Naples, Baia, and Puzzole.

The drawing (see Tab. XI.), which is a view of the harbour of Ponza, will give you a very good idea of the appearance of the isolated rocks of lava and basaltes which have been separated, by the force of the sea, from the softer parts of the island, and of which there are an infinite number, as you will see in the exact geometrical plan of the island of Ponza (Tab. X.), which likewise accompanies this letter.

When I was last in England, I inquired of many of the manufacturers of glass, whether it had ever happened, that the glass cooling in their furnaces had taken any distinct forms like prisms or crystallizations; but I got no satisfactory answer until I applied to the ingenious Mr. PARKER, of Fleet-street, who not only informed me, that, some years ago, a quantity of his flint glass had been rendered unserviceable by taking fuch a form in cooling; but also gave me several curious specimens of the glass itself: some of them are in laminæ, which may be easily separated; and others resemble basaltic columns in miniature, having regular faces. I was much pleafed with this discovery, proving to me, beyond a doubt, the volcanic origin of most basaltes. Many of the rocks of lava of the island of Ponza are, with respect to their configurations, strikingly like the specimens of Mr. PARKER's above-mentioned glass, none being very regularly formed basaltes, but all having a tendency towards it. Mr. PARKER could not account for the accident that occasioned his glass to take the basaltic forms:

forms; but I have remarked, both in Sicily and at Naples, that such lava's as have run into the sea, are either sormed into regular basaltes, or have a great tendency towards such a form. The lava's of Mount Etna, which ran into the sea near lacci, as appears in my account of them in the Campi Phlegræi, are perfect basaltes; and a lava that ran into the sea from Mount Vesuvius, near Torre del Greco, in 1631, has an evident tendency to the basaltic forms. On Mount Vesuvius I never found any thing like columns of basaltes, except the abovementioned at Torre del Greco, and some fragments of very complete ones, which I picked up near the crater, after the eruption of 1779, and which had been thrown out of the mouth of the volcano.

The island of Palmarole, which is about four miles from Ponza, is not much more than a mile in circumference, is composed of the same volcanic matter, and probably was once a part of Ponza; and indeed it appears as if the island of Zannone, which lies at about the same distance from the island of Ponza, was once likewise a part of the same island of Ponza; for many rocks of lava rise above water in a line between the two last mentioned islands, and the water is much shallower there than in the other parts of the gulph of Terracina.

The island of Zannone is larger and much higher than Palmarole, and the half of the island nearest the Continent is composed of a lime-stone, exactly similar to that of the Apennines, on the Continent near it; the other half is composed of lava's and tuffa's, resembling in every respect the soil of the other islands just described. Neither Palmarole nor Zannone are inhabited; but the latter furnishes brushwood in abundance for the use of the inhabitants of Ponza, whose number, including the garrison, amounts to near seventeen hundred.

The uninhabited island of St. Stefano furnishes fuel in the like manner for the inhabitants of Ventotiene.

It is probable, that all these islands and rocks may in time be levelled by the action of the sea. Ponza, in its present state, is the mere skeleton of a volcanic island, as little more than its harder vitristed parts remain, and they seem to be slowly and gradually mouldering away. Other new volcanic islands may likewise be produced in these parts.

The gulphs of Gaeta and Terracina may, in the course of time, become another Campo Felice \*; for, as has been mentioned in one of my former communications on this subject. the rich and fertile plain fo called, which extends from the bay of Naples to the Apennines, behind Caserta and Capua. has evidently been intirely formed by a fuccession of such volcanic eruptions. Vefuvius, the Solfaterra, and the high volcanic ground, on which great part of this city is built, were once probably islands; and we may conceive, the islands of Procita, Ischia, Ventotiene, Palmarole, Ponza, and Zannone, to be the outline of a new portion of land, intended by nature to be added to the neighbouring Continent; and the Lipari islands (all of which are volcanic) may be looked upon in the same light with respect to a future intended addition of territory to the island of Sicily. If you cast your eye, Sir, on. the map at the head of my description of the Campi Phlegræi, you will better understand my meaning.

<sup>\*</sup> The governor of the castle of Ponza, who has resided there sifty-three years, told me, that the island was still subject to earthquakes; that there had been one violent shock there about four years ago; but that the most violent one he ever felt there was on the very day and hour of the great earthquake which destroyed Lisbon; that two houses out of three, which were then on the island, were thrown down. This seems to prove, that the volcanic matter, which gave birth to these islands, is not exhausted.

The more opportunities I have of examining this volcanio country, the more I am convinced of the truth of what I have already ventured to advance, which is, that volcanoes should be considered in a creative rather than a destructive light. Many new discoveries have been made of late years, particularly, as you well know, Sir, in the South-Seas, of islands which owe their birth to volcanic explosions; and some, indeed, where the volcanic fire still operates. I am led to believe, that upon further examination, most of the elevated islands at a confiderable distance from Continents would be found to have a volcanic origin; as the low and flat islands appear in general to have been formed of the spoils of sea productions, such as corals, madrepores, &c. But I will stop here, and not deviate from the plan which I have hitherto strictly followed, of reporting faithfully to my learned Brethren of the Royal Society fuch facts only as come immediately under my own obfervation, and as I think may be worthy of their notice, and leave them at full liberty to reason upon them.

We may flatter ourselves, as a very great progress has been made of late years in the knowledge of volcanoes, that by combining such observations as we are already in possession of, with those which may be made hereafter, in the four quarters of the world (in all of which nature seems to have operated in a like manner), a much better theory of the earth may be established than the miserable ones that have hitherto appeared.

Those who have not had an opportunity of examining a volcanic country, as I have for more than twenty years, would little suspect, that many curious productions and combinations of lava's and tussa's were of a volcanic origin; especially when they have undergone various chemical operations of nature, some of which, as I have mentioned in a former

communication, as well as in this, have been capable of converting tuffa's, lava's, and pumice stone, into the purest clay.

I have remarked, that young observers in this branca of natural history are but too apt to fall into the dangerous error of limiting the order of nature to their confined ideas: for example, should they suspect a mountain to have been a volcano, they immediately climb to its summit to seek for the crater, and if they neither find one, or any figns of lava or pumice stone, directly conclude such a mountain not to be volcanic: whereas, only suppose Mount Etna to have ceased erupting for many ages, and that half of its conical part should have mouldered away by time (which would naturally be the confequence) and the harder parts remain in points, forming an immense circuit of mountains (Etna extending at its basis more than one hundred and fifty miles); such an obferver as I have just mentioned would certainly not find a crater on the top of any of these mountains, and his ideas would be too limited to conceive, that this whole range of mountains were only part of what once constituted a complete cone and crater of a volcano. It cannot be too strongly recommended to observers in this, as well as in every other branch of natural history, not to be over-hasty in their decisions, nor to attribute every production they meet with to a fingle operation of nature, when perhaps it has undergone various, of which I have given examples in the island which has been the principal subject of this letter. That which was one day in a calcareous state, and formed by an insect in the sea, becomes vitrified in another, by the action of the volcanic fire, and the addition of fome natural ingredients, fuch as fea falts and weeds, and is again transformed to a pure clay by another curious process Vol. LXXVI. Ddd

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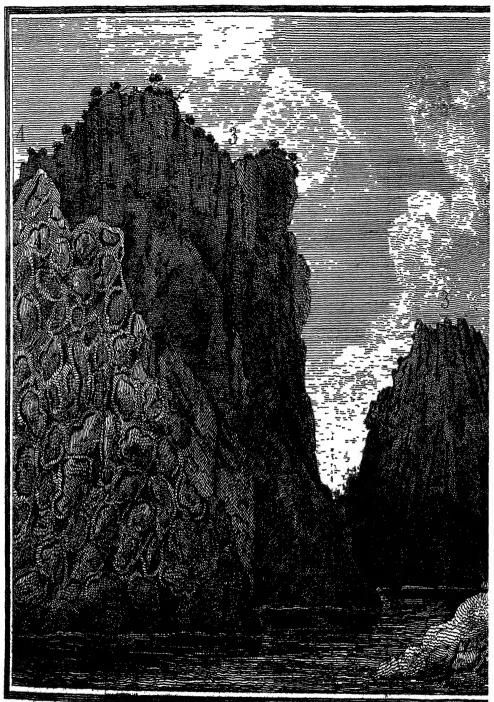
of nature. The naturalist may indeed decide as to the present quality of any natural production; but it would be presumption in him to decide as to its former states. As far as I can judge in this curious country, active nature seems to be constantly employed in composing, decomposing, and recomposing; but surely for all-wise and benevolent purposes, though on a scale perhaps much too great and extensive for our weak and limited comprehension.

I have the honour to be, with great regard and esteem, &c.

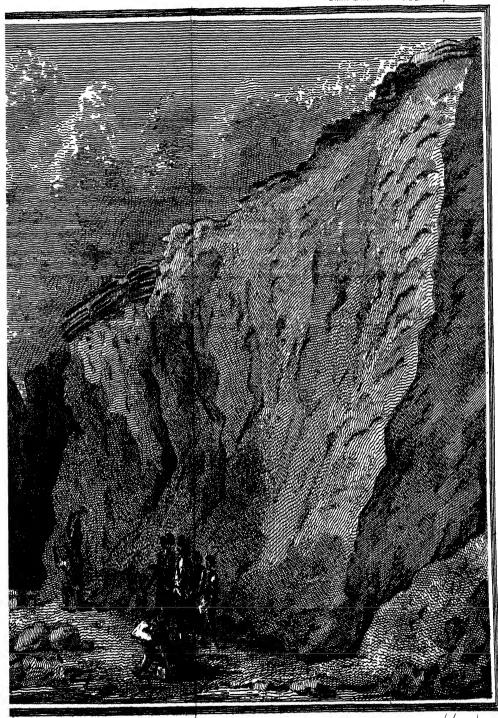
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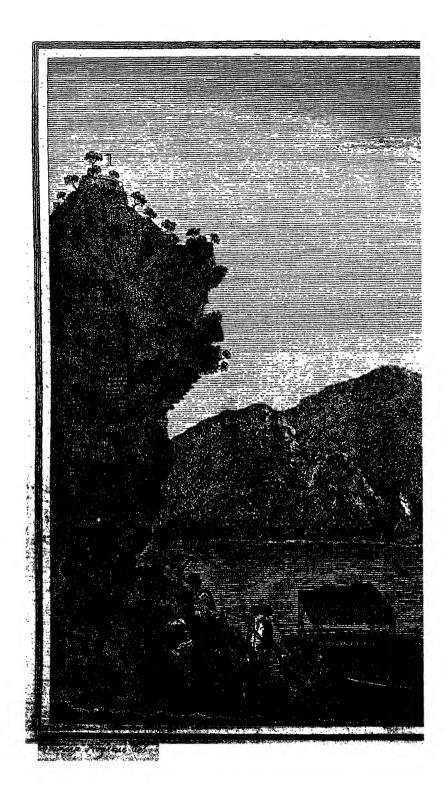
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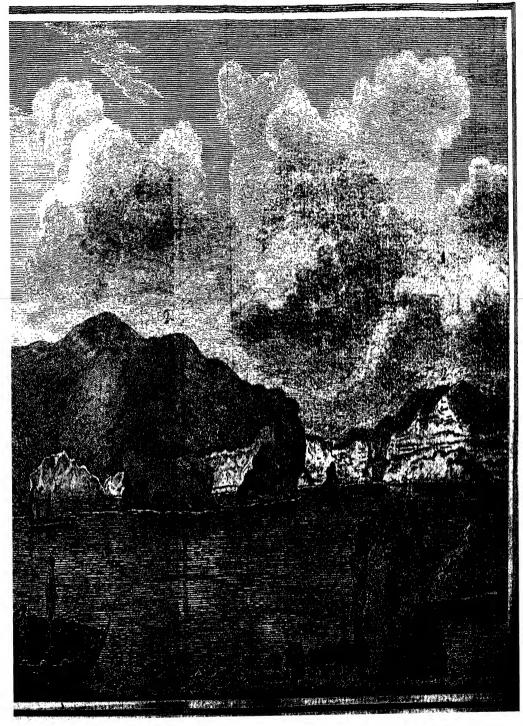
THE earth is not yet so perfectly quiet in Calabria and at Messina, as to encourage the inhabitants to begin to rebuild their houses, and they continue to live in wooden bar-There has, however, been no earthquake of confequence during these last three months. My conjecture, that the volcanic matter (which was supposed to have occasioned the late earthquakes) had vented itself at the bottom of the fea between Calabria and Sicily, seems to have been verified; for the pilot of one of his Sicilian Majesty's sciabecques, having fome time after the earthquakes cast anchor off the point of Palizzi, where he had often anchored in twenty-five fathom water, found no bottom till he came to fixty-five fathom, and having founded for two miles out at fea towards the point of Spartivento in Calabria, he still found the same considerable alteration in the depth of the sea. The inhabitants of Palizzi likewise declare, that during the great earthquake of the 5th of February, 1783, the fea had frothed and boiled up tremendoully off their point.

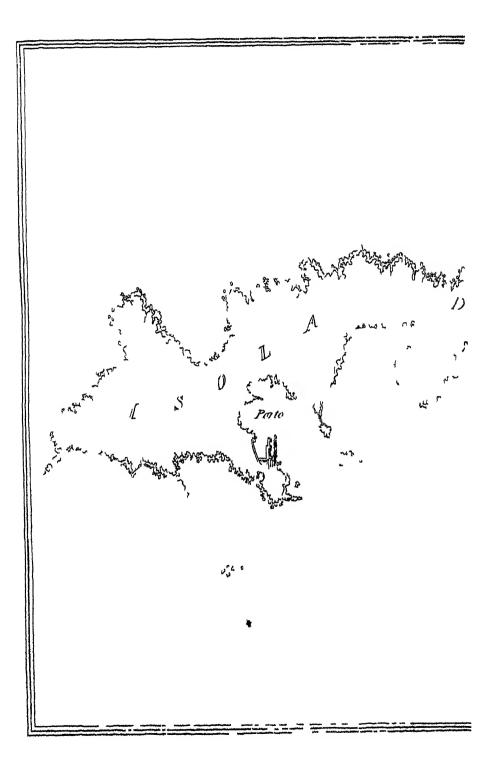


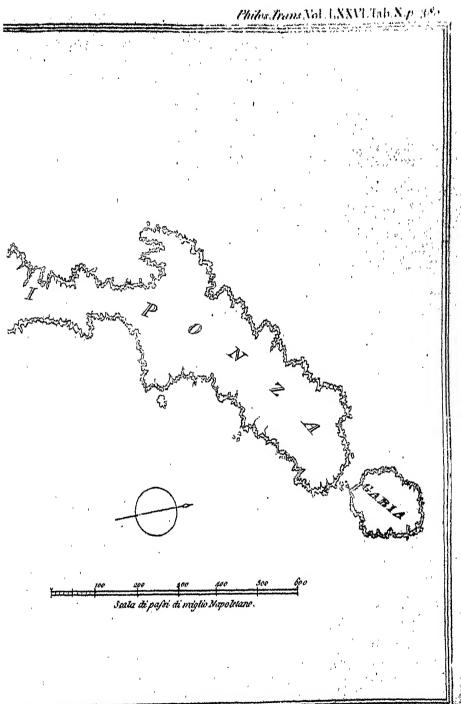
Francist Prager













#### EXPLANATION OF THE PLATES.

- Tab. X. Plan of the island of Ponza.
- Tab. XI. View of part of the infide of the harbour of the illand of Ponza.
  - Fig. 1. Rock of lava, which in many parts is formed into regular small basaltes of a reddish cast, having probably been tinged with some ochre. Most of the detached rocks of this island resemble this.
  - Fig. 2. See p. 374.
- Tab. XII. View taken from the outside of the harbour of the island of Ponza, near the Lighthouse.
  - Fig. 1. Rock of volcanic matter converted to pure clay.
    - 2. Ditto, with strata of pumice-stone.
    - 3. Rocks of lava inclining to take basaltic forms
    - 4. Rock composed of spherical basaltes.



XIX. An Account of a new Electrical Fish. In a Letter from Lieutenant William Paterson to Sir Joseph Banks, Bart. P. R. S.

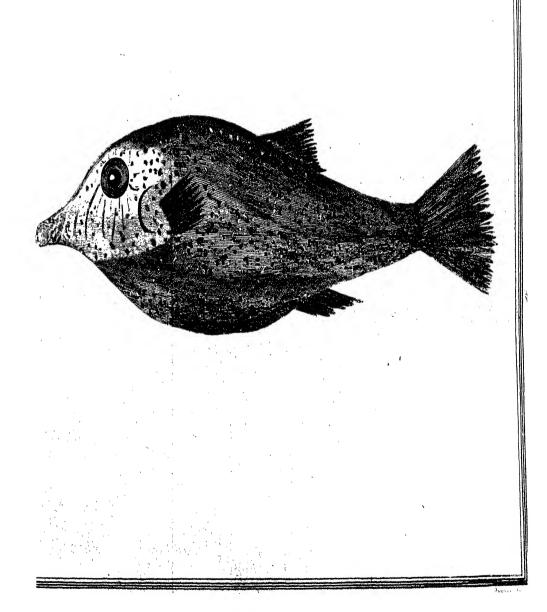
## Read May 11, 1786.

5 1 R,

WHILE at the island of Johanna, one of the Comoraislands, in my way to the East-Indies, with the 98th
Regiment, I met with an electrical fish, which has hitherto
escaped the observation of naturalists, and seems in many respects to differ from the electrical fishes already described;
which induces me to send you the following account of it,
with a very impersect Drawing, and to beg that, if you think
it deserves attention, you will do me the honour of presenting
it to the Royal Society. The situation of a subaltern officer,
in an army upon foreign service, will, I hope, sufficiently
apologize for my sending you so very impersect a sketch of
the sish, which was made in the field, in a hot climate, under
every disadvantage.

The fish is seven inches long, two inches and a half broad, has a long projecting mouth, and seems to be of the genus Tetrodon. The back of the fish is a dark brown colour, the belly part of sea-green, the sides yellow, and the fins and tail of a sandy green. The body is interspersed with red, green, and white spots, the white ones particularly bright; the eyes large, the iris red, its outer edge tinged with yellow. (See Tab. XIII.)

The



The island of Johanna is situated in latitude 12° 13' fouth. The coast is wholly composed of coral rocks, which are in many places hollowed by the fea. In these cavities I found feveral of the electrical fishes. The water is about 56° or 60° of heat of FAHRENHEIT's thermometer. I caught two of them in a linen bag, closed up at one end, and open at the other. In attempting to take one of them in my hand, it gave me fo fevere an electrical shock, that I was obliged to quit my hold. I however fecured them both in the linen bag, and carried them to the camp, which was about two miles diffant. Upon my arrival there, one of them was found to be dead, and the other in a very weak state, which made me anxious to prove, by the evidence of others, that it possessed the powers of electricity, while it was yet alive. I had it put into a tub of water, and defired the Surgeon of the regiment to lay hold of it between his hands; upon doing which he received an evident electrical stroke. Afterwards the Adjutant touched it with his finger upon the back, and felt a very slight shock, but sufficiently strong to ascertain the fact.

After so very impersect an account, I will not trouble you with any observations of my own upon this singular sish; but beg you will consider this only as a direction to others who may hereafter visit that island, and from their situation, and knowledge in natural history, may be better able to describe the fish, and give an account of its electrical organs.

I have the honour to be, with great esteem, &c.

W. PATERSON, Lieutenant 98th regiment.



XX. Observation of the Transit of Mercury over the Sun's Disc, made at Louvain, in the Netherlands, May 3, 1786. By Nathaniel Pigott, Esq. F. R. S.

## Read June 15, 1786.

Louvain, May 15, 1786.

THE transit of Mercury was to happen a few days after my arrival at this place from England. Although I brought no astronomical instruments with me, I wished to observe this phænomenon; and upon application to M. THYSBAERT, Président du Collège Royal, a very distinguished Member of this University, he supplied me, in the politest manner, with the following instruments, and a convenient place for the obfervation. He carried his attention to the most trifling circumstances, in order to make my situation, in every respect, agreeable. The inftruments he provided me with were a Gregorian reflector of 21 inches focal length, with an aperture of 41 inches, the magnifying power of which I esteemed about 70 or 80, with a good quadrant 18 inches radius, and a compound pendulum clock, steadily fixed, beating dead seconds. These instruments were made in London, and used for the observation

Mr. N. PIGOTT's Observation of the Transit of Mercury. 385 observation of Mercury. The rate of the clock, and the apparent times thence deduced, were obtained by equal altitudes of the fun, taken with the quadrant. These were the only instruments I had, and therefore such observations as are not dependent on the measure of time, are to be considered as made by estimation; however, the most important, the internal and external contacts of Mercury, and hence the egress of his center and the interval of time between the two contacts, were made in a very fatisfactory manner. About fix o'clock, when I attended for the observation, there being a great number of folar spots, Mercury might easily have been mistaken for one; but his motion foon removed every doubt in that respect. Flying clouds obscreed the sun at intervals; but during the last half hour, the weather was fine, the sky clear, the limb of the fun well defined; Mercury round and very black. There feems to have been some mistake, in respect of this phænomenon, either in the calculation or the printing of the Connoissance des Temps of this year: the emersion of the center of Mercury is there set down at 19 h. 45' apparent time at Paris; whereas, by my observation, the egress of the center at Louvain was at 20 h. 47' 28" or 29" apparent time. Taking here no other equation into confideration, except the difference of meridians between Paris and Louvain, which, by a great number of observations, I determined in 1775 to be 9' 37" in time \*, the emersion of the center at Paris must have been at 20 h. 37' 51" or 52", which differs nearly 53' from the computed time. By the same reasoning, I should suppose, that the emersion of the center of Mercury at Greenwich was obferved at 20 h. 28' 35" or 36". Mercury being so very near

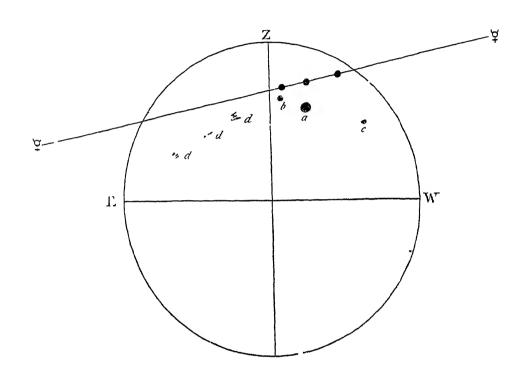
<sup>\*</sup> See Philosophical Transactions, vol. LXVIII. p. 654.

the earth, the effects of parallax must be considerable, and the western situation of Greenwich of 18' 53" in time from this place, must occasion a retardation, which, on computation, may be hereafter allowed for, and added to the supposed time of the egress above-mentioned, deduced from my observation here.

While I am writing this Paper, the respective situation of Greenwich and Louvain strikes me. The latitude of Greenwich is 51° 28′ 40″, that of Louvain 50° 53′ 3″\*; the difference little more than half a degree. Greenwich is 9′ 16′ west, and Louvain 9′ 37″ east of the Paris Observatory; the parallax above-mentioned is therefore nearly, but in a contrary sense, equal at the two places, and thus the effects of both are compensated relatively to Paris. What other advantage may result from this circumstance, would require consideration. I have not leisure, at present, to revolve it in my mind, as I am desirous to lay this Paper before the Royal Society as soon as I can, by the favour of Dr. Maskelyne, our Astronomer Royal.

<sup>\*</sup> See Philosophical Transactions, vol. LXVIII. p. 643.

## Observations of the Transit of Mercury at Louvain.



### Apparent time.

- H. M. S.
- 18 32 30 flying clouds; Mercury ill defined, with some twifting.
- 19 13 30 the fpot (a) appears thrice as large as Mercury; fpot (b) twice ditto.
- 19 16 30 a perpendicular from the fun's limb on E. W. bisects Mercury and (b).
- 19 27 30 perpendicular, as above, equi-distant from (a) and (b).

  Vol. LXXVI. E e e Apparent

Apparent time.

H. M. S.

19 34 30 perpendicular, as above, bisects Mercury and spot (a).

19 42 30 perpendicular from Mercury on E. W. is beyond ipot (.1).

19 45 30 it is sensibly beyond spot (a).

20 12 30 perpendicular from the fun's limb on E. W. equidistant from (a) and (c).

20 27 30 Mercury very black, round and well defined.

20 45 41 internal contact; perhaps a few feconds too foon.

20 47 26 emersion of center by estimation.

20 49 16 external contact.

20 49 41 Mercury certainly clear of the fun.

a. b. c. d. d. are spots in the sun; Z. zenith; E. East; W. west of the solar disc.

The internal contact being at 20 h. 45' 41", and the external at 20 h. 49' 16", the emersion of the center of Mercury must have been at 20 h. 47' 28"½; which differs only 2½ feconds from the estimated time; and the duration of total egress was 3 m. 35 s.

N. B. The reasons why the nine first observations are all marked at 30" is, that in reality they were set down at the minute only; and that I have added 2'30" to each to reduce the time by the clock to apparent time; more nicety would have been superfluous; but the four last were rigorously computed.



XXI. Observation of the late Transit of Mercury over the Sun, observed by Edward Pigott, Esq. at Louvain in the Netherlands; communicated by him in a Letter to Nevil Maskelyne, D. D. F. R. S. and Astronomer Royal.

## Read June 15, 1786.

S I R, Louvain, May 27, 1786.

WE have been fortunate here in seeing Mercury's egress.
I observed it thus:

Apparent time, May 3.

H. M. S.

20 45 25 Mercury's limb in contact with the fun's limb; uncertain.

20 45 37 ditto ditto; certain.

20 47 17 Mercury bisected by the sun's limb.

20 49 22 Mercury quite out; clouds for a short interval, which renders the observation rather doubtful.

Though the air was not perfectly free from thin clouds, nevertheless the limbs were well defined. At 20 h. 45' 25", when I first judged Mercury's limb in contact with the sun's, his form, I think, became rather oval. These observations were made with RAMSDEN's two-feet achromatic, magnifying about 70 times. The above times disagreeing so considerably with the tables will, I imagine, not a little surprise M. DE LALANDE.

I remain, Sir, with great regard, &c.

EDW. PIGOTT.

XXII. Additional Observations on making a Thermometer for measuring the higher Degrees of Heat. By Mr. Josiah Wedgwood, F. R. S. and Potter to Her Majesty.

## Read June 22, 1786.

If thermometer for measuring the higher degrees of heat having been honoured with the notice of this illustrious Society, I now request a further indulgence for a few more observations on the same subject.

In my first Paper \* I communicated every thing that experience had then taught me, respecting both the construction and use of this thermometer; but more extensive practice has since convinced me, that other managements and precautions are necessary, in order to bring it to the perfection it is capable of receiving: for pieces made of the same clay, and exactly of the same dimensions, have been found to differ in the degree of their diminution by fire, in consequence of some circumstances in the mode of their formation, at that time unheeded, and very difficult to be developed.

Of the two ways proposed for forming them, the mould and the press, the former was made choice of, as being, for general use, the most commodious. The soft clay was pressed into a square mould with the singers; and the pieces, when dry, were pared down on two opposite sides, by means of a

<sup>\*</sup> Philosophical Transactions, Vol. LXXII.

paring gage made for that purpose, so as to pass exactly to o at the entrance of the converging canal of the menture g gage.

But the pieces thus formed have been found lithle, in passing through strong sire, to receive a little alteration in their signre, which produces an uncertainty with respect to their so nequent measurement: the two sides, instead of continuing slat, become concave; the edges, both at top and bottom projecting beyond the middle part, sometimes very considerably, as at a and b, sig. 1. (Tab. XIV) where AB represents a perpendicular section of an unburnt piece, and ab a like section of the same piece after it has undergone a heat of 160 degrees. This irregularity in the form, which is sensible only after passing through the high degrees of sire, was observed in some of the early experiments, but was not then looked upon as being productive of any error.

On more attentively examining this matter, it appeared, that when the clay is pressed into a mould, the surface in contact with the mould acquires a more compact texture than the inner part of the mass; -that this compactness restrains, in some degree, its diminution in the fire; -- and therefore, that when this furface, or less diminishable crust, is pared off from the two fides only, the piece may be confidered as having its upper and lower strata (AA and BB, fig 1.) composed of a less diminishable matter than the intermediate part, the necessary consequence of which structure will be such a figure as we find the pieces to assume; for if any stratum in the mass shrinks less than the rest, the extremities of that stratum must be lest proportionably prominent. That this was the true cause of the inequality, I was convinced by firing some pieces unadjusted, with all their surfaces entire, as they came from the mould; for these pieces, after passing through the same strong fires with the preceding, continued flat, with the angles regularly sharp, and without the least sensible prominence in any part.

Some of the moulds, employed for this use, were made of plaster, a material more convenient for the workman than metal, as the pieces part more freely from it, but which contributed greatly to increase the above-mentioned irregularity: for the plaster, by absorbing a portion of the water from the clay contiguous to it, renders the surface at the same time, even at the instant of contact, much more consistent, and consequently more difficult to press into the angles of the mould; so that the outsides of these pieces were not only more compressed, but formed of clay of a different temper from the inner parts, being much drier or sirmer; a circumstance which, as will appear hereafter, restrains still more their diminution in the sire.

The moulds were therefore laid aside, and the press adopted in their stead; for as the soft clay, pressed in a cylindrical vessel, gives way and escapes through an aperture made for that purpose (by which means it is formed into long rods), the sides of the piece cannot be supposed to receive so great a degree of compressure against the sides of the aperture through which it is delivered in this operation, as it does against the sides of the mould, by which it is confined till every part has born a pressure sufficient to force the clay into every angle, which is much greater than even a workman would imagine till he comes to try the experiment himself.

But with this change some new difficulties arose; for pieces pressed through the same aperture, and from the same press-ful of clay, and adjusted, when dry, to the same point in the gage, were sound, after passing together through the same

strong fires, to differ in their dimensions from one another, in some instances more than any of the preceding.

Having hit erto paid no particular attention myself to the mere manual labour of pressing the clay, I determined, upon this event, to go through that and every other operation, however simple and seemingly insignificant, with my own hands. In doing this I observed, that the power necessary for forcing the clay through an aperture which bore but a small proportion to the diameter of the mass of clay in the press, was so great as to squeeze out, along with the clay that first passed through, a considerable portion of the water that belonged to the rest. From this over-proportion of water in the composition of the first pieces they were soft and spongy, and the succeeding ones more and more compact, till at length the clay proved to stiff as scarcely to be forced through at all.

Clay, containing different proportions of water, is well known to diminish differently in drying; but it was not imagined that, when dry, there would be any difference in its subsequent diminutions by fire. Experiments however, multiplied in a variety of circumstances, shewed decisively, what the pieces formed in the mould had given grounds to suspect, that those formed of the softest clay, and which had undergone the least pressure, diminished most in burning; and that the diminution is uniformly less and less, in proportion to the greater degree of pressure or compactness.

The knowledge of the cause of the irregularity suggested a remedy. I lessened the width of the press very much, so as to bring the diameter of the mass of clay, and that of the aperture through which it is delivered, to a nearer proportion without another. A much less degree of force being now sufficient, the pieces, or rods, were proportionably more uniform, though

though there was still a sensible difference, in consistence, between those which were first and last pressed out from the same mass of clay. The intermediate ones, within a certain distance from the two extremes, corresponded very nearly with one another; so that by rejecting a sufficient number of the first and last, and using the intermediate ones only, the inequality may be considered as almost annihilated.

I nevertheless still found that, in strong fire, the edges became a little prominent, though not so much as before. I was aware that these pieces must partake, in some degree, of the imperfection of those made in the mould; having their furfaces rendered, by their friction against the sides of the aperture, more compact than the inner part. But I suspected that fomething might depend also upon the form, and accordingly made many trials for ascertaining the form that might be least liable to this irregularity: the angles only were bevilled off, the fides were rounded, the pieces were rounded all over, made of ovals and other curves, and both the longest and shortest dimensions were used as the extent to be measured: the general refult was, that the nearer they came to a circular figure, the less inequality they contracted in the fire, and by making them entirely circular, the imperfection appeared to be obviated altogether; cylindric pieces bearing the strongest fires without the least appearance of prominence or inequality in any part of their furface. I have therefore chosen this last form, leaving only one narrow flat fide (ab, fig. 2.) as a bottom for the pieces to rest upon, and to distinguish the position in which they are to be measured in the gage.

I have endeavoured at the fame time to obviate whatever inaccuracy the inequality of compactness may be capable of producing, by so adjusting the aperture through which the rods

rods are pressed, and on which their figure and dimensions depend, as to superfede the use of the paring gage altogether: that the whole furface may remain of the fame uniform compactness which it received in the press. And as it is scarcely practicable, in any mode of forming foft clay, to have all the pieces precifely of the same dimensions after drying, I do not reject those which come within two or three degrees of the standard, but, instead of injuring the surface by paring or rubbing. I mark on the ends the degrees which they respectively exceed or fall short; which degrees are accordingly to be substracted, or added, in all observations of heat made with those pieces. Strictly speaking, an allowance ought to be made also for the proportional diminution upon this excess or deficiency itself; but the allowance for three degrees would not, at the melting heats of copper, filver, or gold, amount to more than a seventh part of a degree; and at the extreme point of heat that I have been able to attain, when the piece has diminished one-fourth of its whole thickness, it comes only to four-fifths of a degree.

It may be proper to take notice of an irregularity in the apparent diminutions of the pieces, which was sometimes observed to happen from another cause, their bending a little in strong fire, so as to be prevented from going so far in the gage as they would have done if they had continued perfectly straight. But as this takes place only in pieces of considerable length, and as they derive no advantage of any kind from that length, the remedy is too obvious to need being here mentioned.

Another fallacious appearance arose, not from any imperfection in the pieces themselves, but from a deception with respect to the heat in which the comparison of them had been Vol. LXXVI. F f f made. made. In one period of the course of my experiments, I employed, for firing them, a small, shallow, cylindrical vessel (sig. 3.) setting the pieces on end, close together, on its bottom, and placing it in the middle of the suel, in a common air-furnace, with care to keep the site as equal all round it as possible. It was expected, that all the pieces would receive an equal heat; and as they were found, after the operation, to differ in their dimensions, sometimes considerably, from one another, these differences proved a source of much perplexity, till it was discovered that the pieces had really undergone unequal degrees of heat.

In the paper on the comparison of this thermometer with FAHRENHEIT's \*, I have taken notice of the great difficulty of obtaining, in small furnaces, a perfectly equal heat, even through the extent occupied by a few of these little pieces: and how different the heat may be in different parts of one veffel, we may be fatisfied by an easy experiment, viz. setting a cylindrical rod of clay, of the length of eight or ten inches, upright in the middle of a crucible, and urging it with strong fire in a common small furnace; the rod will be found very differently diminished at different parts of its height; and if its height be fufficient to reach fome way above the fuel, nearly the whole range of the thermometric scale may be produced in one rod; an ocular proof, not only of the diversity of heat within a small compass, but likewise of the peculiar fensibility of this thermometer, every part of the mass expreffing distinctly the degree of heat which it has itself felt. It will be proper, in this experiment, to have a tube fixed in the bottom of the crucible, for keeping the rod steady, as at fig. 4. By this means the heat of my air-furnace renders a

<sup>\*</sup> Philosophical Transactions, vol. LXXIV.

rod of the thermometric clay tapering, from about four parts in diameter at top to three at bottom, which are nearly the proportions between the width of the piece when unburnt, or but just ignited, and when it has suffered a heat of 160 degrees.

To the foregoing fources of inequality in the pieces, one more may be added, small cavities, or air-bubbles accidentally inclosed, which sometimes happened in the earlier experiments. In order to prevent these, particular attention is now paid by the workmen to what we call banding or flapping the clay, an operation by which its different parts are intermixed, and the mass rendered of an uniform temper throughout. The workman takes a lump of the clay in his hands, perhaps of two pounds weight, and, breaking it in two in the middle, lays one part upon the other, and presses them flat again, repeating this forty or fifty times, or perhaps oftener. Now, confidering the pieces at first as two dissimilar masses, with any number of airbubbles inclosed; each of these pieces being by the first doubling divided into two, by the next into four, by the third into eight, and so on in geometrical progression, each of the original maffes will be divided by the fiftieth repetition into upwards of eleven thousand millions of millions of invisible laminæ:-invisible, because the lump of clay would, long before the last doubling, be of one uniform colour, though at first one-half of it had been black, and the other white. If therefore no air be inclosed between the pieces at the times of their being put together in this process, all the air which might have been in the mass before would certainly be driven out; and, to avoid as much as possible the introduction of any fresh portions of air, the two separated pieces are each time made fmooth, and a little convex, on the furfaces that are to be brought together.

By due attention to the circumstances above stated, any single quantity of clay may be made up into thermometer-pieces, that shall differ very little, if any thing at all, from one another.

But a new difficulty now arof., more embarraffing than any of the former; that of procuring fresh supplies of clay, of the same thermometric quality with the first. The quantity of the clay which, after trial of many others, I had made choice of, was small; but the particular spot it was taken from being known, and having purchased the little estate in which it was raifed, I had not a doubt of obtaining more of the same when it should be wanted: for clays in general, when raised from an equal depth, in the same stratum, and near the same place, are found to possess the same properties, with respect to ductility in the hands of the workman, a disposition to assume by fire a porcelain or vitreous texture, fingly or in composition, and all other qualities relative to their use in pottery. In this, however, I was deceived; for when a fresh supply was wanted, to complete my experiments, though I had some taken from a pit joining to the first, and at the same depth, it was found to diminish differently from the former parcel. I then had some raised from different parts of the same field and bed, and at different depths; and in various other places in Cornwall, from the spot where this species of clayis first met with to the Land's-End; but all these clays differed so much from the first in the quantity of their diminution by fire, and most of them likewife from each other, that I despaired of being ever able to find one that would correspond with it, or any natural clays. that could be obtained twice of exactly the same thermometric properties, how fimilar foever in other respects.

Upon a review of the numerous comparisons which I have made of these new clays, in different degrees of heat, from the commencement of redness up to intense fire, the most striking differences of the greatest part of them from the old seemed to originate in the lower stages of heat; and of those which were got from the neighbourhood of the old, the variations from it in the higher stages seemed, for the most part, to be only consequences of those differences in the lower ones.

I have mentioned, in the first Paper, that the original thermometer-pieces had their bulk enlarged a little on the approach of ignition; but that by the time they became visibly red-hot throughout, they are reduced to their former dimensions again; and at this moment the thermometric diminution begins. The new clays had their bulk enlarged in a much greater proportion, and the enlargement was of much longer continuance: some of them required a heat of 15 degrees to destroy the increase which ignition had produced in their bulk, and bring them back to their original dimensions: after this period, most of them diminished pretty regularly, and uniformly with the old, being nearly so many degrees behind it, in all the succeeding stages of heat, as they required to bring them back from the enlarged state.

I have mentioned also, in my former paper, that a quantity of air is extricated from the clay, most rapidly at the period in which the augmentation of bulk takes place; and that the augmentation was probably owing to this air forcing the particles of the clay a little asunder, previous to the instant of its escape. It was therefore presumed, that the greater extension of these new clays might be owing, either to a greater quantity, or stronger adhesion, of this combined air: and as clay, kept moist for a length of time, in certain circumstances, undergoes a process seemingly analogous to fermentation.

tion, it was hoped that, by fuch a process, part of its combined air might be detached.

But experiments made on this idea have proved, that these clays, kept moist for a twelvemonth,—kept for a considerable length of time in a heat just below visible redness,—boiled in water for many hours,—alternately, and repeatedly, moistened and dried,—suffer no alteration in their thermometric properties, and continue to differ from the standard clay just as much as they did at first.

Some of these new clays differed from the old in a property still more essential, and by which I was much more disconcerted; for though they continued diminishing with tolerable regularity, keeping only fome degrees behind it, up to a certain period of heat, about that in which cast iron melts; yet many of the pieces, urged with a heat known to be greater than that, were found not to be diminished so much as those which had fuffered only that lower heat. Further experiments shewed, that, after diminishing to a certain point, they begin, upon an increase of the heat beyond that point, to swell again: and as this effect is constant in certain clays, and begins earliest in those which are most vitrescible, and as clays are found to fivell upon the approach of vitrification, I look upon this fecond enlargement of bulk, however inconsiderable, as a sure indication of the clay or composition having gone beyond the true porcelain state, and of a disposition taking place towards vitrification; which stage is always, so far as my experience reaches, attended with a new extrication of air; and in some instances, this air being unable to make its escape from the tenacious mass that envelopes it, the burnt clay is thereby so much increased in bulk as to fwim on water like very light Wood. The degree of heat therefore, at which this enlargement begins, may be considered as a criterion of the degree of vitrescibility of the compount on; which points out a new use of this thermometer, enabling us to ascertain the degree of vitrescibility of bodies that cannot actually be vitristed by any fires which our furnaces are capable of producing.

All my refearches among the natural clays proving fruitlefs, and the experiments having shewn that all those, which could fufficiently refift vitrification, diminished too little in the fire. I endeavoured to find a body posicified of the opposite property. that is, diminishing too much, and, by a mixture of these two, to produce the medium diminution required. As I could not find any natural substance possessed of that property, which would not at the same time render the compound too vitrescible, I was obliged to have recourse to some artificial preparation; and as the earth of alum is the pure argillaceous carth, to which all clays owe their property of diminution in the fire, possessing that property in a greater or less degree according to the quantity of alum earth in their composition, I mixed some of this earth with the clay, and found it to answer my wishes completely, both in procuring the necessary degree of diminution, and increasing its unvitrescibility. So little is this compound disposed to vitrification, that the greatest heat I could give it, that of 160°, did not even bring it to a porcelain texture, but left it still bibulous; and as it does not arrive at the porcelain state in this fire, there can be no danger of its approaching too near to the vitrescent in any heat that we can produce in a furnace.

In order to obtain the exact medium required, I took one of the best of the clays I had procured from Cornwall, and mixed it with different proportions of the alum earth, till the composition was found, on repeated trials, to agree with the original in all degrees of heat. This coincidence was not indeed effential; but as many degrees of heat were already before the public, measured by thermometer-pieces made of the first clay, and as the correspondence of the first with Fahrenhell's scale had likewise been in some measure ascertained, it was desirable that the same degrees of heat should continue to be expressed by the same numbers.

The alum earth is prepared for this purpose by dissolving the alum in water, precipitating with a solution of fixed alkali, and washing the earth repeatedly with large quantities of boiling water: when the earth has settled, the water above it is let off by cocks in the sides of the hogsheads; and when the vessels are filled up with fresh water, care is taken to stir up the earth from the bottom, and mix it thoroughly with the liquor. I find it most convenient to use the earth undried, in its gelatinous state, as in this state it unites easily and perfectly with the clay; whereas, when the alum earth has concreted into dry masses, great labour is necessary to mix them unifermly together.

I have tried several different parcels of English alum, from the same and from different manufactories, and sound no material difference in the quantity of earth it contains \*. Nor indeed would it be of any consequence if there was a difference in this respect, as the proportion of alum earth necessary for

A difference in the quantity of earth may arise from different proportions of GLAUBER's falt and vitriolated tartar, of which I have found quantities very considerable, but nearly alike, in all the English alum I have examined. These salts are doubtless formed by the kelp ashes employed in the preparation of the alum. They are discovered by calcining the died alum with charcoal powder, which decomposes the alum only, leaving the other two salts intermixed with the alum earth, from whence they may be extracted by water.

different clays, and even for different parcels of the same clay, can only be ascertained by repeated trials, adding successive quantities of the earth till the desired essels is found to be produced. Ten hundred weight of the Cornwall porcelain clay which I have now in use required all the earth that was afforded by sive hundred weight of alum.

It is material in this place to observe, that the earth of alum is extremely tenacious of water, infomuch that, though apparently dry, the water and air amount to near as much as the pure earth, and are not to be completely driven out without a full red heat. When divided by the admixture of other earthy bodies, it parts with its water easier indeed than before; but a mixture containing fo much of it as the thermometric compofition does, is far more retentive of water than common clay, and requires to be kept for some time in a heat equal to that of boiling water, before it is to be confidered as dry, that is, before the adjustment of the pieces in the gage. If they are adjusted when only apparently dry, or of such a degree of dryness as they can be brought to by a heat that the hand can bear, the heat of boiling water will diminish them two or three degrees; and the greatest part of what they have thus been deprived of, they gradually recover again on being exposed to the atmosphere, so that the adjustment must be made immediately after the boiling heat.

By the same expedient to which I have thus been obliged to have recourse for procuring to the porcelain clay of Cornwall the standard degree of diminution, and resistence to fire, the same qualities may probably be communicated to any other clay that is tolerably pure from calcareous earth and iron; so that the thermometer clay is no longer to be considered as the produce of any particular spot (which was the principal incon-Vol. LXXVI.

Ggg venience

venience originally imagined to attend it), but may be procured and prepared in all parts of the world where good common clay, and alum, are to be found; and corresponding thermometers may, confequently, be constructed, without any standard to copy from. For, if a converging canal be formed, of any convenient length, with the widths at the two ends in the proportion of 5 to 3, with the fides perfectly straight, and divided into 240 equal parts, numbering the divisions from the wider end \*; - and if a clay be obtained of fuch quality, that when formed, in the manner already mentioned, into pieces of fuch fize as to enter to o in the gage or canal, these pieces shall just begin to diminish, or go a little further in the canal, by a heat visibly red; -go to 27, by the heat in which copper melts; - about 90 by the welding heat of iron; about 160, by the greatest heat that can be produced with coaked pit-coal in a well constructed common air-furnace, about eight inches square, still continuing bibulous, so as to flick to the tongue: fuch gages, and pieces of fuch clay, fo adjusted, will always compose correspondent thermometers.

Having mentioned occasionally several alternate periods of dilatation and contraction in clay, it may be proper to state, and bring into one view, the whole succession of changes which I have observed in this curious material; as otherwise they might create some confusion in the minds of those who have not had occasion to think attentively on this subject, and lead them to ask how a body so variable, and liable to such opposite changes from different degrees of heat, can yet be a just measure of those degrees.

The

<sup>\*</sup> Or the divisions on the side may be continued to 300; and in that case, instead of the widths of the two ends being in proportion of the odd numbers 5 and 3, the one will be just double to the other.

The changes which take place in all the natural clays that have come under my examination are fix.

- 1. The first is, the shrinking of the moist clay in drying, from the mere loss of its water. The purer the clay is, the more water it requires to soften it, and the more it diminishes in bulk by the loss of that water.
- 2. The dry clay, gradually heated, preserves its bulk unvaried up to the approach of ignition. At this period it is enlarged a little; probably, as already observed, from its combined air endeavouring to escape.
- 3. When this air has made its escape, the clay begins to diminish, or to lose the bulk it had before acquired; and returns back, sooner or later, to the same dimensions which it was of when dry. It is at this point that the thermometric diminution commences.
- 4. From this point the clay continues to diminish more and more in proportion as the heat is increased. This I call the thermometric stage of diminution: it is of greater or less extent, terminating at different periods of heat, according to the nature of the clay: in the standard thermometer clay, it commences with visible ignition, and continues to (doubtless far beyond) the extreme heats of our furnaces, an interval confifting of 160 degrees of the feale: in others, it begins 4, 6, and in some even 15 of those degrees later, and terminates also much fooner: and in fome its whole extent is not above 20 of the same degrees. Throughout the greatest part of this stage, the clays are found to retain their property of sticking to the tongue and imbibing water: between this bibulous state and the vitrescent there is an intermediate one, distinguished by the name of porcelain; and to the higher term of this porcelain state the stage of thermometric diminution seems to continue.

- 5. When the clay has passed the porcelain state, it begins to be enlarged again, a symptom of the vitrescent stage being commenced; and in this period it swells more or less, according to the nature of its composition.
- 6. By further heat the swelled mass, becoming stuid, subsides, is converted into glass or slag, and contracted into less volume than the clay occupied in any of its preceding states.

It is plain, therefore, that clay can be a measure of heat no further than from ignition, or that point beyond ignition where the third stage terminates, to the beginning of the vitrescent stage; and that, as the three first changes are completely passed before the clay is applied to thermometric purposes, being strictly no other than preparatory processes, the thermometerpieces, whatever clay they may be made of (provided it is sufficiently unvitrescible), are to be considered as possessing only the fourth stage. But a fingular property of the composition of clay and alum earth remains to be mentioned, viz. that it has really no other than this one stage: it suffers no enlargement of its bulk at ignition, or in any other period; but proceeds in one uninterrupted course of diminution, from the soft state in which the pieces are formed, up to the extreme fires of our furnaces. Though the diminution, however, is uninterrupted, it is at the same time so inconsiderable at the beginning, from the heat of boiling water (at which the pieces are adjusted) up to ignition, that the same point of visible redness is taken for the commencement of the scale, in this as in the original clay, without any fensible error or variation in their progress.

I am inclined to believe, though experiments have not yet enabled me to speak with certainty on this point, that the same cause which enlarges the natural clays on their first exposure to the fire, operates also in this composition, but in a much lower degree; that while the natural clays have their whole mass distended by the efforts of the air in forcing its passage, the composition is only restrained in its diminution, or prevented from diminishing so sast as it otherwise would do, and as it is found to do in the subsequent part of its course, after the air has escaped from it.

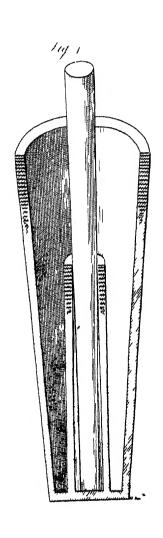
As the composition of clay and alum earth is far more tenacious of water than the clay itself, and was found, after being dried by the heat of boiling water, to yield, by distillation in a retort, above three times as much aqueous sluid as the original thermometric clay did; it seems probable, that a part of this water, retained to the approach of ignition, and in a state of chemical combination, may facilitate the passage of the air, ferving as a vehicle to convey it off through interstices not permeable to air alone, and consequently enabling it to cscape without doing that violence to the mass, which the natural clays sustain from the expulsion of their air after the water has been detached from it; for the experiments of Dr. Priestley have shown, that vessels even of burnt clay are permeable to air when they have imbibed water into their substance, though not at all so in a dry state.

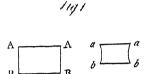
I have now communicated the refult of a series of experiments which have taken considerable time, attention, and labour to complete. Whether the importance of the object will justify me in troubling this illustrious Society with so minute a detail of the most material operations, and their results, is not for me to determine. If the thermometer should not yet be brought to the perfection that may be wished, I flatter myself that some abler hand may now take up the subject to more advantage; and that philosophers and artists will

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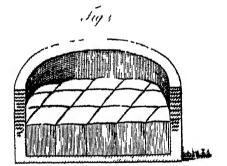
not be less successful in supplying what may still be deficient, and in ascertaining, by the contraction of argillucerus matter, the measurements and effects of the various degrees through the immense extent of luminous sire, than they have been with respect to the limited and narrow compass of low heat, which is measurable by the expansion of stuids.











XXIII. The Latitude and Longitude of York determined from a Variety of Astronomical Observations; together with a Recommendation of the Method of determining the Longitude of Places by Observations of the Moon's Transit over the Meridian. Contained in a Letter from Edward Pigott, Esq. to Nevil Maskelyne, D. D. F. R. S. and Astronomer Royal.

## Read June 29, 1786.

SIR,

Bootham, York, March 16, 1786.

HE great number and variety of observations I have made for determining the longitude and latitude of York will, I believe, settle those points very accurately: I therefore wish to have them presented to the Royal Society, and beg the favour of you to be at that trouble. The instruments I used were a good gridinon pendulum clock, a 21 seet restector, an eighteen-inch quadrant by BIRD, and a transit instrument made by Sisson.

The difference of meridians between Greenwich and York was found by the following methods.

## Occultations of stars by the moon.

```
App. time.

1783

h.

y.

York, immersion of a star of the ninth magnitude during the eclipse of the moon; good

Paris, at L'Observatoire de la Marine; ditto.

11 49 39½

Ditto, by M. Messier, who determined its R.A.

349° 22′ 17″ and south declination 5° 27′ 54″.

Oct. 7

14 26 28½ York, immersion of $\phi$ Aquarii, instantaneous.

14 37 15½ Greenwich, ditto.

Dec. 30

8 1 24

York, immersion of $\particle{T}$ Pissium, instantaneous: I find I wrote down the minute wrong, it is here corrected.

8 2 56½ Greenwich, immersion of ditto.
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Mr. GOODRICKE was so obliging as to be at the trouble of computing these occultations, and sent me the results as follows:

### Observed meridian R.A.'s of the moon's limb.

In 1783 this method of finding the difference of meridians occurred to me, and I wrote to Mr. BAYLEY, your late Affistant, for information, being entirely ignorant it had ever been noticed; but have fince seen, Sir, that you mention it in your valuable Instructions for the Observations of the Transit of Venus, annexed to the Nautical Almanac of 1769. I have also just perused on the same subject Abbé Toaldo's ingenious pamphlet written in 1784, which you were so kind as to send

me. Still I find that the great exactness of this method is not suspected; I therefore shall, in the latter part of this Paper, enter into some necessary detail, being convinced that, in a very short time, it must be universally adopted, having every advantage over Jupiter's first satellite, and but little inserior in precision to occultations.

## Difference of our meridians by each observation.

Dec	,	36	1784, July 2.	<b>1</b>	23
1781, Dec. 20.	-	•			
Dec. 29.	4	10	Nov. 20.	4	23
1782, June 17.	4	25	Dec. 20.	4	27
Nov. 30.	4	20	Dec. 22.	4	20
Dec. 18.	4	25	1785, Mar. 19.	4	25
1783, Nov. 3.	4	<b>32</b>	Aug. 16.	4	22
Dec. 6.	4	39:	Aug. 18.	4	36
Dec. 30.	4	16	Sept. 12.	4	35
1784, May 1.	4	8:	Sept. 17.	4	25
May 25.	4	11	Nov. 12.	4	34
			Nov. 14.	4	18

4' 24" ton a mean.

## Observations of Jupiter's first Satellite.

Dates, &cc.		
1782, June 3.	h. 12 36 48 12 51 9 12 51 7 13 57 40	York, it immerged near Jupiter. Paris, M. Mechain. Paris, M. Cassini. Buda, Father Whiss.

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Hhh

Obser-

# Observations of Jupiter's first Satellite continued.

Dates, &c.	App. time	
1782, July 21 Emersions.	h. , ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	York. Greenwich, Dr. Maskelyne. Paris, M. Mechain; high wind. Paris, M. Cassini. Buda, Father Weiss; moon very near Jupiter.
1783, July 3 Immeriions.	12 9 50 12 14 20 12 24 8	York; it immerged near Jupiter. Greenwich. Paris, M. Mechain.
Sept. 17 Emersions.	9 48 15 9 47 44 9 46 39 10 1 0	York. York, Mr. Goodricke; very good. Oxford, Mr. Hornssy. Paris, M. Mechain; very good.
1784, Aug. 4 Immersions.	10 10 55 10 10 57 10 24 57	York; tolerably good. York, Mr. Goodricke; middling. Paris, M. Mechain; air a little hazy.
Sept. 3 Emersions.	14 39 5 <sup>2</sup> 14 53 5 <sup>1</sup>	York; emerged near Jupiter. Paris; thinks rather too late.
Sept. 5	9 8 54 9 13 15 9 22 18 9 22 45	York; good. Greenwich, Dr. MASKELYNE. Sparis, M. MECHAIN; 6 feet reflector, magnitying 450 times. Paris; with a 3½ tripl. object glass achromatic.
Sept. 12 Emersions.	11 6 9 11 6 24 11 10 42 11 19 47 11 19 50	York; good. York, Mr. Goodricke; very good. Greenwich, Dr. Maskelyne. Paris, M. Mechain; as on the 5th. Paris, M. Mechain; as on the 5th.
1785, July 15 Immersions.	13 37 32 13 42 1	York; good.  Solution By tables corrected by the observations of Green- wich and Marscilles of July 31, 1785.
July 31 Immersions.	11 53 18 11 57 32 12 18 53	York; good, Greenwich; air very clear, Marfeilles, M. BERNARD.
		Obfer-

# Observations of Jupiter's first Satellite continued.

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Dates, &c.
             App. time.
                14 2 59 York; excellent; air remarkably clear.
1785, Aug. 30
Immersions. | 14 7 3 | Greenwich; ditto.
                14 28 33 Marieilles, M. BERNARD.
      Sept. 15 12 25 2 York; good.
                12 25 4 York, Mr. Goodricke; good; moon-light.
12 29 23 Greenwich; air clear.
12 50 46 Marfeilles, M. Blenard.
 Immersions.
                 7 58 6 York.
      Nov. 18
                  8 2 39 Greenwich; air very clear.
  Emersions.
                             Paris, M. MECHAIN; a thin cloud.
                             York; Jupiter rather low.
       Dec. 2 11 44 24
                             Greenwich; ditto; air clear.
                11 49 13
  Emerfions.
```

By letters from M. MECHAIN, Buda is 1 h. 6' 33" cast of Paris, and Marseilles also cast o h. 12' 7".

I observed with a 2½ feet reflector, which I believe to be about 10" of time inferior to the telescopes of Greenwich, Oxford, Paris, and Buda. As for Marseilles no instrument is mentioned; therefore, except for that place, 10" must be added to my immersions, and the same subtracted from the emersions; then the difference of meridians between Greenwich and York will be as follows, when each of the observations is compared to mine, and a mean thereof taken.

Emertions.

Immersions.

1782, June 3.		1782, July 21.	• -
1783, July 3.	4 36	1782, Sept. 17.	4 &
1784, Aug. 4.	_	1784, Sept. 3.	4 53
1785, July 15.	4 19	Sept. 5.	4 33
July 31.	•	Sept. 12.	4 37
Aug. 30.		1785, Nov. 18.	4 46
Sept. 15.		Dec. 12.	4 59
	4 24½ on a mean		4 38
			-

Therefore, by a mean of the immersions and emersions, York is 4' 31" west of Greenwich. Mr. Goodricke's emersion of Sept. 17, 1783, is used instead of mine, it being undoubtedly more exact.

To enter into any detail concerning the eclipses of Jupiter's satellites would be useless, as it is a matter so amply considered by every astronomer. I shall only say that the exactness expected even from those of the first satellite is, in my opinion, too highly rated. Among the various objections, there is one I have often experienced, and which proceeds solely from the disposition of the eye, that of seeing more distinctly at one time than at another. It may not be improper also to mention, that the observation I should have relied on as the best, that of August 30, 1785, marked excellent, and air remarkably clear both at Greenwich and York, is one of those which differ the most from the truth. This I remark without having the most distant inclination of drawing any conclusion; a single instance can be of no weight.

Part of the eclipse of the Moon, Sept. 10, 1783.

The two last columns shew the difference of meridians between Greenwich and York. The observations marked with an asterisk were made by Mr. Goodricke.

Cali'eus bifected	Spots observed:	York, by Mr. roodricke and me. App. time.	M. ME- CHAIN.	Paris, by M. Mes- sier. App.time.	meridians by M. MŁ	Diff. of merid. by M. Mes-
Galileus bisected - 12 25 56* 12 39 16 3 57 Arisfarchus bisected. 12 28 59 12 43 8 4 46	Aristarchus covered — Copernicus touches  Copernicus bisected  Copernicus covered — Plato touches — Plato covered — Manilius touches —  Manilius touches —  Tycho touches —  Menelaus bisected — Prom. Acut. Cen. covered Proclus bisected —  Mare Crissum touches  Mare Crissum touches  Mare Crissum covered Grimaldus emerges — Grimaldus emerged  Galileus emerges — Galileus bisected —	9 45 32 9 49 13* 9 57 39 9 57 20 9 58 33* 9 58 55 9 59 59 7 10 11 33* 10 11 57* 10 12 47* 10 13 32 10 15 41* 10 13 30 18* 10 25 26* 10 30 18* 10 32 33 10 10 32 43* 10 32 35 30 12 23 59* 12 23 59* 12 23 59* 12 25 56*	9 58 33 10 2 3 18 10 11 18 10 11 15 10 12 5 10 12 5 10 12 5 10 12 5 10 12 5 10 25 34 10 25 34 10 25 34 10 25 34 10 27 19 10 29 19 10 29 19 10 43 56 10 43 56 10 43 34 10 49 11 12 36 48 12 37 28 12 37 28 12 39 16	10 11 9 10 11 9 10 11 9 10 12 41 10 18 40 10 19 28 10 25 24 10 25 24 10 25 24 10 25 24 10 25 24 10 27 8 10 27 8 10 27 8	2 2 2 3 9 7 5 7 1 5 8 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	- 48 431 - 44 431 - 44 431 - 44 431 - 44 431 - 44 441 - 44 444 - 44

Difference of meridians on a mean 4' 16"

M. Mechain's Observatory was 9' 23", and M. Messier's 9' 18" east of. Greenwich.

Thus

Thus I have given a comparative view of the different methods I employed in fettling the longitude of our Observatory, which is in Bootham, about 400 or 500 yards N. W. of the Minster. The occultations and meridian transits of the moon's limb, which make it  $4'25''\frac{1}{2}$ , or  $1^{\circ}6'2_{3}''$ , would have been quite sufficient; but still it is interesting and useful to know how far the others err. With respect to the eclipses of the moon's spots, I think that method is in general too much neglected; and that it might be relied on infinitely more, if certain circumstances were mutually attended to.

1st, To be particular in specifying the clearness of the sky; for in hazy weather the results are very erroneous.

2dly, To chuse such spots that are well defined, and leave no hesitation as to the part eclipsed.

3dly, That every observer should, as much as possible, use telescopes equally powerful; at least let the magnifying powers be the same.

A principal objection may still be urged, viz. the difficulty of distinguishing the true shadow from the penumbra. Was this obviated, I believe, the results would be more exact than from Jupiter's first satellite: undoubtedly the shadow appears better defined if magnified little; but I am much inclined to think, that with high magnifying powers there is greater certainty of chusing the same part of the shadow, which perhaps is more than a sufficient compensation for the loss of distinctness.

Concerning the meridian observations of the moon's limb.

The advantages and precision of this method for determining the difference of meridians is, as I have already faid, so little suspected, suspected, that I flatter myself, the particulars I am going to mention will not be thought superfluous.

The rule I adopted is this:

The increase of the moon's R.A. in 12 hours (or any given time) found by computation, is to 12 hours as the increase of the moon's R.A. between two places, found by observation, is to the difference of meridians.

#### EXAMPLE.

## November 30, 1782.

h. , , , 13 12 57,62 meridian transit of the moon's second limb  $\left.\right\}$  at Greenwich by 13 13 29,08 ditto of  $\alpha$  mg  $\left.\right\}$  clock.

31,46 Difference of R.A.

13 14 8,05 meridian transit of the moon's second limb at York by clock.
13 14 30,13 ditto of a mg

22,08 difference at York,
31,46 difference at Greenwich,

} the clocks going nearly fidereal time no correction is required.

9,38 increase of the moon's apparent R.A. between Greenwich and York, by observation.

141 in seconds of a degree, ditto, ditto, ditto.

The increase of the moon's R.A. for 12 hours by computation is 23340 seconds, and 12 hours reduced into seconds is . 43200; therefore, according to the rule stated above,

23340 : 43200 :: 141 : difference of meridians=261-

These easy observations and short reduction are the whole of the business. Instead of computing the moon's R.A. for 12 hours, I have constantly taken it from the Nautical Almanacs, which give it sufficiently exact, provided some attention be paid to the increase or decrease of the moon's motion. Were the following circumstances attended to, the results would undoubtedly be much more exact.

Ist, Compare the observations to the same made in several other places.

2dly, Let several and the same stars be observed at these places.

3dly, Such stars as are nearest in R.A. and declination to the moon are infinitely preferable.

4thly, Your advice to get as near as possible an equal number of observations of each limb, to take a mean of each set, and then a mean of both means, cannot be too strongly urged. I am perfectly of your opinion, that it will considerably correct the error of telescopes and sight.

5thly, The adjustment of the telescopes to the eye of the observer before the observation, which you also recommend, will appear very judicious to every astronomer, who must have frequently perceived what you mention, that the fight is subject to vary.

6thly, As a principal error proceeds from the observation of the moon's limb, I think it may be considerably lessened, if certain little round spots near each limb were also observed in settled Observatories; in which case the libration of the moon will perhaps be a consideration.

7thly, When the difference of meridians, or of the latitudes of the places, is very confiderable, the change of the moon's diameter becomes an equation.

Though fuch are the requisites to use this method with advantage, only one or two of them have been employed in the observations that I have reduced. Two thirds of these observations had not even the same stars observed at Greenwich and York; and yet none of the results, except a doubtful one,

differ

differ 15" from the mean; therefore, I think, we may expect a still greater exactness, perhaps within 10", if the above particulars be attended to.

When the same stars are not observed, it is necessary for the observers at both places to compute their R.A. from tables, in order to get the apparent R.A. of the moon's limb; though this is not so satisfactory as by actual observation, still the difference will be trifling, provided the stars R.A.'s are accurately settled. Your catalogue undoubtedly may be depended on the most, and those stars preserved which have their proper motions ascertained. A few years ago, I had the pleasure of communicating to you the proper motion of  $\beta$  Virginis, which I found to be 1".02 per year, increasing in R.A.\*: was this unknown, and that star observed alone with the moon, it would occasion, at this time, a very considerable error.

I am also of opinion, that the same method can be put in practice by travellers with little trouble, and a transit instrument constructed so as to six up with facility in any place. Though I have not considered this sufficiently, I shall, nevertheless, subjoin a few remarks that may engage others to turn their thoughts more sully to the subject.

It is not necessary, perhaps, that the instrument should be perfectly in the meridian to a few seconds of time, provided stars, nearly in the same parallel of declination with the moon, are observed: nay, I am inclined to think, that if the instrument deviates even a quarter or half of a degree, or more, sufficient exactness can be obtained, as a table might be com-

<sup>\*</sup> Some time previous to this communication, I had found, by the comparison of my transit observations of a Aquila and B Virginis, that the latter had moved forward with a proper motion of O'', 91 of time, or of 13'', 65 of R.A. from 1767 to 1783, in 16 years, or at the rate of O'', 853 a year, on supposition that the proper motion of a Aquila is O'', 57 a year forward.

puted, shewing the moon's parallax and motion for such deviation, which deviation may easily be found by the well known method of observing stars whose difference of declination is considerable.

As travellers very feldom meet with fituations to observe stars near the pole, or find a proper object for determining the error of the line of collimation, I shall recommend the tollowing idea, which, I believe, has never yet been noticed, and hope it will answer the purpose. Having computed the apparent R.A. of four, fix, or more stars, which have nearly the same parallel of declination, observe half of them with the instrument inverted, and the other half when in its right position; if the difference of R.A.'s between each fet by observation agree with the computation, there is no error; but if they difagree, half that disagreement is the error of the line of collimation. The fame observations may also serve to determine whether the distance of the corresponding wires are equal. In case of necessity, each limb of the sun might be observed in the same manner, though probably with less precision. By a single trial I made above two years ago, the refult was much more exact than I expected. MAYER's Catalogue of Stars will prove of great use to those that adopt the above method.

In fuch a number of observations, it is not surprising that a few should be erroneous; I have rejected only three.

A meridian transit of the moon's limb, August 18, 1782; Sagitarii was the only star observed at York; it, gives for difference of meridians, . . . . . 3 55

Perhaps the star has a proper motion, or a mistake of one second might have been made in marking the clock.

An immersion of Jupiter's sirst satellite, June 22, 1783, which make the difference of meridians, .

3 4<sup>2</sup> The

I am rather furprised, that the immersions of known stars of the fixth and seventh magnitude behind the dark limb of the moon are not constantly observed in fixed Observatories, as they would frequently be of great use.

#### Latitude of York.

The following determinations for the latitude of York were made with a BIRD's 18-inch quadrant, the telescope of two feet focus, with which instrument observations of the same star seldom differ 10".

### Latitude of the Observatory.

53 53 53 53 53 53	57 57 57 57 57 57 57	41 by 2 52 by 1 37 by 1 33 by 2 57 by 4 49 by 8	ditto ditto ditto ditto ditto ditto	s of Aicturus.  of γ Lyre.  or β Arretis.  of β Cygni.  of Algol.  of γ Lyre.  of β Draconis.  of μ Draconis.
53 53 53	57 57	46 by 6 56 by 2	ditto ditto	of a Draconis.

<sup>53 57 45+</sup>latitude on a mean.

The line of collimation was deduced from  $\beta$ ,  $\gamma$ , and  $\mu$  Draconis; half of each fet observed with the face of the quadrant to the east, and half with its face to the west. This, as well as the other methods, is very tedious, particularly when required to be often repeated, as is the case in travelling; I shall therefore propose the following invention, the idea of which was improved on by Mr. SMEATON, and slatter myself it will prove of the greatest facility.

The error of the line of collimation includes the fixed errors of the instrument, and those that are subject to change, occafioned by the wires and glasses, &c. of the telescope moving. The error of these last may be found by making the telescope turn on its center, so that the sun, stars, or terrestrial objects may be observed on the horizontal wire in two manners; first, when the wire is in its natural position, and then inverted, which is performed by turning the telescope 180 degrees, or half round: thus, this part of the error can always be known with the greatest ease; and in order to find the fixed errors, it is requifite for a fingle time to get the whole error of the line of collimation by one of the common methods, from which the error of the telescope being deducted, the fixed errors become known; and as they are unchangeable, if any alteration should take place, it proceeds from the telescope, and may cafily be detected as shewn above. Perhaps, instead of the whole telescope, it would be sufficient only to make that part turn containing the eye-glass and wires.

As the following observations made also at York may be of use, I beg, Sir, you will annex them to my paper on the longitude and latitude of that city, which lately I had the pleasure of sending you.

Dates.	App	time.	
1781,July1ç 1782,May24 July 20 Nov. 30	12 2 11 2 20 5	3 12 7 40:	Emersion of Jupiter's second satellite; night fine.  Immersion of Jupiter's second satellite; good.  Emersion of Jupiter's 2d sat.; doubtful; air very hazy.  Immersion of a my behind the moon; instantaneous.  Ditto ditto; in another part of the town.  Eclipse of the moon.
2783,Mar.18	8 2 10	7 50 7 33* 9 36 0 18	Total immersion of the moon; air very clear.  Ditto; good.  Moon begins to emerge;  Certainly emerged;  Air hazy.
June 26	13 3	5 21 4 52*	Immersion of Jupiter's second satellite; good.  Ditto; middling. Eclipse of the moon; air clear.
Sept. 10	12 I 12 I 12 2 12 2 12 2 12 2 12 2 13 2 13 2 13 2	7 30 9 35 1 14 1 56* 2 24 2 24* 1 23* 2 18*	Appearance of penumbra.  Moon not emerged, but light strong.  Ditto; very strong.  Moon begins to emerge, but uncertain.  Ditto; more certain.  Ditto; ditto.  Moon certainly emerged.  Ditto.  End of the celipse, doubtful; air hazy.  Ditto.  Certainly ended, but not clear of penumbra.  Ditto, ditto; air clearer.  Several spots were observed, but are here omitted, for fear of being too voluminous.  Semersion of Jupiter's second satellite; air clear; but
Sept. 16	ł		Upiter low.
Oct. 11	7 3 7 3 5 4 5 4	4 21 2 53 6 16	Emersion of Jupiter's 3d sat.; Jupiter low; undulation. Emersion of Jupiter's second satellite. Ditto; tolerably good. Emersion of Jupiter's third satellite. Equal in brightness to the second satellite; air clear. Immersion of Jupiter's third satellite; tolerably good,
1784,July27	110	7 46	though undulation.  Dates.

Daten.	App, time.	
4784, Aug. 26 Oct. 11	h. , , 8 54 12 9 49 30	Immersion of # \$ behind the moon; instantaneous.    Emersion of Jupicer's second satellite; good, though     flight haze.   Ditto.   Emersion of Jupiter's second satellite.   Ditto.   Immersion of Jupiter's second satellite; air clear.   Immersion of Jupiter's third satellite, good; the air a
Nov 12	9 49 26 * 9 33 59 9 34 I*	Ditto.  Emersion of Jupiter's second satellite.  Ditto.
1785 July 15 Aug. 18 Scpt. 17	11 44 37 12 10 55	Immersion of Jupiter's third facellite, good; the air a Immersion of Jupiter's fecond facellite; good; a little valemersion of Jupiter's third facellite; poursh.
Oct. 29 Nov. 15	6 33 26 9 24 ±	Emersion of Jupiter's third latellite; pour lin.  I examined Jupiter's fourth satellite during 20', without being certain whether it had diminished in light.  Immersion of 125 8 by the moon, exact within 3''.
Dec. 15	5 50 48	Immeriion of 125 & by the moon, exact within 3".

I have again marked with an afterisk the observations made by Mr. Goodricke, who desired me to communicate them. This worthy young man exists no more; he is not only regretted by many friends, but will prove a loss to astronomy, as the discoveries he so rapidly made sufficiently evince: also his quickness in the study of mathematics was well known to several persons eminent in that line.

#### Declination of the needle.

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1780, Sept. 13. at 2\frac{1}{2}, by a mean of 22 trials, 2\frac{3}{2} 40\frac{1}{2} 1782, Dec. 26. at 0\frac{3}{2}, by a mean of 16 trials, 2\frac{3}{2} 5+\frac{1}{2} 1783, Nov. 14. at 0\frac{1}{2}, by a mean of 19 trials, 2\frac{3}{2} 50-\frac{1}{2} 1784, Jan. 17. at 0\frac{2}{3}, by a mean of 13 trials, 2\frac{3}{2} 54+\frac{1}{2}
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These observations were taken with all possible exactness; the needle was four inches long, and made by Dollond.

Sir H. Englefield, when at Scarborough, in August and September, 1781, was so kind as to observe, at noon, the height of his barometer and thermometer. I also made similar observations observations in the Observatory at York; from which, by eight comparisons, none disagreeing above 0,018 of an inch from the mean, I find, that the quicksilver at the sea stood 0,063 of an inch higher than at York. The barometers were made by Ramsden, and they agreed together to 0,005 part of an inch. We may later also expect to get the mean height of the barometer and thermometer, as there are several gentlement that observe them every day, particularly Mr. Wyvil and Dr. White at York, and Mr. Chomonley at Bransby.

I remain, Sir, with great regard, &c.

EDW. PIGOTT.

May 26, 1786.



XXIV. Advertisement of the expected Return of the Comet of 1532 and 1661 in the Year 1788. By the Rev. Nevil Maskelyne, D. D. F. R. S. and Astronomer Royal.

## Read June 29, 1786.

THE comet of 1531, 1607, and 1682, having returned in the year 1759, according to Dr. Halley's prediction in his Synopsis Astronomiæ Cometicæ, sirst published in the Philosophical Transactions in 1705, and re-published with his Astronomical Tables in 1749, there is no reason to doubt that all the other comets will return after their proper periods, according to the remark of the same author.

In the first edition of the Synopsis he supposed the comets of 1532 and 1661, from the similarity of the elements of their orbits, to be one and the same; but in the second edition he has seemed to lessen the weight of his first conjecture by not repeating it. Probably he thought it best to establish this new point in astronomy, the doctrine of the revolution of comets in elliptic orbits, as all philosophical matters in the beginning should be, on the most certain grounds; and seared that the vague observations of the comet, made by APIAN in 1532, might rather detract from, than add to, the evidence arising from more certain data. Astronomers, however, have generally acquiesced in his first conjecture of the comets of 1532 and 1661 being one and the same, and to expect its return to its perihelium accordingly in 1789.

The

The interval between the passages of the comet by the perihelium in 1532 and 1661 is 128 years, 89 days, 1 hour, 29 minutes (32 of the years being bissextile), which added to the time of the perihelium in 1661, together with 11 days to reduce it from the Julian to the Gregorian stile, which we now use, brings out the expected time of the next perihelium to be April 27th, 1 h. 10' in the year 1789.

The periodic times of the comet, which appeared in 1531, 1607, and 1682, having been of 76 and 75 years alternately, Dr. HALLEY supposed, that the subsequent period would be of 76 years, and that it would return in the year 1758; but, upon confidering its near approach to Jupiter, in its descent towards the fun in the fummer of 1681, he found, that the action of Jupiter upon the comet was, for feveral months together, equal to onefiftieth part of the fun upon it, tending to increase the inclination of the orbit to the plane of the ecliptic, and lengthen the periodic time. Accordingly, the inclination of the orbit was found by the observations made in the following year 1682 to be 22' greater than in the year 1607. The effect of the augmentation of the periodic time could not be feen till the next return, which he supposed would be protracted by Jupiter's action to the latter end of the year 1758, or the beginning of 1759. M. CLAIRAUT, previous to its return, took the pains to calculate the actions both of Jupiter and Saturn on it during the whole periods from 1607 to 1682, and from 1682 to 1759, and thence predicted its return to its perihelium by the middle of April; it came about the middle of March, only a month fooner, which was a sufficient approximation to the truth in so delicate a matter, and did honour to this great mathematician, and his laborious calculations.

The comet in question is also, from the position of its orbit, liable to be much disturbed both by Jupiter and Saturn, particularly in its ascent from the sun after passing its perihelium, if they should happen to be near it, when it appoaches to or crosses their orbits; because it is very near the plane of them at that time. When it passed the orbit of Jupiter in the beginning of February 1682, O. S. it was 50° in consequentia of that planet; and when it passed the orbit of Saturn in the beginning of October 1663, it was 17° in consequentia of it. Hence its motion would be accelerated while it was approaching towards the orbit of either planet by its separate action, and retarded when it had passed its orbit; but, as it would be subjected to the effect of retardation through a greater part of its orbit than to that of acceleration, the former would exceed the latter, and confequently the periodic time would be fhortened; but probably not much, on account of the confiderable distance of the comet from the planets when it passed by them; and therefore we may still expect it to return to its perihelium in the beginning of the year 1789, or the latter end of the year 1788, and certainly some time before the 27th of April 1789. But of this we shall be better informed after the end of this year, from the answers to the prize question proposed by the Royal Academy of Sciences at Paris, to compute the disturbances of the comet of 1532 and 1661, and thence to predict its return \*.

<sup>\*</sup> Since this was written, I received the unwelcome news, in a letter from M. MECHAIN, of the Royal Academy of Sciences at Paris, that the Academy has not received fatisfactory answers concerning the disturbances of the comet between 1532 and 1661, and 1661 and the approaching return, and that the prize is referred to be adjudged of at Easter 1788, and that it will be 6000 livres. N. M.

If it should come to its perihelium on the 1st of January 1789, it might probably be visible, with a good achromatic telescope, in its descent to the sun, the middle of September 1788, and sooner or later, according as its perihelium should be sooner or later. It will approach us soom the southern parts of its orbit, and therefore will sirst appear with considerable south latitude and south declination; so that persons residing nearer the equator than we do, or in south latitude, will have an opportunity of discovering it before us. It is to be wished that it may be first seen by some astronomer in such a situation, and surnished with proper instruments for settling its place in the heavens, the earliest good observations being most valuable for determining its elliptic orbit, and proving its identity with the comets of 1532 and 1661. The Cape of Good Hope would be an excellent situation for this purpose.

In order to affift aftronomers in looking out for this comet, I have here given its heliocentric and geocentric longitudes and latitudes and correspondent distances from the sun and earth, on supposition that it shall come to its perihelium on January 1, 1789. But if that should happen sooner or later, the heliocentric longitudes and latitudes and distances from the sun will stand good if applied to days as much earlier or later, as the time of the perihelium may happen sooner or later; and the geocentric longitudes and latitudes and distances from the earth must be re-computed accordingly. The calculations are made for a parabolic orbit from the elements determined by Dr. Halley from Heyelius's observations in 1661, only allowing for the precession of the equinoxes. The elements made use of were as follows:

Time of perihelium January 1, 1789, at noon. Perihelium distance 0,44851.

Place of ascending node 25 24° 18'.

Inclination of orbit to the ecliptic 32° 36'.

Perihelium forwarder in orbit than the ascending node 33° 28'.

It motion is direct.

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Computed places of the comet, on supposition that it shall return to its perihelium January 1, 1789, at noon.

Times.	Lift. from ⊙•	from	Heli tric tude	lon	gi.		lat	i-	Ge tric tude	lon	gi-		lati-	rroduct of distances from O and carth.
1788 Apr. 23, 7 June 4, 1 July 14, 5 Aug. 2,46 — 20,43 Sept. 7, 2 — 24, 6 Oct. 10,26 — 26,6., Nov. 9,34 — 23,36 Dec. 7,21 — 23,37 — 24,35 1789	3, 2,75 2,5 2,25 2, 1,75 1,50 1,25 1,0 0,75 0,50	2,57 2,15 1,79 1,51 1,29 1,13 1,01 0,88 0,76 0,62 0,50	II II II II II O O O I 2	3 7 11 13 10 20 24 29 5 14 26 13 20 24	54 16 16 47 39 16 24 51 48 58	30 31 32 32 32 32 32 32 32 32 32 32 32 32 32	29 8 0	S	S. 11 11 0 0 0 0 11 11 10 10 10 10 9 9 9	26 3 4 2 25 3 28 158 4 29 14 12	30 31 8 6 12 22 50 31 31 55	27 31 38 42 48 53 56 56 52 46 39 27 20	0 45 7 S 0	0,25
Jan. 1, c	0,45	0,59	13	23	25	117	17	N	19	2	50	113	8 1/	0,26

The last observation made by Hevelius on the comet in 1661 was when its distance from the earth was 0,986, and from the sun 1,37, with what he calls a very long and good telescope; at which time it appeared faint and small with it, though

though still sufficiently visible. Let us suppose this to have been a telescope of 9-seet socal length, with an aperture of 1,65 inch; then, because the diameter of the aperture of a telescope sufficient to render the comet equally visible should be as the product of its distances from the sun and earth, and the product of the numbers above-mentioned 0,986 and 1,37 is 1,35, we shall have the following analogy to find the aperture of a restracting telescope sufficient to shew the comet as it appeared to Hevelius. As 1,35: 1,65 inch: 9: 11 inches, so is the product of distances from the sun and earth to the diameter of the aperture required in inches.



XXV. A new Method of finding Fluents by Continuation. By the Rev. Samuel Vince, A. M. F. R. S.

## Read July 6, 1786.

ART. I. Put  $\dot{\mathbf{F}} = \frac{x^m \dot{x}}{x^n + x^n} = x^{m-n} \dot{x} - a^n x^{m-2n} \dot{x} + a^{2n} x^{m-3n} \dot{x} - a^{2n} x^{m-2n} \dot{x} + a^{2n}$ &c.  $\pm \frac{a^{2n}x^{m-2n+1}}{a^{m-2n+1}}$ , then  $F = \frac{x^{m-n+1}}{m-n+1} - \frac{a^{n}x^{m-2n+1}}{m-2n+1} + \frac{a^{2n}x^{m-3n+1}}{m-3n+1} - &c.$ =W, where W represents the fluent of the last term. Now  $\frac{x^m \dot{x}}{x - n!} = \frac{x^m \dot{x} \times a^n + x^{n+1}}{a^n + x^n}; \text{ hence } \int \frac{x^m \dot{x}}{a^n + x^n} = \int \frac{x^m \dot{x} \times a^n + x^n}{a^n + x^n} = F$  $\left[\times \overline{a^n + x^n}\right]^{1-r} - \int \mathbf{F} \times \frac{1-r \cdot nx^{n-1}\dot{x}}{\frac{r}{r} + x^n} = \text{(by fubflitting for } \mathbf{F} \text{ its}$ value in the latter quantity)  $F \times \overline{a^n + x^n}^{1-r} - \frac{1-r \cdot n}{m-n+1} \times \frac{1-r \cdot n}{n-n+1}$  $\int \frac{x^{m}x}{x^{m}} + \frac{1-r \cdot na^{n}}{m-2n+1} \times \int \frac{x^{m-n}x}{x^{n}-1} - \frac{1-r \cdot na^{2n}}{m-3n+1} \times \int \frac{x^{m-n}x}{n} + \&c. \pm \frac{x^{m-n}x}{n-2n+1} \times \int \frac{x^{m-n}x}{n} + \frac{x^{m-n}x}{n-2n+1} \times \int \frac{x^{m-n}x}{n} + \frac{x^{m-n}x}{n-2n+1} \times \int \frac{x^{m-n}x}{n} + \frac{x^{m-n}x}{n-2n+1} \times \int \frac{x^{m-n}x}{n-2n+1} \times$  $\int W \times \frac{\overline{1-r \cdot nx^{n-1}x}}{\overline{n-r}}$ ; transpose  $-\frac{\overline{1-r \cdot n}}{\overline{m-n+1}} \times \int \frac{x^{n}x}{\overline{x-r}}$  and divide both fides of the equation by  $\frac{m-rn+1}{m-n+1}$  and we  $\int \frac{x^m \dot{x}}{\frac{n}{m-rn+1}} = \frac{m-n+1}{m-rn+1} \times \mathbf{F} \times \overline{a^n + x^n} = \frac{m-n+1}{m-rn+1} \times \frac{1-r \cdot na^n}{m-2n+1} \times \frac{1-r \cdot na$  $\int \frac{x^{m-n}\dot{x}}{\frac{x}{m-n+1}} - \frac{m-n+1}{m-rn+1} \times \frac{1-r \cdot na^{2n}}{m-3n+1} \times \int \frac{x^{m-2n}\dot{x}}{\frac{x}{m-1}+1} + \&c. \pm \frac{m-n+1}{m-rn+1} \times \frac{1-r \cdot na^{2n}}{m-rn+1} \times \frac{1-r \cdot na^{2n}}{m$ 

 $\int W \times \frac{1-r \cdot nx^{n-1}\dot{x}}{1-r}$ ; now the fluent of the last term is  $= \frac{m-n+1}{n-n+1} \times W \times \overline{a^n+x^n}^{1-r} \pm \frac{m-n+1}{m-rn+1} \times \int \frac{a^{\upsilon n} x^{m-\upsilon n} x}{n+n!}; \text{ hence by}$ substituting this quantity for the last term, it is manifest, that the first part  $= \frac{m-n+1}{m-rv+1} \times W \times a^{n} + x^{n}$  will be destroyed by the last term of  $\frac{m-n+1}{m-rn+1} \times \mathbf{F} \times \overline{a^n+x^n}^{1-r}$ , when we substitute for F its value; hence if we put  $M = \frac{x^{m-n+1}}{m-n+1} - \frac{a^n x^{m-2n-1}}{m-2n+1} + \frac{a^n x^{m-2n-1}}{m-2n+1}$  $\frac{a^{2n}x^{m-3n+1}}{m-2n+1}$  - &c. omitting the last term  $\pm$  W, we have  $\int \frac{x^m \dot{x}}{1-x^n} r = \frac{m-n+1}{m-rn+1} \times M \times \overline{a^n + x^n} = \frac{m-n+1}{m-rn+1} \times \frac{1-r \cdot na^n}{m-2n+1} \times \frac{1-r \cdot na^n}{m-2n$  $\int \frac{x^{n-n}\dot{x}}{n-n} = \frac{m-n+1}{m-n+1} \times \frac{1-r \cdot na^{2n}}{m-3n+1} \times \int \frac{x^{m-2n}\dot{x}}{n-n} + &c. = \frac{m-n+1}{m-rn+1} \times$  $\times a^{n} \times \int \frac{x^{m-n}x^{n}}{x^{n-n}}$ ; hence, if the fluent of the last term be given, we have the general law of continuation by which we may find the fluent of  $\frac{x^m \dot{x}}{n+n!}$ . If the fluxion be  $\frac{x^m \dot{x}}{n+n!}$  all the terms after the first will be negative, and the last always politive.

Ex. 1. Given the fluent of  $\frac{\dot{x}}{\sqrt{1+x^2}}$  to find the fluent of  $\frac{x^{2i}\dot{x}}{\sqrt{1+x^2}}$ .

Here 
$$n=2$$
,  $a=1$ ,  $m=2s$ ,  $r=\frac{1}{2}$ ,  $M=\frac{x^{2n-1}}{2n-1}-\frac{x^{2n-3}}{2n-3}+8c$ . to  $\Rightarrow x_1$ 

which call Q; hence  $\int \frac{x^{2i}\dot{x}}{\sqrt{1+x^2}} = \frac{2s-1}{2s} \times M \times \sqrt{1+x^2} + \frac{2s-1}{2s \cdot 2s-3} \times \int \frac{x^{2s-2}\dot{x}}{\sqrt{1+x^2}} - \frac{2s-1}{2s \cdot 2s-5} \times \int \frac{x^{2s-4}\dot{x}}{\sqrt{1+x}} + &c. = \frac{2s-1}{2s} \times Q.$ If s = 1,  $\int \frac{x^2\dot{x}}{\sqrt{1+x^2}} = \frac{1}{2}\sqrt{1+x^2} \times x - \frac{1}{2}Q = \alpha.$  s = 2,  $\int \frac{x^4\dot{x}}{\sqrt{1+x^2}} = \frac{3}{4}\sqrt{1+x^2} \times \frac{x^3}{3} - x + \frac{3}{4}\alpha + \frac{3}{4}Q = \beta.$  s = 3,  $\int \frac{x^6\dot{x}}{\sqrt{1+x^2}} = \frac{5}{6}\sqrt{1+x^2} \times \frac{x^5}{5} - \frac{x^3}{3} + x + \frac{5}{6 \cdot 3}\beta - \frac{5}{6}\alpha - \frac{5}{6}Q = \gamma.$  s = 4,  $\int \frac{x^8\dot{x}}{\sqrt{1+x^2}} = \frac{7}{8}\sqrt{1+x^2} \times \frac{x^7}{7} - \frac{x^5}{5} + \frac{x^3}{3} - x + \frac{7}{8 \cdot 5}\gamma - \frac{7}{8 \cdot 3}$   $\beta + \frac{7}{8}\alpha + \frac{7}{8}Q.$ &c.

Ex. 2. To find the fluent of  $x^{\frac{3}{2}} \dot{x} \sqrt{2+x}$ , given the fluent of  $x^{-\frac{1}{2}} \dot{x} \sqrt{2+x}$ , and s an odd number.

Here a=2, n=1,  $r=-\frac{1}{2}$ ,  $\frac{s}{a}=m$ ,  $m-vn=-\frac{1}{2}$ , or  $\frac{s}{a}-v$ 

$$= -\frac{1}{2}; : v = \frac{s+1}{2}, M = \frac{2x^{2}}{s} - \frac{4x^{2}}{s-2} + \frac{8x^{2}}{s-4} - \&c. \text{ and the}$$
fluent (Q) of  $x^{-\frac{1}{2}}\dot{x}\sqrt{2+x}$  is  $\pi + \sqrt{2x+x^{2}}$ , where  $\pi = \text{hyp.}$ 

$$\log 1 + x + \sqrt{2x+x^{2}}; \text{ hence } \int x^{\frac{5}{2}}\dot{x}\sqrt{2+x} = \frac{s}{s+3} \times \frac{1}{2+x} = \frac{s}{s+3} \times \frac{1}{2+x} \times \frac{1$$

<u>--</u>بـــ

If 
$$s = 1$$
,  $\int x^{\frac{1}{2}} x^{\frac{1}{2}} \sqrt{2 + x} = \frac{1}{2} \times 2 + x^{\frac{1}{2}} \times 2 + x$ 

II. Let 
$$\dot{F} = \frac{x^n \dot{x}}{a + bx^m + x^{2m}} = x^{m-2m} \dot{x} - P x^{m-3m} \dot{x} + Q x^{m-4m} \dot{x}$$
 &c.  $\pm$ 

 $\frac{\nabla x^{n-2m}\dot{x}}{a+bx^m+x^{2m}} = \frac{Wx^{n-\frac{1}{2}+1}\dot{x}}{a+bx^m+x^{2m}}, \text{ then } F = \frac{x^{n-2m+1}}{n-2m+1} - \frac{Px^{n-3m-1}}{n-3m+1} + \frac{Qx^{n-4m+1}}{n-4m+1} - & \text{exc.} \pm T \pm U, \text{ where T and U are put for the fluents of the two last terms, and P, Q, &c. for the co efficients arising from$ 

the division. Now, 
$$\int \frac{x^{n}\dot{x}}{\sqrt{a+bx^{m}+x^{2m}}} = \int \frac{x^{n}\dot{x} \times \overline{a+bx^{m}+x^{2m}}}{a+bx^{m}+x^{2m}} = F \times \overline{a+bx^{m}+x^{2m}} = \int \frac{x^{n}\dot{x} \times \overline{a+bx^{m}+x^{2m}}}{a+bx^{m}+x^{2m}} = \int \frac{x^{n}\dot{x} \times \overline{a+bx^{m}+x^{2m}}}{a+$$

fubstituting for F its value in the latter quantity, and putting A, B, C, &c for the co-efficients which arise in consequence

thereof) 
$$F \times \overline{a + bx^m + x^{2m}}$$
 - A  $\times \int \frac{x^n \dot{x}}{a + bx^m + x^{2m}} + B \times$ 

$$\int \frac{x^{n-m}\dot{x}}{a+bx^m+x^{2m}} - C \times \int \frac{x^{n-2m}\dot{y}}{a+bx^m+x^{2m}} + \&c.$$
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Mr. VINCE's new Method of

$$=\int \mathbf{T} \times \frac{\overline{1-.mbx^{m-1}} \cdot \overline{+1-r} \cdot 2mx^{2r-1} \cdot \overline{x}}{\overline{a+bx^{m}+x^{-n}}}$$

 $= \int U \times \frac{1-r \cdot mbx^{m-1}\dot{x} + 1-r \cdot 2^{mx^{2m-1}}\dot{x}}{a+bx^{m}+x^{2n}}; \text{ hence by transposition}$ 

and division we have  $\int \frac{x^n \dot{x}}{a + bx^m + x^{2m}} = \frac{\tau}{1 + \Lambda} \times F \times \overline{a + bx^m + x^{2m}}^{\tau - r}$ 

$$+ \frac{r_{1}}{1+A} \times \int \frac{x^{n-m}\dot{x}}{a+bx^{m}+x^{2/3}} - \frac{C}{1+A} \times \int \frac{x^{n-m}\dot{x}}{a+bx^{m}+x^{2/3}} + &c.$$

$$= \int \frac{T}{1+A} \times \frac{1-r \cdot mbx^{m-1}\dot{x}+1-r \cdot 2m \cdot 2m \cdot 2m-1}{a+bx^{m}+x^{2/3}} r$$

 $\mp \int \frac{U}{1+\lambda} \times \frac{\overline{1-r \cdot mbx^{m-1}}\dot{x} + \overline{1-r \cdot 2mx^{2m-1}}\dot{x}}{\overline{a+bx^m+x^{2m}}}.$  Now the fluents

of these two last terms are  $=\frac{T}{I+A} \times \overline{a+bx^m+x^{2n}}$   $\stackrel{I-r}{=} \frac{V}{I+A}$ 

$$\int_{\overline{a+bx^m+x^{2m}}]'}^{x^{n-sm}\dot{x}} \operatorname{and} = \frac{U}{1+A} \times \overline{a+bx^m+x^{2m}} \Big|_{1+A}^{1-r} = \frac{W}{1+A} \int_{\overline{a+bx^m+x^{2m}}]'}^{x^{n-s+1}\cdot m} \dot{x}$$

respectively; hence, by substituting these for the last term, it is manifest that  $=\frac{T}{1+A} \times \overline{a+bx^m+x^{2m}}$  and  $=\frac{U}{1+A}$ 

 $\times \overline{a + bx^m + x^{2m}}$  will be destroyed by the two last terms of  $\frac{1}{1+A} \times F \times \overline{a + bx^m + x^{2m}}$  when we substitute for F its value;

hence, if we put  $M = \frac{x^{n-2m-1}}{n-2m+1} - \frac{Px^{n-3m+1}}{n-3m+1} + \frac{Qx^{n-4m+1}}{n-4m+1} - &c.$  omitting the two last terms  $\pm T$  and  $\pm U$ , we shall have

$$\int \frac{x^n \dot{x}}{a + bx^m + x^{2m}} = \frac{1}{1+A} \times M \times \overline{a + bx^m + x^{2m}}^{1-r} + \frac{B}{1+A} \times A$$

$$\int \frac{x^{n-2m}\dot{x}}{a+bx^m+x^{2m}} - \frac{C}{1+A} \times \int \frac{x^{n-2m}\dot{x}}{a+bx^m+x^{2m}} + &c. \pm \frac{V}{1+A} \times$$

 $\int$ 

$$\int \frac{x^{n-sm}\dot{x}}{a+bx^{m}+x^{2n})'} = \frac{W}{1+\Delta} \times \frac{x^{n-s+1+m}\dot{x}}{a+bx^{n}+x^{2n}}; \text{ hence if the two last}$$

fluents be given, we have the general law of continuation up to  $\frac{x^n \dot{x}}{a + bx^m + x^{2m}}$  in the fame manner as before.

III. In general, if we proceed as in the two last articles, we shall find  $\int \frac{x^n \dot{x}}{a + bx^m + \&c. \ x'^m} = \frac{M}{P} \times a + bx^m + \&c. \ x'^m = \frac{A}{P} \times a + bx^m + \&c. \$ 

number of these last terms is t, and  $M = \frac{x^{n-t}m+1}{n-tm+1} - \frac{Qx^{n-t+1} \cdot m-1}{n-t+1 \cdot m+1} + &c.$  omitting, as before, the terms at the end arising from the remainders. Hence if the last t fluents be given, we can by continuation find the required fluent.

Because the division of  $\frac{x^n\dot{x}}{a+bx^m+&c.\ x^{im}}$  may be expressed by an ascending series  $x^n\dot{x}-Qx^{n+m}\dot{x}+Rx^{n+2m}\dot{x}-&c.$  it is manifest, that by the same method we may continue the sluents downwards as well as upwards.

IV. Let 
$$\hat{F} = \frac{x^n \dot{x}}{1-x} = -x^{n-1} \dot{x} - x^{n-2} \dot{x} - x^{n-3} \dot{x} - \&c. - x^{n-r} \dot{x} + \frac{x^{n-r} \dot{x}}{1-x}$$
, then  $F = -\frac{x^n}{n} - \frac{x^{n-1}}{n-1} - \frac{x^{n-2}}{n-2} - \&c. - \frac{x^{n-r+1}}{n-r+1} + W$ , where W is the fluent of the laft term. Now  $\frac{x^r \dot{x}}{\sqrt{1-x}} = \frac{x^n \dot{y}}{1-x} \times \sqrt{\frac{1-x}{1+x}}$ .

hence 
$$\int \frac{\lambda^{n} \dot{x}}{\sqrt{1-x^{2}}} = \int \frac{x^{n} \dot{x}}{1-x} \times \sqrt{\frac{1-x}{1+x}} = F \times \sqrt{\frac{1-y}{1+x}} + \int F \times \frac{\dot{x}}{\sqrt{1+x^{2}\times 1+x}} = F \times \sqrt{\frac{1-x}{1+x}} - \int \frac{\sqrt{n} \dot{x}}{\sqrt{1-x}\times 1+x} - \int \frac{\sqrt{n-1} \dot{x}}{\sqrt{1-x}\times 1+x} - \frac{x^{n-1} \dot{x}}{\sqrt{1-x}\times 1+x} - & \text{&c.} - \int \frac{x^{n-r+1} \dot{x}}{\sqrt{1-x}\times 1+x} + \int W \times \frac{\dot{x}}{\sqrt{1-x^{2}\times 1+x}} - & \text{But}$$

$$\frac{x^{n}\dot{x}}{\sqrt{2}\times 1+x} = \frac{x^{n-1}\dot{x}}{n\sqrt{1-x^{2}}} + \frac{x^{n}}{n\sqrt{1-x^{2}}} + \frac{x^{n}}{n\sqrt{1-x^{2}}} + \frac{x^{n-r}\dot{x}}{n\sqrt{1-x^{2}}} + \frac{x^{n-r}\dot{x}}{n\sqrt{1-x^{2}}} \pm \frac{x^{n-r}\dot{x}}{n\sqrt{1-x^{2}}} + \frac{x^{n-r}\dot{x}}{n\sqrt{1-x^{2}}} + \frac{x^{n-r}\dot{x}}{n\sqrt{1-x^{2}}} + \frac{x^{n-r}\dot{x}}{n-1} \cdot \sqrt{1-x^{2}} + \frac{x^{n-r}\dot{x}}{n-2} \cdot \sqrt{1-x^{2}} + \frac{x^{$$

Hence 
$$\int \frac{x^n \dot{x}}{\sqrt{1-x^2}} = F \times \sqrt{\frac{1-x}{1+x}} - \frac{1}{n} \times \int \frac{x^{n-1}\dot{x}}{\sqrt{1-x^2}} + \frac{1}{n} - \frac{1}{n-1} \times \int \frac{x^{n-2}\dot{x}}{\sqrt{1-x^2}} + \frac{1}{n} - \frac{1}{n-1} \times \int \frac{x^{n-2}\dot{x}}{\sqrt{1-x^2}} + \frac{1}{n-1} + \frac{1}{n-2} \times \int \frac{x^{n-3}\dot{x}}{\sqrt{1-x^2}} + &c. \pm \frac{1}{n} \pm \frac{1}{n-1} \pm &c.$$

$$-\frac{1}{n-r+1} \times \int \frac{x^{n-r}\dot{x}}{\sqrt{1-x^2}} = \frac{1}{n} \pm \frac{1}{n-1} \pm &c. + \frac{1}{n-r+1} \times \int \frac{x^{n-r}\dot{x}}{\sqrt{1-x} \times 1+x} + \int W \times \frac{\dot{x}}{\sqrt{1-x^2} \times 1+x} - W \times \frac{\dot{x}}{\sqrt{1-x^2} \times 1+x} - W \times \frac{\dot{x}}{\sqrt{1-x^2} \times 1+x} = -W \times \int \frac{x^{n-r}\dot{x}}{\sqrt{1-x^2}} + \int \frac{\sqrt{n-r}\dot{x}}{\sqrt{1-x^2}}; \text{ also } \int \frac{x^{n-r}\dot{x}}{\sqrt{1-x^2} \times 1+x} = -x^{n-r} \times \sqrt{\frac{-v}{r^2}} + \frac{1}{n-r} \times \int \frac{x^{n-r}\dot{x}}{\sqrt{1-x^2}} - \frac{x^{n-r}\dot{x}}{\sqrt{1-x^2}}; \text{ hence, by substituting these quantities in the two last terms, it is manifest that } - W \times \frac{1-x}{1-x} \quad \text{will be destroyed by the last term of}$$

 $\mathbf{F} \times \frac{\mathbf{I} - \mathbf{I}}{\mathbf{I} + \mathbf{I}}$  when we substitute for F its value; therefore, if we put  $M = -\frac{1}{n} - \frac{1}{n-1} - &c. -\frac{1}{n-1+1}$ , we shall  $\int \frac{\sqrt{n_{v}^{2}}}{\sqrt{1+n_{v}^{2}}} = M^{\frac{1}{2}} \int_{0}^{1} \frac{1}{\sqrt{1+n_{v}^{2}}} dx = M^{\frac{1}{2}} \int_{0}^{1} \frac{1}{\sqrt{1+n_{v}^{2}$  $+\frac{1}{n}-\frac{1}{n-1}\times\int_{-\infty}^{\sqrt{n-2}}\frac{1}{n}-\frac{1}{n}-\frac{1}{n-1}+\frac{1}{n-2}\times\int_{-\infty}^{2^{n-3}}\frac{x^{n-3}}{\sqrt{x^{n-3}}}+\&c.$  $\frac{1}{1 + \frac{1}{1 + 1}} = &c. - \frac{1}{n - 1} \wedge \frac{1}{1 - 1 + 1} \times \int_{\sqrt{1 - 1}}^{\sqrt{n - \hat{x}}} \sqrt{\frac{1 - 1}{1 - 1}}$  $\frac{1}{n} = \frac{1}{n-1} = &c. + \frac{1}{n-r+1} \times \frac{1}{n-r} \times \int_{-\frac{1}{n-r-1}}^{\frac{n-r-1}{2}} .$  Hence, if the two last fluents be given, we have the general law of continuation up to the fluent of  $\frac{\sqrt{x}}{\sqrt{x}-x^2}$ , where the index of x without the vinculum increases by unity each time. And in the fame manner we may (by increasing the index of x without by m) find the fluent of  $\frac{x^n x}{\sqrt{x^2 + x^2}}$  if we have given the fluents of  $v^{n-rm}\dot{x} = and \frac{x^{n-r+1-rm}}{\sqrt{x^{n-r}}}$ . Thus we have a general law of continuation, where the index of x without is increased by half the index under the vinculum.

V. Affirme  $\dot{F} = \frac{a^n \dot{a}}{x^m - b} = x^{n - m} \dot{x} + b x^{n - 2m} \dot{x} + b^n \dot{a}^{n - 3m} \dot{x} + \&c. + \frac{b^n x^{n - rm} \dot{x}}{a^m - b}$ , then  $\dot{F} = \frac{x^{n - rm} \dot{x}}{n - m + 1} + \frac{b x^{n - 2m + 1}}{n - 2m + 1} + \frac{b^2 x^{n - 3m + 1}}{n + 3^{m + 1}} + \&c. + W$ , where W is put for the fluent of the last term. Now  $\int x^n \dot{x} \sqrt{\frac{n}{x^m - b}} = \int \frac{n}{x^m - b} \times \sqrt{x^m - \mu} \times x^m - \dot{b} = \dot{F} \times \sqrt{x^m - a \times x^m + b}$ 

$$-\int \mathbf{F} \times \frac{2mx^{2m-1}\dot{x}-a+b \cdot mx^{m-1}\dot{x}}{2\sqrt{x''-a}\times x''-b}} = \text{(by fubfituting for } \mathbf{F} \text{ ite}$$
value in the latter quantity, and putting A, B, C, &c. for the co-efficients which arise therefrom) } \mathbf{F} \times \sqrt{x''-a}\times x'''-b} - \mathbf{A}\int \frac{x^n\dot{x}}{\sqrt{x'''-a}\times x'''-b}} - \mathbf{B}\int \frac{x^{n-m}\dot{x}}{\sqrt{x'''-a}\times x'''-b}} - \mathbf{C}\int \frac{x^{n-m}\dot{x}}{\sqrt{x''''-a}\times x''''-a}} - \mathbf{C}\int \frac{x^{n-m}\dot{x}}{\sqrt{x''''-a}\times x'''-a}} - \mathbf{C}\int \frac{x^{n-m}\dot{x}}{\sqrt{x'''''-a}\times x'''-a}} - \mathbf{C}\int \frac{x^{n-m}\dot{x}}{\sqrt{x'''''-a}\times x'''-a}} - \mathbf{C}\int \frac{x^{n-m}\dot{x}}{\sqrt{x''''''-a}\times x''''-a}} - \mathbf{C}\int \frac{x^{n-m}\dot{x}}{\sqrt{x'''''-a}\times x'''-a}} - \mathbf{C}\int \frac{x^{n-m}\dot{x}}{\sqrt{

$$-\int W \times \frac{2m\sqrt{x^m-c}}{2\sqrt{x^m-c}} \times \sqrt{x^m-b}$$
 is  $-W \times \sqrt{x^m-d} \times x^{d'}-b$   $+b' \times \int x^{n-m}\dot{x}\sqrt{\frac{x''-c}{x''-b}}$ ; hence, by fubfituting this for the laft term, it is manifoft, that  $-W \times \sqrt{x^m-d} \times x^m-b$  when we fubfitute for F its value; therefore, if we put  $M = \frac{x^{m-c}+1}{x^m-d+1} + \frac{bx^{m-2m+1}}{n-2m+1} + &c. + \frac{b^{m-1}\sqrt{n-m+1}}{n-m+1}$ , we have  $\int x'x\sqrt{\frac{m-r}{x^n-b}} = M \times \sqrt{x^m-a} \times x^m-b - A \int x^{m-m}\dot{x}\sqrt{\frac{x^m-a}{x^m-b}} - \frac{1}{2\lambda d} + Bx \int x^{m-2m}\dot{x}\sqrt{\frac{m-r}{x^m-b}} - \frac{1}{2\lambda d} + Bx \int x^{m-2m}\dot{x}\sqrt{\frac{m-r}{x^m-b}} - \frac{1}{2\lambda d} + Bx^{m-1} + Cx^{m-2m}\dot{x}\sqrt{\frac{m-r}{x^m-b}} - \frac{1}{2\lambda d'} + Bx^{m-1} + Cx^{m-2m}\dot{x}\sqrt{\frac{m-r}{x^m-b}} - \frac{1}{2\lambda d'} + Bx^{m-1} + Cx^{m-2m}\dot{x}\sqrt{\frac{m-r}{x^m-a}} - \frac{1}{2\lambda d'} + Bx^{m-1} + Cx^{m-1}\dot{x}\sqrt{\frac{m-r}{x^m-a}} - \frac{1}{2\lambda d'} + Bx^{m-1}\dot{x}\sqrt{\frac{m-r}{x^m-a}} - \frac{1}{2\lambda d'} + Bx^{m-1}\dot{x}\sqrt{\frac{m-r}{x^m-a}} - \frac{1}{2\lambda d'} + Bx^{m-1}\dot{x}\sqrt{\frac{m-r}{x^m-a}} - \frac{1}{2\lambda d'} + \frac{1}{2\lambda d'}$ 

The utility of finding fluents by continuation was manifest to Sir Isaac Newton, who first proposed it; and since his time some of the most eminent mathematicians have employed much of their attention upon it. The method which I have investigated and exemplified in this Paper I offer as being entirely new; and at the same time it not only exhibits, at once, the general law up to the required fluent, but also appears, from some of the instances here given, to be more extensive and convenient in its application than any method hitherto offered.

The general resolution of the given fluxion into a series of fluxions of the same kind, where the index of the unknown quantity without the vinculum keeps decreasing or increasing either by the index under or by half the index, has not, that I know of, before been given; which furnishes us at once not only with a very easy method of continuing fluents, but also points out a very simple method of investigating the fluent of the given fluxion without continuation. For if  $\int \dot{A} = p + b \int \dot{B}$  $+c\int \dot{C} + d\int \dot{D} + &c. \int \dot{B} = p' + c' \int \dot{C} + d' \int \dot{D} + &c. \int \dot{C} =$  $p'' + d'' \int \dot{\mathbf{D}} + &c. &c. &c. &c. &then if for <math>\int \dot{\mathbf{B}}, \int \dot{\mathbf{C}}, &c. &c. &c. &we$ substitute their respective values, we shall get a general series for / A without continuation. The extent of any new method is, at first, seldom obvious; and how far that which is here proposed may be successfully employed in other cases will best appear from its application. Different methods will always be found to have their uses in particular cases; for where one becomes impracticable another will often be found to succeed; and I hope that which is here offered will contribute fomething towards facilitating the investigation of fluents.



XXVI. Conjectures relative to the Petrifactions found in St. Peter's Mountain, near Maestricht. By Petrus Camper, M. D. F. R. S.

## Read July 6, 1786.

THE discovery of a great number of petrified bones about the year 1770, in the mountain of St. Peter at Maestricht, and particularly of large jaw-bones with their teeth, suggested to the late M. Hoffman, first Surgeon to the Military Hospital at Maestricht, a worthy member of several learned Societies, and a great admirer of natural history, the idea that these maxillæ belonged to crocodiles. This notion was spread by himself and his literary correspondents through all Europe.

He did me the favour to fend me, not only the history of those petrifactions, but also several figures of the jaw-bones in question, and of other bones, which were all intirely new to me, except some fragments of the bones of turtles. I discovered, however, at the very first sight, the characteristical differences which distinguished these bones from those of crocodiles, of which I had at that time several in my collection.

His intention was to write upon this subject, and to send his essay, containing his reasons for supposing these bones to belong to crocodiles, to the Royal Society; but I dissuaded him, as a friend, from doing this, lest he should afterwards be under a necessity of retracting his opinion: and I sent him a figure of Vol. LXXVI. Mm m

the lower jaw of a crocodile, accurately done by my own hand, and foon after the skull and under jaw of a pretty large crocodile; which induced him to defer his design of writing about these antiquities of the old world, until he should be better informed on the subject of cetaceous sishes.

Major Drouin, of Maestricht, who made, about the same time, a collection of an infinite variety of corals, madrepores, alcyoniums, echinites, belemnites, shells, and petrified wood, from the same mountain and its environs, likewise procured a beautiful specimen of two maxillary bones of the same incognitum, but with the insides turned outwards; and this gentleman also supposed them to belong to the crocodile. A sketch of this specimen is to be found in M. Buchoz's Dons de la Nature, tab. 68. But the specimen itself is now in Teyler's Museum, at Haerlem, with the whole of Major Drouin's collection.

Another still more valuable and perfect specimen is to be seen at the house of the reverend Dean Godding, of which there is likewise a rough sketch in M. Buchoz's Dons de la Nature, pl. 66. In this the greater part of both the upper and under maxillary bones is intire, and a bone, with small teeth, belonging to the palate; by which it appears, the animal had not only teeth in the jaw-bones, but also in the throat, as several sishes have, but which are never found in the mouth of crocodiles.

Notwithstanding all my endeavours to convince my friends, and afterwards M. DROUIN, and particularly the Dean, whose valuable and truly beautiful specimens I saw in the year 1782, I never could prevail upon them to adopt my opinion, that these bones belonged to physeteres or respiring sishes. M. HOFFMANN, adhering closely to the Linnæan System, objected

jected,

jected, that the physeteres had teeth only in the lower jaw-bone, whereas this fossil monster had them in both upper and lower maxilla. He did not seem to recollect, that φυσητής signifies something respiring, or breathing, and applied to sishes, breathing fishes; nor that the physeteres, according to the Linnæan system, have small teeth in the upper jaw-bone, though larger ones in the lower jaw, according to the observations of Dr. Otho Fabricius, in his Fauna Groenlandica, p. 42. where he mentions the macrocephalus, and p. 45. where he speaks of the microps.

In August 1782, I sent M. Godding, who had favoured me with a copy of his valuable specimen, a full demonstration of its being the head of a physeter, or breathing fish, Delphinus, or Orca, or under whatever genus it may be ranked, as having large teeth of the same size in both the maxillæ. But in vain; for he continues still to call it a crocodile, as if its value depended upon the species of the animal.

The analogy of all the other marine bodies seems to make it still more probable, that these large bones belong to the inhabitants of the sea, and not of rivers. The large turtles, the numberless echinites, madrepores, shells, alcyoniums, betermites, orthoceratites, and so on, are all sea animals; and the crocodile would, in that case, be the only inhabitant of the rivers mixed with them.

The pretended crocodile found near Whitby, in Yorkshire, Phil. Trans. vol. L. p. II. 1758, § 92. p. 688. and ibid. § 108. p. 786. is undoubtedly the skeleton of a Balæna.

§ 2. After the decease of M. Hoffman, his family having offered the whole collection for sale, I went in August 1782 to Maestricht on purpose to examine it; and I could not but greatly admire the richness and beauty of the collection, espe-

cially that of the fossil bones from St. Peter's mountain; but as the heirs did not consider the expences necessary to transport the collection down the Maese, where each sovereign puts an enormous duty upon every thing that passes through his territories, nor the small number of persons who were likely to purchase it, they rated the price so high that nobody chose to hid for it.

The eldest daughter having at length become possessed of the whole, offered me the principal specimens at a price I agreed to. Amongst them were the duplicates I have already sent to the British Museum, and with which the honourable Trustees are perfectly satisfied. These specimens may serve ikewise to ascertain what I have said about them, as being eal fragments of physeteres, some of turtles, and the like, but not a single one of any species of crocodile.

§ 3. The arguments for their being jaw-bones and vertebræ of fishes seem to be, first, the smoothness of these bones; and, fecondly, the many holes by which the nerves go out at the fide, and under each tooth, as is very evident in that beautiful specimen now in the British Museum, on the outside of which eleven holes are visible, in the same manner as they are in the delphini, and more particularly in the lower jaw-bone of the cete, the Physeter macrocephalus, or pot-fish, cachalot, &c. Thirdly, the form of the teeth, which have folid roots, as in tab. XV. fig. 6. B, C, E, F, and the fix teeth of tab. XVI. Fourthly, because there are little teeth in the palate, as in Dean Godding's specimen. Fifthly, because the vertebræ have the appearance of true cetaceous vertebræ, as in fig. 5. tab. XV. and in feveral beautiful and large specimens now in the Museum. Several of these vertebræ were besides intirely unknown known to me, and not at all analogous to the vertebræ of the crocodile, described and represented by Dr. N. Grew.

§ 4. As I intended to visit London in 1785, I flattered myself I should still find the skeleton of the great crocodile formerly at Gresham College, and be able to find out such characteristic distinctions as should be necessary to decide the question. Dr. Gray was so kind as to go with me to the lower apartments of the British Museum, where we found, though not without difficulty, the skeleton much neglected, spoiled, and deprived of several interesting parts. I admired, nevertheless, the remainder of it, being infinitely pleased with the transverse sutures, tab. XV. sig. 1, 2. a, b. c, f. δ, ζ. by which not only those of the neck and thorax, but those of the loins also, are divided, and which I made a drawing of, as large as the life, the 20th of October, 1785, of which sig. 1. and 2. are very accurate copies.

I confess I had not observed that particular division or suture in the skeleton of a small crocodile, of thirteen inches, made by my youngest son; but after being apprized of it by the large skeleton in the Museum, of twelve seet sour inches, Paris measure, on looking at my own when I returned home, I sound them both alike, and that those parts were not epiphyses; of which, however, the transverse processes of the neck. sig. 1. d, e, q, o, n, p, have all the appearance, though there is no other epiphysis to be observed in the rest of the bones of that large skeleton.

When we compare the fossil vertebra, fig. 5. with those now in the Museum, we shall find the epiphyses AB, CD, analogous to a, b, c, d, fig. 4. being the real epiphyses in the vertebra of a young porpoise.

I procured,

I procured, in London, the largest vertebræ of the neck of a turtle I could get, and prepared two of them as in fig. 3. in which, as along the back of that singular creature, I found the transverse divisions a, c, d, f: of all which I have not seen a single instance amongst the dorsal spinæ from St. Peter's mountain, one of which consists of seven, another of twelve, and a third of sourteen vertebræ. Some of the vertebræ have, I acknowledge, an inferior process, as in the crocodile, l, m, sig. 1. Of these I have sent likewise two to the Museum. The oftrich, and the turtle Mydas, have such processes, but no quadruped I know of.

The articulation of the vertebræ with each other, by the furfaces of the bodies themselves, is intirely different, not only from that of the crocodile, but from that of all the cetaceous sishes I have ever seen: and I dare venture to assert, I have seen a great many, exclusive of those in my collection. The anterior part of the Maestricht vertebræ is more or less triangular and hollow, as in sig. 5. C, D, L. The posterior A B is convex. Both these surfaces are very smooth, as if they had been covered with a very thin cartilage, and moved one upon the other, without being united by an elastic lamella, as in all quadrupeds and cetaceous sishes; in which the vertebræ have on both the surfaces a round brim, or circular edge, a, b, i, b, by means of which the ligaments are connected, and a flat hollow surface within, as b, i, sig. 4. for the elastic pulp that is between them.

§ 5. The dentition is so singular in these fossil jaw-bones that it deserves a particular description. In all quadrupeds, as in man, the teeth which appear first are all shed at a certain period of life, and in the mean time new ones are formed above, under, or at the sides of the primordial or temporary

teeth,

teeth, but in different fockets. The grinders are not all renewed, but in general three when there are fix, and two when there are five. Nature, however, is not always uniform in this operation. Mr. John Hunter, a worthy Member of our Society, has given a very interesting and complete natural history of the teeth, in which these observations are stated.

In the crocodile the succeeding or secondary teeth appear even when the animal's head is equal to two seet; that is, when it has acquired one-third of its usual growth. When they grow too fast, before the temporary tooth is shed, they perforate the side of the bone, at the part where they meet with the least resistance. Instances of this variety occur in the large crocodile's head, which is in my collection.

In all quadrupeds the enamel is, of the folid parts of the teeth, the first formed, making a cavity, in which the other bony substance is deposited, and formed by lamellæ placed one within another, as is observed by Mr. John Hunter in the work already mentioned, p. 92. To this the root is added, which is filled in the same manner till the tooth is long enough to pierce through the gums.

But in the fossil jaw bones of St. Peter's mountain, a small secondary tooth is formed, with its enamel and solid root at once, within the bony substance of the primordial or temporary tooth itself, as is to be seen in the small fragment now in the British Museum, and in tab. XVI. A, B, C, D, E; which, by continuing to grow, seem to make by degrees sufficient cavities in the bony roots of the primary teeth: but what becomes of them at last, and how they are shed, I am not able to guess. I have one in my collection, where the succeeding tooth is intirely formed within the center and substance of the primordial tooth. In the 6th figure (tab.XV.) a little oyal cavity is observable,

observable, which has been the feat of a new or secondary tooth.

§ 6. The maxilla inferior of the incognitum, fent by me to the British Museum, is a most magnificent specimen, having fourteen teeth. A similar one, somewhat longer (as it measures 3? feet) in my own collection, has also fourteen. Another fragment of the left side, two feet long and eight inches broad, shews the primordial and succeeding teeth in the clearest manner.

The specimen, of which I sent a drawing (tab. XVI.) to the illustrious President of our Society, Sir Joseph Banks, is still more useful to confirm the mode of dentition than any other I have in my museum.

§ 7. Several ribs and the phalanges of the toes of the fore-feet, a specimen of which I sent in a fragment from the same rock, of about a foot long and eight inches broad, may serve as another proof of the difference between these and the crocodile's toes, when compared with the still valuable, though neglected, skeleton in the British Museum; which I am forry I could not make a drawing of, having been too much employed on other objects.

All these characteristic differences cannot fail to convince the learned Society of the truth of what I have afferted, about the animal these bones belonged to; for though we cannot determine exactly the species itself, yet I flatter myself the preceding observations evidently prove, that they did not belong to any animal of the crocodile kind.

§ 8. Another very beautiful specimen, a foot and a half long, and about ten inches broad, I have been induced to add, because it contains the anterior part of the scutum of a very large turtle. Of this Mr. JOHN HUNTER has an analogous bone

bone from the same mountain in his valuable collection, but sent to him under another name. I am convinced it belonged formerly to a turtle; sirst, because I have from the same mountain the intire back of a turtle, sour feet long and sixteen inches broad, a little damaged at the sides, and a pretty large fragment of another turtle, in my possession. 2dly, Because I have a similar one, but so placed within the matrix as to shew the inside, which is perseally analogous to the inside of that piece in the back of a large turtle I got in London, by the favour of Mr. Sheldon. 3dly, Because I have amongst these bones the lower jaw-bone of a very large turtle, of which the crura, though not intire, are seven inches long, and distant from one another six inches; the thickness is equal to 14 inch.

All these fragments prove the frequency of turtle bones amongst the other fossil bones found in the mountain near Maestricht.

Dr. MICHAELIS wrote to me some time ago, that the abovementioned fragment, in Mr. J. Hunter's Collection, belonged to a bird; which I could hardly believe, as I never had fren in any collection whatfoever, either in London, Paris, Bruffels, Gottingen, Cassel, Brunswic, Hanover, or Berlin, nor in my own country, any fossil bone belonging to a bird. I know there is a small one described in the Abbé Rozier's Journal de Physique, for March 1782, which is at present in the collection of M. D'ARCET, at Paris. I expect also from Montmartre a small leg of a petrified bird; but these are the only ones I have ever heard of, those of Stonesield, near Woodftock, being most undoubtedly of fishes. I think it is a circumstance worthy the attention of the curious, that no human N n nbones. Vol. LXXVI.

# Dr. CAMPER's Conjectures relative to the

bones, and of birds but very few, have been hitherto found in a petrified state, and belonging to the old world.

## PETRUS CAMPER.

Klein Lankum, near Francker, June 18, 1786.

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## EXPLANATION OF THE PLATES.

#### T A B. XV.

Fig. 1, 2. Are vertebræ taken from the skeleton of the crocodile described by Dr. Neh. Grew, in his Catalogue of the Natural Rarities at Gresham College, p. 42. and p. 43.

 $a, b. c, f. \delta, \zeta$  the bodies of the vertebræ; a, b of the fourth; c, f of the first vertebra of the neck;  $\beta, z, t$  and x, y, w the spinous processes;  $\gamma \beta$  and s the ascending; t, and u v the descending processes; g, b, c, i. d, e, n, p, o, q. the transverse, united by cartilages to the bodies of the vertebræ. Grew calls them of a mucronata. The transverse processes of the fourth vertebra being lost, the roots of the mucronated processes are very evident at g b, i k.

On the under part of these vertebræ are (l and m) processes, similar to those we find in the vertebræ of the neck in turtles and birds. Not only the six posterior but the sive anterior vertebræ of the back are provided with such processes; of these, however, Dr. Grew makes no mention.

Fig. 2. Represents the seventh vertebra of the back; A, and C. are the ascending and descending process, forming the articulations with the adjacent vertebra; B. the transverse process, to which is united the rib FB. in B.; DE. the spinous process; H, H, I. the body of the same vertebra.

These figures are as large as the life, and made from the same skeleton, now in the British Museum. The whole length is equal to 12; feet, Paris measure; the head equal to 2 feet; the neck equal to 1 foot; the trunk equal to 3 feet 8 inches; the tail equal to 5 feet 8 inches. The measurement given by Dr. Grew does not agree with mine; but he seems not to have taken it with great attention (p. 42.), for he makes use of the words about, almost, &c.

OBSERVATION. What struck me was, the transverse suture, a, b. c, f. δ, ζ. which divided the bodies of all the vertebræ of the neck, back, and loins. This division ended with the os sacrum, which was intire, as were also the vertebræ of the tail. Dr. Grew seems only to haven taken notice of the sutures belonging to the transverse processes.

I have a small skeleton of a crocodile equal to 13 inches, in which the 7 vertebræ of the neck, 12 of the back, and the 5 of the loins, are divided in the same manner as in the large skeleton in the British Museum. Those of the os facrum and tail are without, and have no mark of an epiphysis.

CONCLUSION. The transverse division of the vertebræ abovementioned is also peculiar to this animal; and there is no epiphysis, as in other animals.

To be fure of this, I diffected and made a skeleton of the Lacerta Iguana, Linn. sp. 26. perfectly well described by

Nnn2

MARC-

MARCGRAF, Hift. Bras. p. 236. cap. 11.; but I found no fuch divisions, though the animal was young, and though it had still epiphyses on the legs, &c. The neck consists of 4 vertebræ, the back of 11, the loins of 9, the os sacrum of 2, as in the crocodile; the tail of more than 60.

The diffection of tortoiles seemed to me of consequence, at least a more accurate inspection of the vertebræ, particularly those of the neck, as being analogous in some respects to those of the crocodile, especially in the structure of the inferior processes D, and E, with l, m, sig. 1.

Fig. 3. Represents two vertebræ of the neck of a pretty large turtle, natural size.

AB, BC. the bodies; L. and I. the ascending, H. and T. the descending processes; R. K. the spinous, a, b. d, e. the transverse, and D. E. the inferior processes.

a, b, c. d, e, f. the transverse division of these, similar to that in the crocodile.

Fig. 4. A vertebra from the tail of a young phocæna or porpoise; in which a, b. is an orbicular plate, united by means of cartilage to the body of the vertebra a, d. which is provided with such a one on both sides, a, b. and c, d.

Those bony lamellæ are the epiphyses of the vertebræ, and are alike in all quadrupeds, to which class all the cetaceous fishes belong. When we consider the structure in general of these last, we find the hind legs only are wanting, and of course the offa innominata; but the offa pubis are very remarkable in all of them.

Fig. 5. Is a fossil vertebra of the unknown animal, whose bones are so often met with in St. Peter's Mountain at Maes-

processes; C, K, I. the medullary canal, running under K, E, F, in a direction parallel to IF, and coming out again at F. The remaining marks of the lamellated epiphyses I, D. and A, B. are evident proofs of the analogy between these and the vertebræ of the cetaceous sishes; and also of their want of resemblance to the vertebræ of the crocodile, as will appear by comparing the first and second sigures with the fifth.

Fig. 6. Is a very accurate drawing of one of the fossil teeth belonging to the same incognitum. ABC is its point, of a lanceolated figure, whose edges BA, and AC, are dentated; BC is the root, uneven, bony, fixed within the socket with D, G, F.; D, G, B, C is covered with the gums; II, I is an oval sinuosity, in which generally the secondary teeth are generated, as is seen in tab. XVI. representing a fragment of the upper jaw-bone of the same incognitum, A, B, C, D, E.

The teeth in all the Physeteres and Delphini have solid roots, except in the young ones, in which they often have cavities to receive the blood-vessels and nerves. But the crocodile has the teeth intirely hollow, as appears in

Fig. 7. in which the cavity  $\Pi$ ,  $\Delta$ ,  $\Theta$ , shews the difference between the crocodile's teeth and those of the cetaceous and other sishes. This tooth is the anterior one of a large head of a crocodile, two feet long, and of the same size as that in the British Museum. A hollow tooth may notwithstanding belong to a Physeter, as Dr. Otho Fabricius observes in his Fauna Groenlandica, p. 44. when speaking of the Physeter microps: of which he says, "Habet in maxilla inferiori dentes

# Dr. CAMPER's Conjectures, &c.

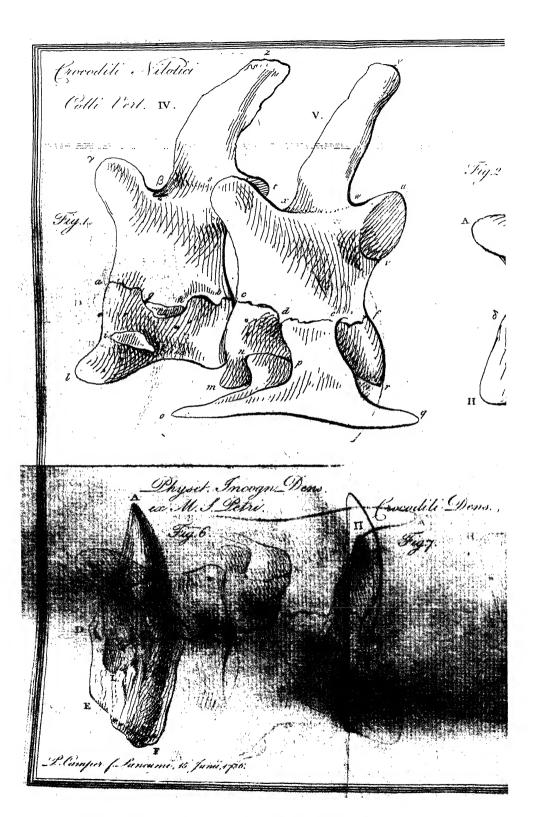
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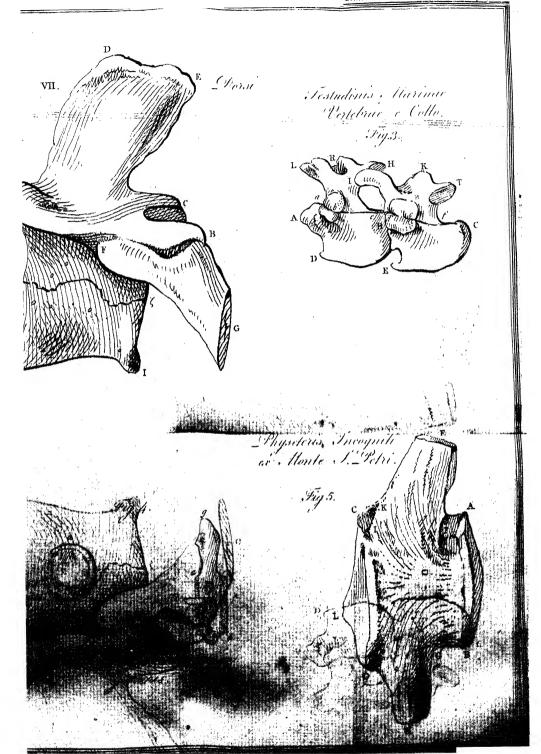
22, utrinque 11 arcuatos, falciformes, intus ad apicem usque cavos," within they are hollow to the very end.

#### T A B. XVI.

Fragmentum Maxillæ superioris, lateris dextri capitis Physeteris incogniti, ex Monte St. Petri, Traj. ad Mosam. Origo dentium serotinorum ex ipsis radicibus solidis primo enatorum in quinque manisesta est. Quæ ad dentitionem hanc singularem pertinent, ex sigur. 2. Tab. Fragm. similis sed Maxill. inst. 12 Aug. 1784. peti debent.











XXVII. Catalogue of One Thousand new Nebulæ and Clusters of Stars. By William Herschel, LL.D. F. R. S.

## Read April 27, 1786.

THE following Catalogue, which contains one thousand new Nebulæ and Clusters of stars, is extracted from a steries of observations (or Sweeps of the heavens), which was begun in the year 1783, and which I am still continuing till the whole be completed. As I may, perhaps, find an opportunity hereafter to publish these observations at full length, I shall now only mention such circumstances, relating to the instrument and apparatus with which they were made, as will be necessary to shew what degree of accuracy may be expected in the determination of the places of these Nebulæ and Clusters of stars; and also to serve any astronomer, who wishes to review them, to form a judgment what instrument will suffice for this purpose.

The telescope I have used, as has been observed on a former occasion\*, is a Newtonian reflector of 20-seet socal length, and 18.75 inches aperture. The sweeping power has been 157, except where another is expressly mentioned. The sield of view 15' 4".

My eye-glass is mounted on that side of an octagon tube, which, in the horizontal position of the instrument, makes an angle of 45° with the vertical; having found, by experience, that this position, resembling the situation of a reading desk, is

<sup>\*</sup> Philosophical Transactions, vol. LXXIV. p. 437.

preferable to the perpendicular one commonly used in the Newtonian construction.

In the present improved state of the apparatus this telescope will, in general, give the relative place of an object by a single observation true to within 1½ or 2 minutes of polar distance, and 4 or 6 seconds of time in right ascension. But when there is an opportunity of repeating the observation, it will hardly disser a single minute in the former, and seldom so much as 3 or 4" in the latter. My apparatus, however, has not been equally perfect from the beginning; for, being from time to time adapted to the different views I had in sweeping, it could only arrive to its present degree of perfection by many experiments and gradual improvements.

To begin a short history of this 20-sect telescope. In the month of October of the already mentioned year I began to use it, being then mounted on its present stand, but with a lateral motion under the point of support of the great speculum, by which its direction could be changed about 15 degrees. It had also a kind of moveable gallery in front, about nine feet long, which permitted me to follow a celestial object near 15 degrees more; by which means I obtained a range of 30 degrees without moving the stand. The Newtonian form has the capital advantage of rendering observations equally commodious in all altitudes; I had therefore placed the instrument in the meridian, that I might view the stars in their most favourable situation.

When I had seen most of the objects I wished to examine, I proceeded to the work of a general review of the heavens. The first method that occurred was, to suffer the telescope to hang freely in the center; then, walking backwards and forwards on the moveable gallery, I drew the instrument from that

that position by a handle fastened to a place near the eye glass, so as to make it follow me, and perform a kind of very slow oscillations of 12 or 14 degrees in breadth, each taking up generally from 4 to 5 minutes of time. At the end of each oscillation I made a short memorandum of the objects I chanced to see; and when a new nebula or cluster of stars came in my way, I made a delineation of the stars in the field of view, both of the finder and of the telescope, that it might serve me to find them again. This being done, the instrument was, by means of a fine motion under my hands, either lowered or raised about 8 or 10 minutes, and another oscillation was then performed like the first. Thus I continued generally for about 10, 20, or 30 oscillations, according as circumstances would permit; and the whole of it was then called a Sweep, and as such numbered and registered in my journal.

When I had completed 41 Sweeps, the disadvantages of this method were too evident to proceed any longer. By going into the light so often as was necessary to write down my observations, the eye could never return foon enough to that full dilatation of the iris which is absolutely required for delicate observations. The difficulty also of keeping a proper memorandum of the parts of the heavens which had been examined in so irregular a manner, intermixed with many short and long ftops while I was writing, as well as the fatigue attending the motion, upon a not very convenient gallery, with a telescope in my hands of no little weight, especially at the extremes of the ofcillations, where it made a confiderable arch upwards, were fufficient motives to induce me to look out for another method of fweeping. And it is evident, that the places of nebulæ hitherto determined, which was till the 13th of December, 1783, must be liable to great inaccuracy. I therefore began 000 Vol. LXXVI.

began now to fweep with a vertical motion; and as this increased the labour of continually elevating and depressing the telescope by hand, I called in the affistance of a workman to do that part of the business, by which means I could observe very commodiously, and for a much longer time than before.

Soon after I removed also the only then remaining obstacle to seeing well, by having recourse to an affistant, whose care it was to write down, and at the same time loudly to repeat after me, every thing I required to be written down. In this manner all the descriptions of nebulæ and other observations were recorded; by which I obtained the singular advantage that the descriptions were actually writing and repeating to me while I had the object before my eye, and could at pleasure correct them, whenever they disagreed with the picture before me without looking from it.

In about half a dozen sweeps, done according to this new way, I found that the stars of Flamsteed's Catalogue entered nearly at the time when they were expected; this suggested the possibility of converting my telescope into a transit instrument. By way of trial, Dec. 18, 1783, I began to use a watch, and noted the times of the transits of stars and nebulæ to the nearest minute; and, this succeeding, Dec. 24, a sidereal time-piece was introduced.

I found also that, by the turns of the handle which gave motion to the telescope, it was practicable, in a coarse way, to ascertain the difference of altitude between any two objects that passed the field of view; on which account, Dec. 30, I began to use an index-board, divided into inches, and marked with numbers, which, being placed behind the rope that moved the telescope, would point out at what altitude a certain index, affixed to the rope, was situated. My tackle of ropes and

pullies was fuch that, while the telescope traversed an arch of two degrees, the mark on the rope passed over about 24 inches of the index-board: but the exact measure was always to be determined experimentally, as it varied according to the fituation of the instrument. I perceived immediately that the quantity of rope used in the motion of the telescope would be much better observed by the affistant, if the index were brought within doors near the writing desk: to effect this, 1 used a small cord, which, being led off from the great one, was carried over a pulley into the observatory, so as to pass over a fet of numbers, which I now divided into fuch parts as, in an equatorial fituation of the inftrument, would give nearly each equal to one minute.

It would exceed the limits of this Paper to enumerate the various trials I made to bring the right afcension to greater perfection; fuch as causing the tube sometimes to hang inclining or rubbing against a perpendicular plane; at others, drawing it against the same by a small weight, fastened to a cord, paffing over a fide pulley, &c. I shall also pass over the several changes in the form of the machine shewing the polar distance, which, for convenience fake, was foon brought to an index moving over a dial, in the manner of a clock.

By way of directing the person who gives motion to the telescope, a small machinery was added, which strikes a bell at each extreme of the breadth of the fweep, and is adjustable to any required number of turns of the handle.

In June, 1784, I introduced a finall quadrant of altitude, the use of which became soon after of the greatest consequence in determining the value of the numbers of the polar distance piece. Hitherto I had fettled this value by caufing a ftar to pass vertically through the field of the finder, which was very accurately accurately limited to two degrees; but now I found, by many comparisons between the degree determined by the quadrant and by the finder, that I had generally under-rated the value of the numbers. Fortunately so many stars of Flams i edd's Catalogue had been taken, that the numbers between their different polar distances were sufficient to recover the value of the degree; but this occasioned a laborious re-calculation of the places of all objects taken in near 300 sweeps. The quadrant being once introduced, I carried the refinements of the determination, in high sweeps where the ropes acted very unequally, so far as to ascertain by it separately the value of every 20 or 30 minutes throughout the whole breadth of a sweep of two degrees, and the numbers were then accordingly cast up by so many different tables calculated on purpose.

Being still disappointed in many instances, when, on a review of a nebula whose place I had before determined, I perceived a difference of 4 or 5 minutes in polar distance, I began at last intirely to new model the machinery of the polar distance piece, and on Sept. 24, 1785, completed one with the following capital improvements. My former piece shewed a set of numbers whose value differed in every situation of the telescope, and therefore required different and very extensive tables to cast them up in degrees and minutes. This shews at once both the degree and minute of the polar distance of every celestial object, without requiring any tables to cast up numbers. the next place, the confiderable inaccuracy arifing from the unequal tension of the great ropes, and their expansion or contraction by moisture or dryness, is intirely taken away; for now my index cord is contrived so as to go off from the front of the telescope itself, in the direction of a tangent to the arch it describes when moving; by which means this cord will even

ferve as an hygroineter to shew the variations of the ropes that suspend the telescope. If a shower of rain, for instance, should shorten them so as to elevate the telescope 2, 4, or 6 minutes, which has happened fometimes, notwithstanding they have all been well faturated with oil, the index cord will immediately make the polar-distance-clock show this effect of the rain, by pointing out an equal change on the dial. As to the variations of the cord itself, they are in the first place very trifling, fince it confifts merely of a few threads of hemp, very loofely twisted, well oiled, and always equally stretched; but especially these variations are of no consequence, as they are so easily to be discovered by the check of the quadrant of altitude affixed to the telescope, or the successive transits of known stars, and may either be immediately corrected by the adjustable hand of the polar distance dial, or be left to be accounted for afterwards.

The improvement of the right ascension has not been less attended to; and the Royal Society having kindly intrusted me with an excellent time-piece, I succeeded at last by means of the addition of the following apparatus. Against the side of the tube is fixed a vertical iron plate, and the point of suspension of the telescope is disposed so as to permit this plate to be just in contact with a roller which remains fixed during the time of a sweep. There is also a considerable spring applied on the opposite side, in such a manner as, by always exerting a pressure nearly uniform, to cause the iron plate to rub against the fixed roller as the telescope sweeps up and down. By this means I have frequently, in very stormy weather, observed many hours without sinding my time materially affected, and the corrections will soldom, in accurate observations, exceed a few seconds.

## Dr. HERSCHEL'S Catalogue of One Thousand

To those who are accustomed to the accuracy of trustit instruments in regular observatories, this telescope, notwith-standing the above-mentioned improvements, may perhaps appear far from being brought to persection; but they should recollect the size of the instrument as well as its extensive use, since I can not only follow any object for near a quarter of an hour, without disturbing the situation of the apparatus, but can at pleasure, in a few minutes, turn it to any part of the heavens, and view a celestial object wheresoever it may chance to be situated, even the zenith not excepted.

From this account it will be understood, that the places of a few of the nebulæ and clusters of stars, determined before the 13th of December, 1783, may be faulty in right ascension as far as 1' of time, and in polar distance to 8 or 10' of space. Afterwards the errors will be found to become gradually less considerable till the latter end of the year 1784, when, I suppose, they will seldom exceed half that quantity. From that period to Sept. 24, 1785, they will diminish, and probably not often amount to so much as 3 or 4' in polar distance, and 10 or 12" in right ascension. And now I flatter myself that all places, determined since the last mentioned time, will generally be true to a very small quantity; such as 4 or 6" in right ascension, and 1½ or 2' in polar distance, and often much nearer.

Some of the nebulæ in that part of the heavens which, in a former Paper, I have called the stratum of Coma Berenices, are indeed so crowded that there was no possibility of taking them all in the center of the field of view, and a somewhat less degree of accuracy may therefore be expected; but having used myself by very frequent estimations of the parts of the field of view to judge of their value in time as well as in space,

I corrected this defect at the moment of observation by affixing to the transits of these excentric nebulæ such proper marks of plus or minus in right ascention and polar distance as I judged would bring them to a central observation. A similar method, well known to good astronomers in estimating their tenths of seconds by the proportional space over which the stars move in their meridian passage, makes it unnecessary to expaniate on the degree of accuracy that long practice enables us herein to obtain.

If, however, I had been willing to delay giving this catalogue till, by a repeated review of the heavens, the places had been more accurately determined, the work would undoubtedly have been more perfect; but whoever confiders that it requires years to go through fuch observations will perhaps think with me, that it is the best way to give them in their present state, if it were but to announce the existence of such objects by way of inducing other astronomers also to look out for them. Another motive for not delaying this communication is to shew that my late endeavours to delineate the construction of the heavens have been guided by a careful inspection of them; and, probably, a catalogue which points out no less than one thousand instances of such systems as those are into which I have shewn the heavens to be divided, will considerably support what has been said on this subject in my two last Papers.

When the diurnal motion of the earth was first maintained, it could not but greatly add to the reception of this opinion when the telescope exposed to our view Jupiter, Mars, and Venus, revolving on their axes\*; and if these instances of

To these may now also be added Saturn, on whose body I have, in the year 1780, seen several belts, with spots that changed their situation in the course of a few nights.

the similar condition of other planets support the doctrine of the diurnal motion, the view of so many indereal systems, some of which we may discern to be of a most surprising extent and grandeur, will in like manner add credit to what I have proposed with regard to the condition of our situation within a system of stars: for, to the inhabitants of the nebulæ of the present catalogue, our sidereal system must appear either as a small nebulous patch; an extended streak of milky light; a large resolvable nebula; a very compressed cluster of minute stars hardly discernible; or as an immense collection of large scattered stars of various sizes. And either of these appearances will take place with them according as their own situation is more or less remote from ours.

In the distribution of the nebulæ and clusters of stars into classes, I have partly considered the convenience of other observers: thus, in the first class, the degree of brightness of the nebulæ has been the leading feature, as most likely to point out those which their several instruments may give them expectation to reach. The first class, therefore, contains the brightest of them; the second, those that shine but with a seeble light; and in the third are placed all the very faint ones. Besides this general division, I have added a fourth and a sifth class, which contain nebulæ that, on different accounts, seemed to deserve a more particular description than I had allotted to the three former divisions.

The clusters of stars are forted by their apparent compression, in the manner of my former Catalogues of double, treble, and multiple stars; so that the closest and richest clusters take up the first class; the brightest, largest, and pretty much compressed ones, the second; and those, which consist only of scattered and less collected large stars, are put into the last.

In every class the order of time when the nebulæ and clusters of stars were discovered, or first observed with my 20-feet telescope, has been followed; and that I might describe all these objects in as small a compass as could well be done, I have used single letters to express whole words, an explanation of which, with an example of the manner of reading those letters, is given. It should be observed, that all estimations of brightness and size must be referred to the instrument with which the nebulæ and clusters of stars were seen; the clearness and transparency of the atmosphere, the degree of attention, and many more particular circumstances, should also be taken into consideration; so that probably some of the nebulæ which I have called very bright, and very large, may only be just perceivable, as very small faint patches, in many of our best common telescopes.

The Identity of each nebula in this catalogue has been well ascertained by a projection on a proper map, made on purpose, which pointed out all other nebulæ near its place, and thus afforded the means of a rigorous examination. When, therefore, several nebulæ are found within the limits of the accuracy with which my telescope can discriminate them, in different nights, it may be concluded, that they were seen either at once in the same field of view, or otherwise in immediate succession during the same sweep.

In the same manner these nebulæ have been compared with those that are contained in the two volumes of the Connoissance des Temps, for the years 1783 and 1784, of which none have been inserted in this catalogue. It was indeed easy enough to distinguish the nebulæ of that excellent collection from those of mine which in several places are very near them: The quantity of good light in my telescope having enabled me, Vol. LXXVI.

Ppp

even

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even in bright moon-light nights, to fee occasionally some of the most feeble of the former, when the latter could not by any means be perceived.

Perhaps it will not be displeasing to those who may look out for some of the objects contained in this catalogue, to know that the pictures which were given in a former Paper, representing the various shapes and appearances of several nebulæ, have been actually taken from nature, by Drawings made of them while I had them in view; I have therefore added a reference to these sigures, as the descriptions of the originals which they represent occur in their order in the catalogue.

# Arrangement of the columns, and explanations of the abbreviations.

The first column contains the class and number of the nebulæ.

In the fecond are the dates when the nebulæ were first

The third column contains the star, or other object, by which the place has been determined.

In the fourth column the letter p or f shews that the nebula is either preceding or following the star.

In the fifth is the time, in fidereal minutes and feconds, by how much it precedes or follows the same star.

The letter n or f, contained in the fixth column, denotes that the nebula is north or fouth of the determining star.

In the feventh is the quantity, in degrees and minutes, by how much the nebula is more north or more fouth than the fame star.

The eighth column contains the number of observations that have been made of each nebula; and it is to be noted, that

the determination of the place is generally taken from the last observation, on account of the more perfect state of the telescope.

The ninth column, or remaining space, contains the defcription of the nebulæ, by means of single letters, or now and then a few words added to them.

The abbreviations are to be understood as follows.

B. Bright.

v. very.

F. Faint.

c. confiderably.

L. Large.

p. pretty.

S. Small.

e. extremely.

Of these letters I have composed vB. cB. pB. pF. vF. eF. vL. pL. pS. vS. eS.; all which require no farther explanation.

R. Round.

1. a little.

E. Extended.

i. irregularly.

M. in the middle.

g. gradually.

b. brighter.

f. fuddenly.

m. much.

When these are joined we have iR. mE. IE. bM. gbM. fbM. mbM. lbM. glbM. gmbM. smbM., and by taking in some of the former letters BM. vBM. cBM.; where no other remark will be necessary than that writing for instance bM, or brighter in the middle, it is intended to express, that a nebula, which is faint at the borders, is less so towards the middle. And these degrees of brightness happening sometimes to be so well united from the most imperceptible border to a very luminous center, I have, on such occasions, used the expression vgmbM, or very gradually much brighter in the middle.

r. resolvable.

m. milky.

er. (joined) eafily refolvable.

iF. (joined) of an irregular figure.

C. Cometic, or refembling a telescopic comet.

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N. having a Nucleus, or bright compressed spot.

1, b, or d. (joined to minutes) long, broad, or diameter.

st. a star. stars.

n. north. north of.

f. fouth. fouth of.

p. preceding. np. north preceding. fp. fouth preceding.

f. following. nf. north following. ff. fouth following.

betw. between. ver. 240. verified by a power of 240.

bran. branches.

che. chevelure.

mer. in the direction of the meridian.

par. in the direction of the parallel of declination.

np sf. in a direction from north preceding to south following. sp nf. in a direction from south preceding to north following.

Example. I. 13. 22. 69 Leon. p. 7. 57. n. o. 2. 3. vB. mE. mer. fmbM. 7 or 8'1.

13th nebula of the 1st class. Feb. 22, 1784. It precedes the 69th Leonis of FLAMSTEED's Catalogue 7' 57" in time, and is 0° 2' more north than that star. 3 observations. Very bright, much extended in the direction of the meridian of the nebula, suddenly much brighter in the middle 7 or 8' in length.

I. 32.... p. 5. 11. n. o. 28. 3. cB. S. BN. and 2vF bran. 32d nebula of the first class. April 13, 1784. It precedes the 31st (or 1st d) Virginis of FL. Cat. 5' 11" in time, and is 0° 28' more north than that star. 3 observations. Considerably bright, small, having a bright nucleus, and two very faint branches.

First class. Bright nebulæ.

I.	1783	Stars.		M.	s.		D.	м.	υ.	Description.
1	Dec. 10	82 (3) Ceti	f	2	17	n	0	8	7	cD. cL. iF. bM.
2		3 Leonis	p	18				12		cB.cL vgb N. R.
		34 Sextant	p	28	55	i	0	13	+	cB. pL. C. mbM.
3 4			p	28	27	ſ	0	10	4	cB. pL. C. mbM.
5	30	81 Leonis	P	2	42	n	0	7	2	B. pS. 1R. bM. r.
	1784									
6		64 Virginis	f	33	56	ſ	0	I		vB. pL. gmbM.
7 8	23	49 Leouis	ſ	120	45	1	0	40		v3. L R. The place inac.
8		32 (2.) Virg	f		50	11	0	48	5	cB. pL. iR. mbM. r.
ç	24	10 (1) Virg	f		I,	1	0	35	4	cB. E np ff. N and 2 bian. 31.
10			f	33	3	n	0	4	•	vB. pL. lE. gmbM. 2'l. 1½'b.
11	Feb. 15	5 Comæ Be.	p f		30	1	•	II		1 - 1
12	10	6 Comæ	t	9	I 2	i	0	ç	2	B ps. R. BM. r.
13	22	69 Leonis	P	7	57	n	0	2	3	vB. mE mer. fmbM. 7 or 8'1.   Fig. 11.
<b>5</b> 4		29 (7) Virg	f	0	43	n	1	23	2	cB. cL. niE. near par. 3 or 4'l.
15			f	3	23		0			cB niE sp nf. ibM. 4 or 5' l.
16			f	10				13		
17	3	Le cornel	f	15	50	ſ	I			The 2 p of 3. Both vB. cL. mbM.
18	Mar. I	46 (i) Leo	f	16	18	ſ	1	•		C. II 41. Fig. 4.
19	14	11 Comæ	P				0	46		1 =
20		73 (n) Leonis	f	8	52	1	I			vB. mE. nearly par.
21	`		f	25	31	1	1			vB. cL. R. gmbM.
21	`	-34 Virginis	P	22	24	1	0	17		( <u> </u>
23	-		P	18	24	1	0	19	2	B. S. mE.
24	I .	-30 (g) Virg	P	I	42	ſſ	0	_		
25	-	-34 Virginis	f	4	45	1		40	1	1
26	1	952(K) Leonis	P	3	45	ſ	2	•		
27	Apr.	8 40 (1) Leonis	f	18	47	1	0	43	3	vB. BNM, and 2 F bran. np ff.
28	-	-34 Virginis	P	19	36	n	I	8	2	One of two, at 4 or 5'. dift  B. cL.
29	1	2 73 (n) Leonis	l D	Y	(	ſ	c	30	3	1
30	li .	331 (1 d) Vir			4	n	c		2	
31		31 (1 d) Vu	p	8		n	1	-		1 72 77 124 7 . 78
32	1	-1' - ' - '	P	1 -				28	4	cB. S. BN. and 2 vF. bran.
3-	ı	5 ( v) Virgin	f	3		2 11		39	i	B. L. mE. mbM. r.
3 · 3 ·		_59 ( ) Virgii	ı f		4	2 f	c	34		vB. cL. E np ff. SBN.
3.9	r	7 34 Virginis	P	1	4:	2 n	1			
38	1	1		1 -		1	1		١,	Two. Both B.
37	} -	7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	P			ł	1	20	1	(0.12)
38	(L I	8 32 (2 d) Vir	g) P	111	3	ol n	I I C	, (	) 1	B. vL. mE. mbM

I.	1784	Stars.		M.	s.		D.I	M	ОЬ	Description.
39 43	Apr. 24	[ · · · · ]	p p	21	36 f 48 r	1	0	14	I	vB, vL. fmbM, rN. cL. vB\nM.
41 42		2) (%' Viigin	t t	9 30	24 F 27 I	1	1	8	- (	B. L. iR. lbM. cB. L. iR. vgbM.
43	21	51 (1) Ophiu	' 1		1 (1	1 0	0	51	2	E. vBM. 5 or 6' 1. cB. pl. N.
45 46	_	1	1	0	36 r 54 r 48 f	1		46	1	B. R vgmbM. pB. cL. R. BM. r. B. vL. iF. er. st visible.
<b>4</b> 7 48	17	43 (d) Sagit	. 1	114	6	a	I	33 4+	I I	B. L. R. gbM, er. B. pL, bM. r.
49 <b>5</b> 0	-		t	3		۱ ۱	0	23 33 13	I	cL, R. vBM. m. cL. R. vBM. er.
5: 52	Aug. 2.	22 (2) Sagit 17 Delphini 60 (2) Cygni	r	· 6 · 78	0	n	2	24 51	4	vB. S. R. gmbM. r. vB. cL. mE. mbM. r.
53 5÷	Oct. 5	35 (v) Andr 06 Pegali	f P	12	44	ſ n		50 2		B. cL. R. mbM. Place inacc. cB. mE. mer. gbM. 4'l. 2'b.
55 56 57	Nov. 16	64 (1) Leonis		0	46			29	1	Two, at 1' distance. Both cB. cL. appear like one mE.
5 <sup>5</sup> 59 60	20	7 19 Eridar: 0 15 (1) Navis			18	f n	0 0	22 21 16	1	1
	1785	9 19 Eridani	P	6	5 <sup>1</sup>					
61 62	11	66 Sextantis 055 (& Ceti –80 Ceti	P P f		25 12	n	0	37 25	2	cB. pL. E. bM.
63 64	-	-8 (1 p) Erid 731 Crateris	P İ	15	30	n	0	2 52	2	1
65 66 67		8 12 Hydræ -8 (n) Corvi	f P	25 37	2	ſ n	1 2	7	I	B. vs. iF. mbM.
68 69	_	- 53 Virginis	P P	12	40 4	n n	I	4 34	1	cB. pL. iR.
70 71	-	5 106 Virginis 19 (3) Libræ	P	0	3	n n	I	54 4	. 2	cB. vS. b towards f fide.
72 73 74		3 23 Leonis min	P	13 50	17	n f f	0	13 22 11	I	vB. S.
74 75 76		13 Cán. vena	P P	43 40 38	35		I	9	I	vB.
77 78	April .	3 27 Urfæ	P		3 13 46	n	0	23		vB. L. broadly E. bM.
79 <b>8</b> 0	-		f	33 97	5 <sup>2</sup>	n	1		1	cB. pL. R. vgmbM.
81		641Leonis min	P,	0						cB. cL, m. just p 2 st.

I.	1785	Stars.		M.	s		D.	м.	O¤	Description.
82 83 84 85 86 87 88 99 91 92 93	10	14 (b) Comæ 21 (g) Comæ 40 Comæ 39 Leonis min 44 Leonis min 14 (b) Comæ 15 (c) Comæ	t t t P t r P P	0 19 5 13 9 13 8 6 1	10	n n n n n n n n n n f	I 0 0 0 1 0 0 0	55 18 59 1 55 57	I I I I I I I I I I I I I I I I I I I	cB pl, 1R. mbM. cB 1R. i BM. m. 7 or 8' d. cB. pL. cB. pL. mlM. brightness IE. vB. vL. go.M. cB. cL. 1R. mbM. vB. S. IE. The np of 2 cB. pL R. II. 377. vB. E. par. pBLN. and and and and and all the statements.

### Second class. Faint nebulæ.

ш.	1783	Stars.		М.	s		D.	м.	Oh.	Description.
3 4 5 6 7 8 9 10	Dec. 13 18	11 Aquarii 24(α)Pıf. auft 17 (1 φ) Ceti 41 Ceti 82 (δ) Ceti 	pf pppff	15 14 9 15 0 1 1 2 2 13 1	40 :: 13 5 :: 13 11 18 38 24		0 0 12 0 0 0 0	54 41 42	268134422	pB. S. iF. mbM. F. L. mE. between 2 cBft. pB. pS. R. mbM. C. pB. S. lE. bM. S. C, between 2 L and 1 S ft. F. pL. iR. vlbM.  Two. The first. F. S. r.  The second, F. vS. r. F. pL. E. sp nf. bM. r. F. pL. nearly R. r.
13 14 15 16 17 18 10 20 21 22 23	2:3	3 (1) Leonis 3 (1) Virginis 20 Virginis 56 Leonis 9 (0) Virginis 31 (1 a) Virg 1. Clafs 7 Neb. 31 Bootis 32 (2 a) Virg 31 Bootis 475 Leonis	f f Qf Q P P	9 80 70 97	20 32 54 4. 21 4.	n f f n	0000000	22 42 32 33 1 12 38 22	1 2 4 3 2 1 2 4 1 2	F. vS. nearly R. F. pl. E. followed by III. 91. F. S. F. pS. R. vS. pB. pL. b towards the p fide. F. vS. F. mE. F. pL.

11.	1784		s	tars,		М.	8.		D.	М,	Ob.	Description.
26 27	Jan.	28	11 (s 31 B	y) Virg	f P	18 9		n t	0 0	45 2	1 3	E_
28	1	- 1		) Leonis	_	3	45			18	I	J Two, about 2' asunder. Both
29 30			68 (8	) Leonis		6	30		2	23	1	F. cL. R. Fig 3.
31		22	29 (y 81 (r	) Virg J Leonis	P	-2 6	31 30		0	55 7	2 I	pB. cL. lE. par. r. pB. vS. bM.
32 33			_		P	6	0	n	0	20	1	pB. pL. R. bM.
3+ 35	•		50 (d	r) Virgin ) Virgin	P	51 8	23 45		I	27 15	4 2	F.S. pB. mbM.
36			00 (0	r) virgio	P	46	5	1	I	29	3	F vL. iR. bM. 6'14'b, pB. E. np ff. mbM.
37 38			35 V	:) Virgin 'irginis	P	13	3°	ſ		40 <b>5</b> 3	2	pB. pL. iF. r.
39 40	Mar.		6 (6	Leonis	P	3		i n	ŧ	20	•	<b>1</b> •
41	1		46 (	i) Leonis	f	16	30	1	I	35	4	The f of 3. F. E.
42 43				·) Leonis ζ) Leonis		3	10	n f	1	12 40	1 2	F. S. pB, cL. iF.
44 45	1	_	20 L	eonis	f	28	15	n	0	48	I	Two. Both. F. E. IbM. r.
46				) Leonis	,	37	30 26	n		29	1	pB. S. r.
47 48			85(1	eonis i) Gemin	P	56	45	ſ	0	49 42	2 I	pB. pL. lbM. contains 1 st.
49 50		-	86 I	.eonis	P	15		ſ	1	19	I,	ygbM, r.  Of three that M.pB. cL.R. bM
5	1		-	***	P	13	30	í		2,2	1	That to the n. S.R. bM. III. 2;
52 53				Leonis	P P	10	36	n	I	.5 19	1 2	pB. S. lE, bM. F. E. r.
5	H s	-		Leonis Comæ	P	1 4	24 45		1	29 24		F. S. R. The f. of 2. r. See Note.
5.5 5			25 0		P	8	30		0	1	2	pL. iR. bM. 2 or 3' d.
57 58	}	15	5 (\$	Leonis	P	7	15	ı	0	18	1	Two, distant 1' np if. The p ps. lbM. r. The f. pL. lbM. r.
59 60		_	72 (	t) Virg	f P	26 5	30 15		0	53 10	I	vS.C. in a row with 2 F and 1 Bi
61	41		1	/irginis	P	26		•	l	31	2	Two. nearly par. The first
62 63			_	_	P	24		١.	o	9	2	pL. E. The fecond F. pL. F   F. pL. mE.
64	H	-	12 (	t) Virg	f f	11	45 45	מ	0	57	I	
65 66			30 (	e) Virg	p	9	30	n	0	56	I	pB.
67 68		_	34 V	rirginis	P P	10	24	ſ	I	6 36	1 2	pB.vS. pB.
þ					P	0	48	ſ	o		2	

τI.	1784	Stars.		М.	8.		D.1	м.	оь.	Description.
70	Mar. 15	30 (¢) Virg	f		45		£	7	I	A nebula.
71			f	2	0	n	I	0	I	S.   S. IE.
72	_	3 Wirginis	f t		15	ſ	I	54	I	F. not vS.
73	-		ı	4	U		-	3		
74 75	} -		f	5	30	ſ	ο.	42	1	Two, nearly par. The pB nearly R. The f. pB. vmE. 8 or ro' distance.
76	l .	20 (x) Serps	P	3	12	i	0	42	2	pB. pL. IE. gbM. r.
77	19	52(K) Leonis	P	4	42	ſ		27	2	pB. pL. E. b. M. r. f. pBft.
78	_		P	0	12	11		27		pB. pL. r.
79	<u> </u>	15 Bootis	t	18	30	1		15		F. L. R. lbM. r. 4 or 5' dia"
80	21	47 (8) Cancri	f	4		n	0	55		pB. pL. E. r. 2 or 3 ft in it.
81		51 (m) Leon	f	I	15	ſ		41	1	pB. pL. not R. r.
82			f	8	15	f	I	35	I	
83	_	3 Comæ	P f	0	15	ſ		43		
04			1,	12			l	<b>5</b> 9	1	Two. The p. pB. S.
85 86	} -	25 Comæ	P	13	C	1	0	21	1	The f. F. S.
87	_	.	P	11	15	1	I	33	1	1
88	_		P	10	4.5	1	0	53		S. bM. r.
89	-	6 Comæ	f	11	1:	21 II	0	31	2	S. bM. r. near Bit.
90	_	25 Comæ	P	7	30	ı	0	3	1	
<u>و</u> و			P	6	(	) 1	0	18	1	
92			J.b	5	30	J.	0	24	١.	•
93	3 -		P	4	. (	1	0	51	I	
94	Η -		P	2		J C	I	35	I	
95 96	_	- 27 Comæ	١.	1	4	1 c	I	23 5	ī	
90		- 15 Serpentis - 26 Serpentis	١.	2				35		
97 98		38 Leonis	f		4.			20		
99		52 (K) Leo	f	0	4	2 1	0	12		1
100			f	13	30		0	42	I	1 2
10	3	-	f	14	. (	ol t	0	20	1	pB. S. mbM.
10	2 -	- 70 (0) Leoni	s f	1		1 8		•	I	F. pS. R. lbM. r.
סנ	3 -	- 94 (B) Leoni	s P	9		2 1				F. S. E. r. 2 or 3 st visible in it.
10.			P					48		pB, S, R. r. pLrN.
10		- 34 Virginis	P		•	6 n 8 n	1	28	2 2	
10	•	6 Comæ	F		-	4 1	I			pL.
10		- Come			) 2	6 1			1	mE. r.
10			I	1		4 1	1			r.
11			1		3 1	2 1				S. r.
LI			1	1		8 1	1			Two, about 2' distant. The
	215		1	1	5 1	٠,١	10	, 11	3	Il first R. r. The 2d, E. r.

II.	1784	Stars.		М.	s.		D.M	ОЬ	Description.
113 114	April 8	6 Comæ 34 Virginis	f P	10	54 54	n n	0 9		E. r. F. r.
115 116	} –	6 Comæ	f	14	3		1 21		Two. Both r.
117	_		f f	15		ſ	0 54 0 28	I	r. S. Note.
119 120 121	, –		f	1ð 18	<b>5</b> 4		0 35	I	pL. r. L. r.
122	f 12	34 Virginis	P	17					Two. Both pF. S. bM.
124 125	} _		P. P				O 29	1 1	The two p. of 3. Both F. S. bM. Note. not vF. S. r.
127	_		P P	3		n	III	2	pB. L. E. r.
129		41 Virginis	f	19		n	0 11	1	L. R. bM. r. F. pL. lbM. R. r.
131 131	13	20 (%) Serps 56 Leonis 8 (%) Virgin	P P P	3	30 48 48	ſ	0 26	1	pB. vL. nearly R. lbM.
133 134	-	) (a) Virginis t I (s) Virgin	f	7	46 24	ſ	0 7 1 41 0 0	2	pL. E. pBM. r. not vF. S. E. mer. F. mE.
135	_	= =	f f	5	54 30	n n	0 38	1	S. E. pBM. F. S. iF. r.
137 138	-1	9 (e) Virginis 11 (s) Virgin		9	32 6		2 2 0 20	3	F. pL. r. F.
139 140 141	} -		f f	9 :	30	n k	, 0	3	Two. The 1st is the largest. The 2d vF.
142	) [		f	13 1	.8	n c	18	3	Three nebulæ. The last is the largest.
145	-10	31 (1 d) Virg 1 0 (σ) Virg 1		17 50 2	8 1	ם כ	42	2	F. pL. the largest of 2. vF. S. E.
145 147 148		1 (1 d) Virg I		14 7 3	6 1		34	1	F. pL. mE, r.
149	_ 	4 (a) Serps p			9 1	ı	53	4	not F. R. vgbM. F. pL. iF. r.
751 152	- 1:	Herculis f (') Leonis f		4 I	8 1 4 1	10	- / 1	1	F. pL. nearly R. er. not vF. pL. iR. bM. r. F. mE. r.
[4]	-]2	(18) Virgin p		3 (	o n	2	2	.  {	Two, about 5' distant. Beth. F. pS. C.
155	-1/20	Virginis   p			1	P	40 1 26 1		F. pL. lE. lb. towards p. fide. F. pL. lE. r.

II.	1784	•	Sta	fø,		М.	\$,		D.	M1.	Ob,	Description.
157			20 Vir		p	3	36 38 36	ſ	I	29		F. pL, mE, bM. r. pT. pL nearly R. r.
158 159		7 =	31 (1 d 81 Leo	nie J V 11 g	P f	0	36	n	6	51 24	3	pB. S. bM. almost stellar.
160		* /	-	***	f	1	- 1			45	1	cL. R. vgbM.
161			go Leo	nis	f	.5	36		0	<b>5</b> 3	I	F. not S. R. bM.
162		<b></b> -	34 Vir	ginis	P	51	54		0	0	2	not vF. pL. iR. 1b. towards f. fide.
163		-	***	-	P	33	6	n	I	13	1	pS.
164		alibea.		<b></b>	p	32				13	1	pS. vmE.
165		***		lens.	₽	32	30	n	I	13		F. vmE.
166		-	-	**	P	27	36	n	0	53	I	pB. vS.
167	ļ	_			p	21	30	n	0	49	I	Two nebulæ.
168	J		ĺ			00	- 1	1	1		ī	The most f. E.
169		-	-	_	b	19	30	n	0	49		F.
170 171		_			P	. 3	4~	-	-	サフ	-	Three nebulæ.
172	}		_	-	p'	19	6	n	o	20	I	The two first vs.
173	5				1		1		1			The third S.
174		-	-	•	P	17	48	n	I	16	I	F.
175			-	<b>~</b>	P	12	26	n	I	9		pF. L.
176		***	-	7000	P	3	48	ſ	0	37		F.
177		-	20 Boo	otis	f	3	30	ſ	I	42	I	pF. not S. 18M. r.
178 179		***	28 (B)	Serp	þ	12	6	ſ	0	7	2	Two, very close. Both S. stellar. The f. is largest.
180	Ť	22	15 (*)	Virg	f	8	<b>5</b> 9	ſ	I	18	3	pB. L. iR. er.
181			29 (7)		f	5	18	ſ	0	58	I	pF. pL. E. r.
182		-	-	'	F	·6	24			54	I	pF. pL. E. r.
183		24	51 (θ)	Virg	·P	30	36					pB. cL. E. vimbM.
184	l .	~~	-	- 1	.p	28		n			I	
185			0 37:	!:-	P	11		ח			I	
186 187		25	28 Vir	Sims	f	12	+42			51	1	pF. cL. R. r. pF. pL. r.
107		-		- 1	f	22			1	51 57		
189			72 (1	/) Virg		21	54 54	1				
190			26 (%	Virg	ıf	23		1	0		2	
191	May	•	49 (8)	'Virg	P	4	,	ſ			1	
192		-	18 Lit	oræ (	ŀf	10		t	0	16	2	pF. pL. iE. mer. nearly.
193		F	1 200 (	Virg	P	59	30	γn	to	48	2	
194		19	12 (d)	Bootis	f	7	42				2	
<b>T95</b>		4	1 39 Op	hiuchi		12	:54	H 0	I	•		pB. cL. iR. ibMer.
<b>19</b> 6	P	2	2 54 Hy	rdræ	P	1 6	-42	2 f £	I		I	
197		_	· 51 (e)	Ophin	ı,	1 35	30	S C	1	1		pB. pL. iR. r.
196	1	24	43 (p)	oagitt'	I	1 18	4:	1	C	ۇ. ئىر	Į I	
19		1 S	6 64 (*)	CONTRA	al I	1 2						pB. pL. R. gBM. r.
200	<b>A</b>	2.	4 10 (y)	- waliti	17	1	* (	) Pril	1	43	41 <b>I</b>	F. ps. r. unequality B.

-	•												
11.	1784			Sta	rs		М.	s		D.	М.	Ob	Description.
201	I lv	12	18	Sag	anı	ı	7	54	1	0	55	I	F. pl., lbM. r.
202	3 -7	- 3 I 7	12	(2)	C'~gni	+	17	30	ſ		53	I	A resolvable nebulous patch of st
203			1	(8)	C, Ti	Р	9	30	î		ΙU	l i	pB, pL th. bM.
204	Ano.				1t* 1.11		9	18		i	50		pB. S. stellar, not verified.
205	** 0		- '_	- "6		p	I	42		0	33	1	pB. cL. iE. oM.
200	Sept.	*7	E2	(4)	. vgm		5	36	n	1	22	ı	F. S. crookedly E. r.
207	dop.		11	(0)	P gafi	Р	34	27	1	I	15	1	cL. R. gmbM. er.
208		10			ı z fi		13	48		I	ő	1	F. cL. R. vgbM. ff. ft.
209					Ai ai	p	5	57		I	12	2	F. pL. iR. equally B. r.
210		IT	31	(8)	Andr	f	18	12	1	0	26	I	F. pL. unequally B. near pBft.
211				Tri		f		24	,	0	35	1	1 m = 1 m = 0
212		12	93	Peg	asi	p	10	42	ſ	0	15	1	pB. pL. lE. mbM. r. i. 2 Fft.
213		_	19	Peg	nii l	P	2	36	n		42	1	[ 54
214					lrom	P	7	18	ſ	t	i5	1	l — — — a
215	1												Three. mer. Nearly equal in
216		-	١.	-	_	f	4	30	n	0	41	I	fize. All. F. vS R. propor-
217	j							-					tion of dist. f to n. 2 to I.
218		-		-	_	f	5	30	n	I	22	I	F.
219	}	_	Ι.	_		f	7	36	1	T	22	I	Two. The p. F. vs.
220	J					Ι-			4	1		1	The f. pl.
221		-	3	(·) <b>1</b>	riang	P	6	12	1		15		F. pl. mE. r. $1\frac{1}{2}$ .
222	1		'	-	-	P	5	12	1		0		1 1
223		Res.	1	_	_	P	2	12	1	1	52	I	pB. pS R.
224		_	1 -		Andr	t	0	18	١.	a	5	1	pB*. cL. R. bM. { * Though \$ And. in the field.
225					Trian	f	4	18		0	39	I	F. vS. R.
226	}				Pegafi		4	54	1	0	5	I	F. pL. bM. elliptical.
227			89	(x)	Pegali	P	10	18	n	Q	32	2	F. cL. mE. r.
228		-	6	(β).	Arietis	P	5	12	n	I	7	1	Two. Both F. ps. iR.
229		75	8.	(0)	Pegasi	D	I	27	n	I	4	I	F. pL. R. bM. r.
230 231		_		(Y) 	-	P	ī	3		1	59	I	F.pl. E. par. contains a stell.or st.
232	1	*****		_		f	6	45	n	1	35	I	F. S. R. or large stellar.
233	,		1		~ ~	P	1	4. T.	n	0	12	3	Two. The p. pB. IE. nearly mer.
234		19	47	(λ)	Pegafi	P	98	33		0	14		The f. F. E. nearly par. 1'11.
235	J	20	FI	Pife	ium	p		43	ſ		36		F. pL. broadly E.
236					Aqua		3	53	n		22		pB pL. iR. mbM.
237				Cet		р	4	48	n		36		F. E. mer. 2' l.
238	O&.				Persei		28	34	1		10		pB. mE. near par. mbM. 4'11'b.
239		7	27	(x)	Persei	P	8	27	n	0	2	1	The 1st of 2. pB. pS. r.
240		8										I	pF. pL. iR. er.
241		_			_ :							1	pS. C.
242		11	48	(µ)	Pegali	P	39	50	ſ	0	54	2	F. S. iR. near and p. 2 or 3 ft.
243	•	-		-	(	1	6	27	1	0	54	2	F. S. iR.

II.	1784	Stars.		M.	s		D.	М.	ОЪ.	Description.
244 245 246 247 248 249 250 251 252	Oâ. 14	54 (a) Pegasi 53 Piscium 19 Arietis 13 Pegasi 54 (a) Pegasi 47 Piscium 54 (a) Pegasi 102 (7) Pisc	PffPPP	30 3	48 36 54 0	n f n n n	2 0 0 0 1	28	I I 2 2 I	F. S. 1E. pB. pL. R. 1bM. F. pL. E. 4 or 5' f. cft. pB R. bM. 1' d. F. pS. a quartile with 3 Sft. F. pS. E. f. pBft. F. 1E. p. vBft. pB. cL. E. r. F. pL. oval. 1bM. p. pBft.
253 254 255 256 257 258 259 260	20 Nov. 16	38 Arietis 82 Pegafi 77 Pegafi 34 Pifcium 15 Eridani 43 (γ) Cancri 4 (λ) Leonis 12 Pegafi	f f P f f P	5 8 1 12 8 20 3 2	54 21 06 54 58 22 8	n n i f n n f	0000111	30 34 11 25 39 54 26 46	1 2 3 1 1	pB pL. E. bM. r. F. S. iR. r. pB. pS. R. gbM. r. F. R. gbM. F. pL. iR. mbM. F. vL. lbM. R. 7 or 8' d. F. S. iF. F. pS. lE. F. iR. lefs than 1' d.
262 263 264 265 267 268 269	20 Dec. 9	27 Eridani - 47 (8) Cancri 4 (1 x) Can 15 (1) Nav 27 Eridani 8 (1) Crateris 10 Crateris 106 (1) Pifc	P f P	67 19 25 6	16	f n n n n i	I	40 15 20 28 25 40 16 22 11	IIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIIII	F. l and iE. above 1' d. not vF. bM. 1'\frac{1}{2} d. F S. pF. pS. iF. lE. bM. F. E. bM. r. 1'\frac{1}{2} d. ". vS. R. lbM. F. S. R. SB point M. C. pB. pL. lE mbM. pB. S. iR. mbM.
270 271 272 273 274 275 276	-20	- 86 (γ) Ceti - 92 (α) Ceti - 92 (α) Ceti - 32 (2 τ) Hyo - 10 (r) Virgin	f p p f	14	54 54 55 58 14	n n f n f	0 1 0 1 0	44 47 32 5	3 1 2 3	Two, very close nearly par. The f. smallest and most n. F. S. iR. F. vS. iE. er.
278 279 280 281 282 283 284 285 286	Jan. (	75 Ceti 35 Eridani 14 Hydræ 28 (A) Hydr 41 Ceti - 80 Ceti - 55 (ζ) Ceti	fff	17 21 3	55 27 28 26 34 50	n n f n	I 0 0 0 1	38 21 40 . 0	2 I 2 2 2 I 2	F. mb. vlbM. about 4' I. F. vs. 16. ver. 240. F. vs. E. pB. cL. 1E. mbM. pB. S. mbM. F. mE about 3' land 3' b.

ıf,	1789	Stais.		M.	Ŋ.		D,I	M	ab	Deferipston.
287 288	Jap. 27	17 Eridani 21 Eridani	p p	10	24 55			12	2 3	F. vS. IE, er, unequally B. F. pL. iR. r.
289	31 Feb. 1	7 (v) Lepor 89 (n) Ceti	p f f	2 49	3 <sup>2</sup>	n n	Q :	5 I 2 I	3	F. pL. i triangular F. v. F. pL. R. lbM. f. pLft.
291	4	26 (τ) Erid 5 (μ) Lepor	P	Q	50	n	Q :	25	I 1 I	pF. mE. mer. 3 or 4' l and 1' b. pB. iR. mbM, ip. pcft. pB. S. iR. hM.
293 294	- 7	6(3b) Crater 31 Crateria	P P P	52 6 I	51 45 48	n n	Ö	18 9 53	I	F. S. E. r F. vS. iF. bM.
295 296 297		89 Virginis	p P	O	12	ומ		24	I	pB. pL. pF. L. mbM.
298	8	8 (n) Carvi	f	_	44	n		51	ı	F. pl. lbM. ½ p. is a S ful-
299 300	A	53 Virginis	P D	11		n	2	48 8	2	pB. pL. mbM. pF. eL. pB. pL. iR, mbM.
301 302		2 (14) Cancr		332		ſ	1	34 40 35	I	pF. vS. bM. er. F. S. mbM. r.
303 304 305	Mar.	II Monoc 20 Sextantis	t P	30	53 14	f n	Q	37 49	3	Some Sst with pB nebulosity. F. S. IF, er.
305 307	-	- 88 Virginis	f	Q 3	52 58	n	9	24 43	1	F. vs. iF. r. F. cl. iF. bM.
<b>3</b> 08	,	-82 (m) Virg		12	28 31		Ö	1	1	Two. nearly mer.dift. 4'Sft. betw.
311 311	)	-99 (1) Virg	P	68	34		ı	18		che, touch. If, F. S.
312 313	-	06 (3b) Crate -45 (Ψ) Hyd	11	•	41 53	n	2 I	Q	1	F. L. iR. vgbM. pB. lE. par. b towards f. lide.
314 315	1	- 1 23 (2*) Ca	n f	17	57 29	ħ	I I	<b>55</b>		F. S. iF. bM. F. S. R. bM. C. N.
316	} 1	2 64 (1 b) Ger	1 .	4	16	1	I	17 56	I	Two. ip nf. dift. 1' che. mk. LBoth F. S. equal. N. F. pL. 1E. mbM. r.
318 319 320	-	– 22 (1 p) Ca – 48 (1 i) Can 3 23 Leonis mi	c p	8 9 12	38 10 38	1	0	5 50	I	F. S. bM. r. F. pS. R. lbM.
321 322		- 13 Can. ven	· P	51	31	t	0	50 28	I	pB. L. gbM.    The two first of g in a line.
323 324	] ]		P	40 38	19 3	n	0	17	1	f. S.
325 326	_		P	26 14	5Î	1	00		1	
327 <b>3</b> 28	-		f.	19	43 *43	ţ	0	35	1	F. pS. pB. ps. nearly R. mbM.

11.	1785	Stars.		М.	s.		D.	M.	ОЪ	Description.
329 312 333 333 333 333 333 333 333 333 333	Mar. 13 16  April 3 6	14(b) Comss	999 + 444444 99444 9444 99944 99944 9994 14994 1	48 45 60 60 78 94 19 19 19 19 19 19 19 19 19 19	545°0 4 06 28686 266 44442 2 2 9733286 486 08 2 342 4 2 2 4 2 2 2 973286 486 08 2 5 2 4 2 2 4 2 2 2 3 3 3 4 3 5 2 4 2 2 2 3 3 5 2 4 2 2 2 3 3 3 4 3 5 2 4 2 2 2 3 3 3 4 3 5 2 4 2 2 2 3 3 3 4 3 5 2 4 2 2 2 3 3 3 4 3 5 2 4 2 2 2 3 3 3 4 3 5 2 4 2 2 2 3 3 3 5 2 4 2 2 2 3 3 3 4 3 5 2 4 2 2 2 3 3 3 4 3 5 2 4 2 2 2 3 3 3 4 3 5 2 3 3 5 2 4 2 2 2 3 3 3 4 3 5 2 3 3 5 2 4 2 2 2 3 3 3 4 3 5 2 3 3 5 2 4 2 2 2 3 3 3 3 4 3 5 2 3 3 5 2 4 2 2 2 3 3 3 4 3 5 2 4 2 2 2 3 3 3 4 3 5 2 4 2 2 2 3 3 3 4 3 5 2 4 2 2 2 3 3 3 4 3 5 2 4 2 2 2 3 3 5 2 2 4 2 2 2 3 3 5 2 2 4 2 2 2 3 3 5 2 2 4 2 2 2 3 3 5 2 2 4 2 2 2 3 3 5 2 2 4 2 2 2 3 3 5 2 2 4 2 2 2 3 3 5 2 2 4 2 2 2 3 3 5 2 2 4 2 2 2 3 3 3 2 2 2 2 2 3 3 3 3 2 2 2 2	nifi i nnninnnnnniinninntninnnnnnniinn	0200 0 1000110011200010110011010100000000	5222 2 10890557618431172611285381991846449	3111 1 111212111121111211111111	pF. S. R. r. n. 2 pBit. pB. pL. R. bM. F. pS er. pB. cL. b towards p. fide.  Two. Nearly mer. Most n. pB. pS. bM. Most f. F. S. bM. pF. cL. iE. pB. vS. iR. pF. pS. bM. F. cL. iR. gvlbM. pF. pS. iF. F. vS. stellar. short ray p. fide. F. ftellar. F. pL. iE. just f. pBst. F. pL. iE. just f. pBst. F. pL. iF. pB. S. bM. r. F. S. pF. L. broadly E. pB. \$. pF. L. broadly E. pB. \$. pF. L. iF. pB. pL. pB. pS. nearly R. bM. F. pL. pB. pS. nearly R. bM. F. pL. pB. pL. F. S. pF. pL. lE. b towards ff. side. F. wS. pF. bM. F. pL. F. s. pF. pL. lE. b towards f. side.

II.	178,5	Stars.	1	M.	s.	۱	D.	М.	Ob.	Description.
<del>7</del> 37 <sup>2</sup>	Apr. 11	14 (i) Comæ	P	74	24	n	I	55	1	One of 4. The most n. of the p. side of a quartile. F. S.
373	-		р	13	28	n		16	1	F. L. bM.
37+	-		p	12	22	n	I	12	1	F.S.
37.5			P	11		n	I	14	I	F. pS.
376			P	6	38	n,	0	22	I	pF. S. almost R. bM.
377			Р	6	30	n	1	57	I	About 6' ff I. 90. pB. S. the place is that of the np.
					10	n	1	67	ı	F. cL. IE.
37 <sup>8</sup>		1	P	4	36	n	I	57 18	•	F. S.
379 380		- (a) Comm	þ		38	ſ	I	22	ī	F. pL.
300		15 (c) Comæ		9	46		0	20		F. S.
38 I 38 2		31 Comæ	P	3	16		0	9	ī	F. pS.
302			f	4	26	i	0		1	F. pL.
303			f	5	2			23		F. pL.
383 384 385 386			f	5	40	•	0	-3 4		F. pL.
305			f	5	54	ſ	0		1	<b>■</b>
300			f	5	48		0		1	F. pL.
387 388	1			1		1	1			Two. The time taken between
389	(1) -	41 Comæ	P	7	46	η,	10		1	them.
399			P	7	10	ſ	0	43	1	F.
39	-		P	7	18	n		23		F.
39	2		1	'						Three. The 2 f. p near each
393	3		P	5	46	n	0	14	I	
39	ر ا	1					Ì			The time is that of the 2.
39.			P	3	26		0	33	I	F. S.
39			P	2	16		1	29	I	F. S.
39	7 -		P	2	2	١.	0	4	I	F. S.
39	8 -		P	I	30	n	0	8		F. S.
39	91 -	- 3 (β) Coron	f	6	54	ſ	0	27		
40	I) I	3 26 Bootis	f	47	12	ſ	I	33		
40	I I	4 11 Serpentis	P	2	14	1	I	35		
40	2.1	-112 Ophiuch	i p	1 14	32	n	10	4	11	F. cL. E. sp nf. r. 3' l 2' b.

Third class. Very faint nebulæ.

ш.	1783	Stars.		M.	s.		D	м.	Оь.	Description.
1 2 3	Dec. 21	36 (v) Orion 60 Ceti 95 (o) Lepnis	f	3 13 4	39 :: 15	n	I	57 36	2 1 2	vF. S. mE. In the L. neb. eF. vS. R. lbM. vF. vS. lE. r.
4 5 6		6 (b) Leonis. 47 (e) Leonis 59 (e) Virgin	f	6 10 28	4	n	00	9	3 1	eF. vS. iE. ip. a triangle of Bit. eF. eS. viewed also with 240. vS.

III.	1784	Stars.		M.	s.		D.	м.	ОЪ	Description.
7 8	Jan. 23	3 (β) Can. mi 3 Leonis	f f	36 1	30 6			19 28		Stellar. 240 left some doubt. E. er. 3 of the sl. visible.
9	] _	32 (2 d) Virg	f	46	54	ſ	0	25	2	Two. Both vF. and vS.
10 11 12 13	, -	31 Bootis — — 11 (s) Virg	p p f	38 21 27	15 15 30		0 0	1 34	II	vF. stellar. vF. forming an arch with 3 st. eF. not verified.
14		31 Bootis	р		30	ſ	0	9	1	eF. vL. not verified.
15 16		68 (3) Lecnis	f	7	30	ſ	0	24	1	Two. The p. vf. L. 5 or 6' dia. The f ef. S. Fig. 5.
17 18	23	16 (c) Virgin 	f f	11	o 45	n	0	47 38	I	vF. pS. r. vF. cL. r. ∫ 2vS and close st. with nebulo-
19	Mar. II	2 (1) Can. mi	f	5	16	n	0	28	1	fity left doubtful.
20 21 22 23 24 25 26 27 28 29 30 31 32 33		53 (1) Leonis 73 (n) Leonis 53 (1) Leonis 73 (n) Leonis 20 Leonis 20 Comæ 86 Leonis 11 Comæ 8 (n) Bootis 5 (r) Herculis 5 (ξ) Leonis	£ P£ P£££ P£££££	1 15 14 9 11 26 4 13 2 7 10 3 16 3 13	45 30 6 30 30 30 30 30 30 30 30	ffnfnnfffiiinf	01001000100010	26 11 31 56 19 37 22 10 34 40 56 30	1 2 1 2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	vF. r. vF. S. C. ver. 240. vF. vS. with 240 cL. vF. vS. lE. ver. 240. vS. 240 left fome doubt. vF. S. eF. L. left doubtful. The most f. of 3.vF.vS.II.50.51. vF. L. r. vF. eS. stellar. ver. 240. vF. pS. f. 2 vBst. eF. forms a triangle with 2 Sst. vS. or nebulous double st.ver.240.
36 36	} -	78 (1) Leonis	ł	20	•	ł	0	15	1	Both eF. vS.
37 38 39	3 -	- 12 (t) Virgin 	P f f	11 12	15 15 45	n n	00	_	I	vF, near fome Bit.
40	-	30 (g) Virg	P	11	15	n	0	31	I	,
4: 4:			P		45 *15	n	1	23		vF.
4:	71	- 34 Virginis	P	6	6	1	00	4		1 "
4:	3 -	Vincinia.	P	3		1	1	_	1	Two. mistaken for one; but 240
4	5 [	71 Virginis 32 Bootis	P	25	<i>u</i> ,	1	1	12 47	1	hewed them both. cL. vF. vF. r. 2 or 3 ftin it.
4	8  -	962(10) Can	f	3	33	n f	0	27		eF.

III.	1784	Stars.	M.	s.	D.	M.	Ъ	Description,
50	Mar. 19 4	.5 (1A) Can	3	15	0	4		eF. ver. 240. and cL. R.  Two, np. ff. 6 or 7' dift. Both
51 52	2	27 (v) Leonis	7		0	2 I		eF. p is the largest.
53	15	34 Leonis	1		0	<b>4</b> I		eF. S. lE. r. 3 or 4 ft in it.
54		52 (K) Leon	10	45		27		eF. cL. R. r. no N.
55		46 (i) Leoni:		18	0	3		vF. vS. iR. r. fome st. in it.
56		15 Bootis	13	0		40		eF. vS. E. r.
57			10	30		28		eF. S. ver 240.
58			8	30		43		eF. S. ver 240 and lE.
59	ı	(N) (C)		15		10		eF. S. ver 240.
60	21	47 (8) Cancri	20	0		23 18		vF. S. with 240 near Sit.
61 <b>6</b> 2			26	30	J	10		eF. 240 shewed 5 Sst with nebulof.  Two. nearly mer. Both vF. pS.
			31	30	0	50		R lbM. r. with 240 cL.
63 64	1		36	o n	0	52		eF. 240 shewed some Sst with neb.
65	1	51 (m) Leon	3° 28	15		33		vS. E. r. better with 240
66	ļ.	31 (111) 2000	9	15		<i>4</i> 4		vF. S. E. r. the fame with 240
67			-	45		45		vF. nebul. betw. 2 ft. 2'l. ver. 240
68		3 Comæ		45		40		2 vSft with fusp. neb. 240 doubtf.
69		25 Comæ	5	ō	0	18		vF. S.
70		27 Coinæ	6	0	0	42		vF. not S.
71		42 Comæ	19	30	0	41		3 Sst with suspect. nebul. 240.
72	-	4 (7) Bootis	10	15	I	26		eF.vS. ver 240 and cL.
73		5 (r) Herc	4	0		50		eF. vS. eafily ver. 240.
74		48 Serpentis	1	15	0	5		vF. S. ver. 240
75	Apr. 8	70 (0) Leonis	12	24	1	7		eF. not S.
76	. —		4	0		41		eF. pL. eafily ver. 240.
72	oi .	04 (8) Leonis		12		12		eF. pL. R. r.
79		6 Comæ		18	0	19	_	vF. r. by moon-light.
79 80	12	73 (n) Leonis	.5	26		25	1	eF. not L. IE. r. vF. vS. R. bM. stellar. ver. 240
83				36	0	٠, ١	2	vF. vS. R. flellar.
82	E .	41 Virginis		35 42	•	7		▼F. S. E. r.
83		41 V M 5 M.		18	lo			vF. S. iF. r.
84		70 Virginis	3		-			eF. vS. stellar. ver. 240.
85	1	,	6	12				Three. The two p. vF. S. R.
85 86	15	_{ <sup>†</sup>	,					The last vF. pL. R. Place
87	)	l	6	48				of the 2d not taken.
	13	56 Leonis	5	42		23	1	eF. no time to ver.
	Ĭ	63 (x) Leon	6	24		29	I	eF. a little doubtful.
		3 (v) Virginis	4	54	0	1		vF. vS. vlbM.
91		11 (s) Virg				19		The f. of 2. ef. II. 17.

ın.	1784	<b>-</b>	Star	rs.		M.	s.		D.	м.	ΟЪ.	Description.
92 93	Apri	113	9 (0) Vi	rginıs	f	16	15	ſ	2	4	2,	Two. One vF. vS. The other just by. eF. eS. left doubtful. Three. All. eF. vS. R. In the
94 95 06	}		-	-	f	18	22	ſ	I	46	2	2d observation two of them were overlooked.
96 97 98		_	31 (1 d) —	Virg -	P P	17 3	61	n	0 0	42 0	2 I	The smallest of 2. eF. II. 144. eF. eS. The place not accurate.
<b>9</b> 9		_	32 (2 <i>1</i> ) —	Virg -	f f	47	36 42	1	0 [	33 8		eF. S. eF. E.
101 102		 15	- 2 (1 <b>ξ)</b> \	- Virgin	f P		0 48	n	Ι	23 54	1	eF. pL. R. er. The st almost visible eF. pL.
103			- 4 (2ξ) \			2	12	n	0	19	I I 2	vF. r. vF. vS. left doubtful. Twilight. eF. vL. lbM.
105			31 (1 <i>d</i> ) 33 V11 48 Leon	ginis	P f	7 6	5 <sup>2</sup> 3 <sup>0</sup> 54	n n f	1	35 8 8	I	vF. pL. vlbM. r. eF. pL. a little doubtful. Twil.
107		_	63%))I	eonis		13	18	n	1	7	I	1 ".
110			90 Leoi 20 Boo	tis	f	5	54	ſ	2	49 29	I	vF. vS. lE. ver. 240.
111		18	$\begin{cases} 58(d) \\ 84(\tau) \end{cases}$	,	• •	8	36	n f	I	43	1	vF. vS. r. ver. 240. eF. cL. R. r. mear vBst. b light.
112			74 (φ) Í —	-	f f	10 34	18	ſ	I	5 <sup>2</sup>	I	eF. eS. with 240. 2vSft and nebu.  2 vSft with nebulofity with 240
114 115			28 Virg 67 (æ)		P f		18	_	I	35 10	1	left doubtful. vS. vF. stellar. ver. 240.
116	_		31 (f) I	_ibræ			48			15	Ι	vF. cL. nearly R. lm. The two most f. of 3. That M.
117	Ì	11	100 ()	Virg		59				48	I	vF. vS. The most s. eF. eS. ver. 240. II. 193. eF. vS. stellar. ver. 240.
119	f		_	_	p f	55	42 24	n	0	29 9	I	1 1 1 1
121 122		14	9 (α) I	libræ	p	27	0	ſ	0	<b>3</b> 6	1	nearly R. The p. vF. vS. R. dift. 5'.
123 124		_	18 Her	_	f	43	30 30	ſ	0	47 47	1	vF. pL. R. lbM. vF. stellar. ver. 240.
125	l	16	25 (ρ) I -	300tis	P P	-	12	1	1	10 24		vF. S. iR. lbM. almost stellar.  [ 2 Sst. with suspected nebul. almost ver. 240.
127		-	28 (0)	Bootis	f	3	48	n	0	45	1	Two. 3' dift. par. The f. vF. vS. iR. The p. eF. vS. ver. 240.
***	1				1	l						

ın.	1784	Stars.	1	M.	s		D.	м.	Ob.	Description.
129		28 (o) Bootis	£	17	48	n	0	3	1	Two. about 6' dist. Both eF. vS. R. ver. 240.
131			f		54		0	II		vF. E. close to a st. contains 2 st.
1 32	17	36 (1) Bootis						26		eF. S. IF. the fame with 240.
133		Postis	P	2	36 28		0	35 12		cF. cL. iR. lbM. vF. pL. E. par. r.
134		12 (d) Bootis	f	4 12	30		I	5	ī	eF. vS. stellar. ver. 240.
135 136	]		f	14	8	١.	0	30	2	vr. S. E. nearly par. with 240 like two stel.
137		76 (a) Hercu	ח	2	54	n	0	22	I	vF. not S. iE.
138	11					t	1		į	Two. nearly par. 7' dift. Both
139		10 (19) Libi	Τ	13	36	Γ_	I	9	3	VF. not vS. R.
140	June 11	27 (β) Hercu		23	30		0	51	1	vF. vS. r. ver. 240 np. pBft.
141		16 (↓) Capri		6	42		lo	33		vF. cL. lF. lbM. 240. fame. vF. E. about 2'l.
142		70 Aquilæ	P	3	39	n f	6	31 3		3 vSft with suspected nebulosity.
143 144	Sept. 5	35 (2v) Sagit 39 (b) Cygni	P P	21		ı	1	20		Some eSft. with neb. iE. ver. 240.
145		10 (x) Pegasi	P	25	48		0	53		vF. lE. stellar.
140	1	11-70 -6	f	11	24	n	I	53	I	vF. E. fome Sit. with nebulofity.
147	-	35 Pegafi	f	7	54		I	13		2 or 3 ft. with feeming nebulofity.
148	1	28 Androm	P	4			0			vF. pL. lbM.
149		31 (8) Andr	f	18 18	24	1	0	15	,	eF. vS. R. Near V. 18. vF. SR. bM.
75°	1	2 (a) Trang	P	1	40		ī	,4 ,18	2	vF. vS. stellar. betw. vL. and Sst.
15: 15:	,	39 Arietis	P P	8	12	•	1	49		vF. pS. of equal light.
153		to Andr	P	13				29		vF. pL. lE. vlb. towards f fide.
154	1	1'	f		+ Q	n		20	1	Two. Both eF. vS.
155		1	1	9	10	"	ľ		1	The f is the largest.
156		(0) 2 - 1-			,	1		8		Three forming a rect. triangle.
157	11	43 (β) Andr	I	13	Ð	ſ	2	0	2	In the legs eF. vS. at the rectangle vF. pL.
158 159	1 .				_	1			1	Two. Both eF. S. but une-
160		to Androm	f	20	6	n	I	30	I	[ qual.
161 162	-	17 (r) Perses	P		30		1	• •		vF. S. iE. r.
163		21 Perfei	P	13	42 18	n	0	30 32	I	Two. Both vF. pS. R. lbM.
164			f	15	36	ſ	I	19	1	eF. vs. 240 left a doubt.
	<b>)</b>	66 (v) Cygni				1		-		[ 5 or 6 st. forming a parallelogr.
165	ł -	on (a) Chân		43	0	1	0	4		with mixed nebul. ver. 240.
166	1 4		f	78	18	ľ	0	47	I	eF.v8.E.nf.&4or 5'dist.from1.53.
167 168		43 (β) Andr	f	15	30	ſ	2	12		Two. Both stellar.
169			f		12			46		stellar.
170	· –	- m	f	16	30	1	I	31	1	ftellar,

III.	1784	Stars.	<b>M.</b> S	D.M.	Description.
171	Sept, 13 43	(β) Andr	17 30	0 56	stellar. J Two. Both vS. stellar. a little
172			18		doubtful.
173 174	3 (	(a) Triang	25 24	0 22	stellar. ver. 240.
175			12 4	2 29	stellar. eF. stellar. 240 left some doubt.
176	'o (	γ) Triang	9 36	0 1	vF. cL. iR. r. 2 or 3' d.
177	17	(γ) Persei	9 3	O I	vF. pL. R. SB place M.
179	1 <sub>6</sub> (	(β) Arietis	5 O	•	vF. pL. lE. eF. vS. R. n. cLft.
180		Pegafi Pegafi	3 0 6 48		vF. vS. R. ver. 240.
181 182		Pegasi	38 2.	0 51	4 or 5 Sft. with nebul. 240 doubt.
183	89	(x) Pegaf	0	38	eF. S. iE.
184	20 11	Piicium	17 44 12 50		eF. vS. stellar. ver. 240. vF. E. er. 3 Fst. visible in it.
185 186	20	Piscium	29 15		eF. vS.
187			14 39		eF. stellar, ver. 240 and cL.
188			13 33 8 15	O 6	eF. stellar. just like 187. eF.
189	20	Piscium	4 54		vF. vS.
191		. Ceti	9 12	I 53	vF. mE.
192	72	Ceti	17 24		eF. S. ver. 240. with difficulty eF. ver. 240. with difficulty.
193	81	Ceti	38 6		
194	٠.	-	42 42		eF. eS. ver. 240.
196	] _		47	0 36	Two. Both eF. ver. 240 but just suspected with 157.
197	Oct. 612	(a) Perfe		0 40	cB. mE. vgmbM. near 4' l.
198	7 27	(x) Persei	8 27	•	The f of 2, vF. iF. pS. II. 239
200	14 53	Piscium	4 24	•	2 Sst with nebulosity ver, 240. vF. vS. E. s. pcst.
201	19	Arietis Pıfcium	83 54		eF. vS. stellar. ver. 240.
202	154)		78 18		vF. cL. E. 2'l.
204	59	Pifcium	0 4		vF. S. sp. 2 vSst. eF. ver. 240, discovered in gaging.
205	92	Pifcium	5 30		eF. S.
206	3	( ) Arietis	3 3° 5 13	1	eF. v5. stellar. plainly. ver. 240.
207 208			6 30		eF. vs. iR. just f. pBst.
209	16	7 Delphini	18 (	_	vF. S. R. Two. The p. vF. S. lE.
210	12	4 (a) Pegafi		9 46	The f. vF. vS. stellar.
211			21	5 59	(eF. eS. ver. 240. completely
212			27 3		though with difficulty. eF. cL. ver. 240. betw. 2 Bst.
213			4/ 3	A - 40	III.

m.	1784	Stars.		м.	8.		D.	м.	ОЪ	Description.
214	O&. 16	31 Arietis	P	36				24	I	vF. stellar. ver. 240. eF. stellar. discovered by 240.
215			P	36		n	0	6	I	Two. The p. vF. pS. R. vlbM.
216	] 18	46 (£) Pegasi	f	3	15 25	1	0	37 32	3	The f. vF. pS. R. vlbM.
217	ا	58 (n) Pegasi	f		51	'n	0	4	1	eF. pS. IE.
218	10	15 Delphini	P	5	24		0	2	1	eF. vS. stellar ver. 240. with dif.
219	-	66 Pegafi	P	10	10	n	0	23	4	F. R. bM. 1 ½ d.
221			P	7	10	1	1	0	2	vF. S.
222			P	7	7		0	54	2	vF. S. R. vF. 1E. or oval. 1' d. np. 2 pBft.
223		7 (b) Ceti	f	23	42	f	1 2	I	1 2	vF. S. iR.
224		I (I 7) Erid	P f	12			ł	49	I	eF. E. r. near 1' l. ver. 240.
225	, u I	15 (8) Lepor 70 (q) Pegasi			50			18	1	vF. vS. stellar ver. 240.
226	Nov. 7	64 Ceti	P	2,	24	ı	0		I	2 or 3 Sft. with neb. nearly ver. 240
227	_	1								Two about 1' dist. The p. eF.
228	>	73 (28) Ceti	f	12	54	h n	0	17	I	
229	ر		1	1		٦.			_	240. doubtf.
230	1:	2 55 (l) Pegasi	P	3	36	ı	P	29	I	eF. eS. 240 left fome doubt.
231		- 31 (1 c) Pifc	P	9	C	ſ	I	0	I	Two. Both vF. stellar.
232	[ ]		P	8	27	ſſ	I	0	2	eF. pL. glbM.
233		6 43 (γ) Canc			24		I	6		l
234 235	f		P	3		n	2	4	. 1	eF. S. ver. 240.
236	-	- 4 (λ) Leonis	P	23	22		1	· •		
237		733 Pegafi	f	12		• 1	0	•		
238	-	- 66 Pegasi	P	6		5 n	1 -		1	
239	al -	- 4 Eridani	P	32		1 5 f	I	I	1	
240		O12 Leporis	P	7	55	١,	1 -	-		1
24	1	- 15 (1) Nav	f	68	39	5 n	0	-	1	l
242	_	256 Pegasi	P	9		6 n	0			
243 244	1	948 Ceti	P		3,	4 n	0	27	I	eF. vS. E.
24.5	-	_ 15 Eridani	P	15	- 40	ol f	0			vF. cL. iE. r. unequally B.
246	7 l	- 19 Eridani	P	1	3	8 5	0			
247	7 -		f	6	٠.	5 f	1-			1
248	- 1	- 27 Eridani	P	4	. 2	3 n				
249			P	2		<b>7</b> 1	- 1			Two nearly par, a or of diff.
250 25	[]} I	3 89 (f) Pisci	f	1.		5 1	1.	• • •	1 -	Both vF. vS. R.
25			f	3	4	2 p	I		1	
25	ર્ચ -	_	f	6	4	8 1	o	11	ĮĮ	eF. cL. E.
254	1 -	_ 15 Sextantis			1 3	4 0	I			vF. E. np ff. 5' 1. \ \ b.
25	· -	- 7 Sextantis	f	20	2	7 7	10	42	1 5	vF. vS. p. triangle of Bit.
25	<b>)</b> 2	ol13(ζ) Can.n	ni f	26	•	51 1	. (0	4	5  I	vF. vS. ver. 240.

III.	1784	Stars.		м.	s		D.	м.	ОЪ.	Description.
257	Dec. 20	13 (ζ)Can.mi	f	44	59	ſ	0	55	I	eF. pL. iF.
258	-	- 10 (7) Virgin	p	5	2	ſ	0	7	2,	vF. S. E.
242	1785			7.0	24	ſ	0	38	1	eF. eS. iF.
259 260	Jan.	70 Ceti	P	7	34		0	3° ⊿	ī	eF. vS. stellar.
261		75 Ceti	P P	3	46	ſ	0	<del>4</del> 6	I	vF. cL.
262	process.	-94 Ceti	p	I	16	ſ	I	15	I	eF. ver. 240. with difficulty.
263		24 Eridani	P	3	22		0	11	I	eF. stellar. or lE. almost ver. 240.
264	-	-28 (A) Hydr	P f		48	n		19	2	vF. vS. R. ver. 240.
265	10	45 (θ) Ceti		32	28		)	46	I	eF. stellar. ver. 240.
266			f	3 <b>r</b>	6	۱.	0	43	I	vF. lE, ver. 240. vF. pS. iE. bM.
267		4 14 (ζ) Lepor		0	I	1 .	0	31	1	eF. vS. stellar, ver. 240. easily.
268 269		6 11 (a) Lepor - 19 Leporis		27 32		n	1	2,	1	1
270		- I G Lepons	P	20		n	1	28	1	vF. eS. stellar. ver 240 difficulty.
271		-8 (3 ») Can'		8		n	0	4	1	3 or 4 Sst with neb. vF. ver. 240.
272		76(3b) Crates	1	58	39	n	I	21	I	vF. pS. iF. vlbM.
273	_	1 '- ' -	P	55	43	n	0	39	I	eF. vS. iF.
274	_	-31 Crateris	P	4	40	ſ	ł	14		vF. pL. iF.
275		8 12 Hydræ	f		30	1	I	٠,		vF. vS. bM. ½' f. Sft.
276		– 38 (x) Hyd	P	9	20	ſ	٦	26	I	vF. vS. stellar. 240. the same.    Two. 3 or 4' dist. The most n. vF.
277	} -	- 39 (1 v) Hyc	P	5	С	n	0	30	I	S. The f. vF. vS. Both stell.
278 279	\	-8 (n) Corvi	P	31	26	n	0	16	I	eF. pL. better with 157 than 240.
280			f	18	44	1	I	51	I	$\int \frac{1}{2}'$ p. II. 298. eF. eS. ftell. 240.
			1			1		_	i	vF. pS. r.
281		Trinainia	f	20	_		0	46 12	ī	I
282		-53 Virginis	1	27		n	o.	27	I	vF. vS.
283 284	Mar	741 (a) Bootis 525 (f) Virg	P	54	12	ſ	0	19	1	vF. S. iE. lbM.
285 285	14191	-88 Virginis	f	8		n	1	17	1	eF. vS.
286		-99 (1) Virg	P	9	22	n	0	31	I	vF. L. b towards n.
287			P	7	58	ſ	0	7	I	vF. pS. iF.
288		6 15 (1) Navis		II		ſ	I	7	1	
289	1	06 (3b) Crat		69		•	0	25		1
290	-	2 (f) Corvi	P	16		n T	2	3	1	
291	I	1 75 Cancri	P	2	53 46		I	13	1 _	
292		246 Cancri -23 Leonis	P	177	46	s r		22	1	
293 294		357 (21) Can		2	44	n	0	15	1	
295	•	72 (7) Canc	f	5	47	7   1	0	24	I	vF. vS. R. nf. 2pBft.
296			f	8	4	n  S	I	17		
297	-	-15 (f) Lea	p	13		3 5	0		·	
298	ii -	_18Leonis mi	al P	1 20	56	) I	10	44	. 2	vF. vS. iR. lbM.

III.	1	785			Star	s.		M.	s.		D.	м.	Ob.	Description.
299 300	1	Mar.	13	13 (	Can.	ven.	P	40 40	19	1	I	27 28	1	eF. The most f of 3. vF. II. 322.323
301 302		•		-	,	-	P P	28 27	40	ſ	I	41 2		vF. vS R. eF. vS.
303			_	-		-	f	5	43 26	ſ		43		eF. vS. ver. 240. eF. vS. ver. 240.
304 305		•	_		,	-	f	11		ſ	I	47 9		vF. vS. lE.
306	}		_	_	,	_	£	16	12	n	0	6		Two. The p. vF. vS. The f. 7 or 8' nf the first. vF. vS.
<b>3</b> 07 <b>3</b> 08	j		_	-	,	-	f	17	29		0	13		vF. S.
309		•	-	-	, (A) D		f	18	31	n	0	34	I	eF.vS. vF.vS. iF.
310		•	76	49 (	(ð) B (Trío	ootis min	b	43	12	1	I	32 18	I	
311 312			10	11		. 111111	Þ	24 19		n	2	6	ī	1 - 0 - 20 :
313				13 (	(γ) <b>L</b>	Jr. mi	f	27	9 8	n	1	12	١	1
314		,		J		-	f	49	_		0		1	
315		Apr.	3	27	Urfa	<b>.</b>	f	3	42	п	0	•		•
316				-	•	***	f	51	42		I	43		
317				-	•	-	f f	65		n		19		vF. vS.
318		•		- '-	• ON TT			69				20 26		vF. pL. r. eF. not verified.
319		•	6	7 (	Leon	rf. mi	P	32 26				44		vF. vS. stellar.
320				12	oma	e :119	P	22		1	0	15		
321 322				7 -	-	<u>_</u>	P	19	37	n				vF stellar.
323	η						1	14	43		0	40	ı	Two. The sp. vf. lE. The nf.
3 <sup>2</sup> 3	}	•		-	•	-	P	• •	• •	1	١.	• •		l_eF. 5 or 6' dift.
325				-	•	-	P	13	46	1	P	45	I	eF, vS.
326				-	<b>-</b> 1	-	P	5	47	ſ	0	17	I	saging.
327			-	- ∤	-	-	P	I	45	n	0	33	I	vF. pS.
328			-	31	Con	ıæ	P	6				25		F. S.
329				21	(g) (	Comæ	E		45		1	26		vF. S.
330			10	30	(ς) <sup>1</sup>	eonis	1	4	54 16		0	29 <b>3</b> 6		vF. pS. vlbM. iR. vF. vb. vlbM.
331			_		Leon	nis mi	f	12	46	1	ô	34	Î	1 1
332				72	Leon	nis ,	f	2	48	'n	0			l
333 334				/		-	f	3	17		ı	23		vF.S.
	F						f		-	ĺ	}			Two. 2 or 3' distant. Both vF.
335 336	}			1 -	-	-	1	7		n		12		VS. the most s. faintest.
337				-	-		f	9	34	n		52		vF. S.
338				-	•		f f	25	56	1	0	38	I	
339				-	-		l	26		,	•	44		
340			-	-	•	-	f	28	36	f	0	19	1	vF. vS. pL. two stellar, sus-

III.	1785	Stars.	L	M.	s.		D	.М.	ОЪ	Description.
341	Apr. 10	7 (b) Connæ	p	26	41	n	0	56	1	vF. vS. ver. 240. cafily.
342			p	22	<b>5</b> 5	ſ	0		1	vF. vS. IE.
343			Р	20	7	ſ	0			vF. vS. 240. the fame.
344	1		_	18	31	1	٦	40	,	Two. 5 of 6' diffant. Both cF.
345	}		P	10		1	l	43	1	VS. ver 240.
346		40 Comæ	f	1	38	n	2	8	1	eF. pL. 1E. ver. 210.
347		12 (d) Bootis		7	40		ĮĮ	17		vF. IE. S.
348	II	23 Leonis min	1	3	12	1	I	38	I	ef. IE. a little doubtful.
<b>3</b> 49	-	39Leonis min	1 1	9	28	n	1	18	I	eF. 240 thewed a few Sft. with neb. but doubtf.
350	*****	44Leonis min	f	17	36	n	0	35	1	vF. S.
351	] _		f	20	58	n	٥	51	1	Two. Both vF. vS. the most f.
352	]				3		ı			L is the faintest.
353			f	53	4	Ω	2	26		eF. 240 left it doubtful.
351		14 (b) Comæ		28	29	11	0	43	1	vF. vS. difcovered in gaging.
355			P	21	41	1	0	10	1	vF.S. pmE.
356 357	} -		P	17	40	n	ı	<b>5</b> 5	1	Two or 3, the place is that of II.  371. Both vf. mk. A 4th inspected.
358	)		- 1							Three of a quartile. The place
359			P	14	24	n	ſ	55	1	is that of II. 372. All vF.
300	,							1		( vs. and all within 3',
261			P	0	40	n	0	18	1	vF. vL.
302		15 (c) Comæ	f	3	2		1	3	1	eF. cL. 4 or 5' l. 2' b.
363		41 Comæ	P	b	16		0	~ 1	I	vľ.
304	_		P	•	24		0	25		vř.
365	-		t	1	5		0	41		vF.
366			f		26		I	18		vF. pS.
367		43 Comæ	f		24	ĭ	0	2	1	vF. pl.,
368			I	II	2		0	53	I	vF. mE. 1 I'l. r. discov. gaging.
369			اء		41			29		eF. vS. 240 lest a little doubt.
370			f	28	اه		0	31		vF. S. mH. nearly mer.
371		14 (1) Coron			~ ;		I	8	I	vF. S. R. ver. 240 eafily.
372	13	93 Leonis	P		25 18	n	0	25		vF.cl., moon-light,
373		II Libræ	f	I		1	0	12	I	vF. just n. Sst.
374		II Serpentis	P	12	28				1	eF. pL. r.
375		93 Leonis	P		4	11	0 0	7	2 2	vF. vS. r. eF. vS.
3761	2(1		p/	5	571	n	U	5	4	CT 4 VO

# Fourth class. Planetary nebulæ.

Stars with burs, with milky chevelure, with short rays, remarkable shapes, &c.

rv.	1782	Stars.	1	M.	s.	١	D.	м.	Оъ.	Description.
1	Sept. 7	13(1)Aquarii	p	5	24	n	0	2	11	vB. nearly R. planetary not well defined difk.
2	1783 Dec. 26	13 Monocer	f	6	4	n	ı	27	4	cB. fan-shaped. about 2' l. from the center. Fig. 7.
3	1784 Jan. 16	15 Monocer	p	8	18	n	0	15	4	pB. m. like a st. with an electri- cal brush. Fig 8.
4	Feb. 22	69 Leonis	f	10	3	ſ	I	3	2	eF. S. like an st. with a vF. brush sp. 240 shews the st.
5	_	29 (7) Virg	P	9	O	n	I	33	2	A pBst. with a m. ray s. par.
•	23	59 (c) Leonis	P	9	O	ſ	a	18	I	F. L. C. A central B. point with - eF. m. chev.
:	Mar. 14	51 (m) Leon	f	17	C	ſ	0	39	2	F. pL. m. between 2 Bst. like an electrical brush to the most n. but is not connected. R.
	15	34 Virginis	P	FO	12	ſ	0	51	2	A double Nebula. The che. run into each other. cloie. not vF.
I		51 (m) Leo	þ	21	15	ſ	I	48	I	A pcst. with a vF. brush nf. with 240.2 vSst. visible in it, but not connected.
1	1 May 21	5.1 (e) Ophiu	P	1	42	n	0	14	2	1
1	2 24	3 (p) Sagitt	f	22	c	n	x	47	I	I
1	3 July 17. {	39 (h) Cygni 21 Vulpecu	p	8 2	6	f n	I	35 51	2	f pF. exactly R. of equal light, the edges p. well def. 1'd. See note.
1.	21	27(d)Aquila		6	, 6	f	I	45	2	
5	Sept. 8	21 (a) Andr	f	2	$\epsilon$	1	l <sub>r</sub>	21	1	lama transit to the
16		16(n)Sagitta	f	17	12					1 - 4 - 11 1
R	20	81 Ceti	f	36	30	n	0	36	1	
	ķ	1,	1	l		}	ļ			240. IV.

ıv.	1784	Stars.		М.	s.		D.	M.	Ob.	Description.
18	O&. 6	14 Androm.	p	6	11	n	3	16	4	B. R. a planetary p. well defined disk. 15" dia with a 7 feet reflector.
19	16	5 Monoc.	P	7	6	ſ	٥	10	1	A st. of the 9 magnitude, with m. chev. i elliptical.
20	<b></b>		P	3	42	n	0	3	1	A st. of the 11 or 12 mag. affected like the foregoing, but vF.
21	Nov. 20	12 Leporis	P	8	48	n	0	24	1	vS. stellar. vBN. and vF. chev. not quite central.
22		7 (ξ) Navis	f	3	10	ſ	I	28	2	L. pB. R. er. 6 or 7' d. a faint red colour visible. A st. 8 mag- not far from the center, but not connected. 2d ob. 9 or 10' d.
23	1785 Jan. 6	75 Ceti	P	4	40	ſ	0	6	I	cB. a vBN. with a chev. of 3 or 4' d.
24 25	31	-50 (ζ) Orio 19 Navis	f P	6 <sub>7</sub>	57 0	f n	1	17	1	1 4 5 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
26	Feb. 1	34 (γ) Erid	f	16	16	Λ	0	49	2	vB. perfectly R. or vl. elliptical. planetary but ill defined disk. 2d obs. r. on the borders, and is probably a very compressed cluster of stars at an immense distance.
27	1	7 6 (3 b) Crater	P	28	39	n	I	25	2	
28	_	-31 Crateris	f	1	c	n	0	47	1	pB. L. opening with a branch, or two nebulæ very faintly joined. The f. is fmalleft.
29		84 (v) Crateris	f	3	36	n	0	16	1	

# Fifth class. Very large nebulæ.

v.	1783	Stars.		M,	s,		D	м.	Ob.	Description.
I				l			l		1	cB. mE. ip nf. mbM. Above 50'l. and 7 or 8'b. C. H. See note.
2	1784 Jan. 24	10 (r) Virgin	f	24	46	n	0	17	4	cB.mE.'np if. mbM. er. 9 or 10'l with a branch towards the np.

		1		1	ļ	TiT.	١٠٠	ľ	ν.	LV1.	~~	Description.
-	Tan C4		- I e	nie	ť	104			0	24	ī	eF. vL. er. R. 7 or 8' d.
3	Jan. 24	7	761 1	Virgin	f	7	15	1		45	2	vF. R. 5 or 6' d.
4	Feb. 23	1	τ Co	<b>U</b> 1	f		47			32	- 1	L. E. r. 6 or 7' l,
5	Mar. 14	1	/~1	Bootis			45			6		vL eF r.
	Apr. 8	14	(1)	Teonis	n	3				41	I	vL. F. r. almost R.
7	Apr. o	15	2 (22)	Leonis	F	3 4	34	n l	0	18	3	B E. almost par. but l. np ff.
o		1/	3 ("	LCOM	1	*	27	_			7	near 15' l.
-1	7 / a 0 c	1.	(+ (a)	Ophin	f	22.	48	1	0	40	ï	L. E. broad. m. F.
9	Iviay 22	45	1 (6)	Ophiu	- 1	3-	7			•		Three nebulæ, faintly joined, form
10	Tulm To	٦	(1)	Sagist	f	2	42	n	0	4C	1	a triangle In the middle is a
11	July 12	15	(4)	025	^		4-	_	ľ	17	1	double it.vF. and of great extent.
12	,			_ 1	f		54	ก	0	20	1	Extensive m neb. divided into 2
13		1			1	4	34	-		37	1	parts. the most n. above 15'.
							- 1		1		1	The most i followed by stars.
	Cont	٦,	-1 (1	) Cygni	f	7.1	24	n	Ь	44	2	1
14	sehr.	داد	3-10	<i>J</i> • <i>J</i> 5 ····			~~					in R.A. near 11 deg. and in
1		١							١,	,		P.D. 52'. The f. part divides
1		1		•		1		١				into feveral streams uniting
		1			1							again towards the f.
		_	_	_	f	10		n	lo	) C	3	
15		7	_		1	"	•	1			1	By the Newtonian view above
1		- (						1				1 degree I. By the Front-wiew
- 1		1				1			١			near 2 deg. l. Sec note.
16		, ,	as A	ndrom.	P	Tr	12	n	lc	17	ι (	1 2,-
17				) Triang			48					
-/			1 (	,	7		-4.			50		deg. broad. perhaps 3 degree
					1			1			1	long, but not determined.
18	0.0	-	25 6	Andr	P	1 6	) I I	n	lc	37	4	1 - 7 - 11 1 0 YT
19	1	3	26 (	) Andr 8) Perfe	ı P	45		n	E	16	3	1
•9	1	J	1-0	-,	1	1 70	,				١	division 3 or 4 l. M.
20		20	7 (1	) Ceti	f	33	3 9	ſ	h	48	3 1	
	1785		1' "	,	1	1 3.	, ,		1	•		26' 1 3 or 4' b pb.
21	lan.	21	180	μ)Canis	f	22	18	3 n	h	: 2	2 2	
	1	J-	``	, =				1	١			parallelogram with a ray fouth-
	1					1			1		1	wards; the parall 8'l. 6' b. vF.
22	Feb.	7	6r 7	/irginis	f	10	59	n	ŀ	1	7   3	
23		2	27 [	Jríæ	f	1:	3 18	3 n	l			1 m 1m / 11 / 11
-3 24		6	21 (	g) Com		1 4	20	n Jo	1			
44	1		1	J,		1		-	1	•		4' b. np ff. vBM. a beautiful
	1		1		L	1		1	1		1	appearance.
			-									

Sixth class. Very compressed and rich clusters of stars.

Additional Cl. Cluster. abbreviations fc. Cattered.

com. compressed.

VI.	1783	Stars.		M.	s.		D.	M.	Oh.	Description.
1	Ncv 19	63 (p) Gemi	f	II	0	n	0	12	3	A beautiful Cl. of many L. and com. S. ft. about 12' d.
2		18 (1) Gemi	ť	27	10	ſ	2	9	3	A v. com. Cl. of eSil. if. 5 or or 6' d.
3	1784 Jan. 24	12 Monocer 4 Seat untis	í	1 I 5	30 30	ſ	0 0	18 5	1	A Cl. of v. com. and co. fl. E. A. Cl. of v. com. S. fl
4 5 6	Feb. 11	31 (28) Gem	P	31	0	1		15 57	1	A Cl. of v. com. S. 7 or 8'd. A Cl. of st. of various sizes
4		07 Gemin	P f	_	30			8		pm. com. M. p. rich. An eF. Cl. of eS. ft, with r neb. 8
7		42 Comæ			_		0	6	١	or 10 d.ver. 240. beyond doubt. A v. com. Cl. of ft. 8 or 9' d.
8		26 (x) Virg		23	1					e rich. iR. or IE.
ç	May 17	11 Bootis	f	4	18	n	I	7	I	A Cl. of eS. and com. st. 6 or 7' d. many of the st. visible, the rest
10	2.2	21 (æ) Scorp'	р	1	48	n	0	24	ı	fo S. as to appear nebulous.  A v. com. and cl. Cl. of the
										finallest stars imaginable, all of a dusky rod colour, the next
11	-	39 Ophiuchi	P	13	24	f	0	26	1	frep to an cr. neb.  A fine miniature of the 19 ne- bula of the Connoift des
										Temps (which is a Cl. of v.
										om. ft. much accumulated M. 4 or 5' d. all the ft red.)
12	2,4	43 Ophiuchi	P	12	42	n	1	36	1	2 or 2' I d, the fl. F. red. Another miniature Cl. like the preceding, but rather coarier.
13	June 22	10 (y)'Sagirt	p	14	48	n	ŀ	18	1	A Cl. of S. and p. com that feweral mag. 501 0'd not v. 11ch.
14	July 1	y Vulpec	P	4	0	n	0	33	1	
15	July 1:	2 34 (o) Sagitt	p	6	54	n	0	2.7	τ	1
16		8 12(y) Sagitta	P	4	18	1	I	32	1	A vs. Cl of com. ft.
17	Nov. 1	(1w) Gem	P	54	53	1	ľ	29	2	A v. tich ('l. of v. com. and ess. 4 or 5' d. A ministure of the 35
_	1785						-	م.		Ch of the Coun. de 'I', which it precedes 1' 18" and is 2' n.
18	ł	4 11 Monocer	1	1	15	1	į.		1	iF. 8 or 9' d.
19	1	0 24 (1ft)Libi	f	5	C	ſ	I	16	I	nute and most com. st. of dif-
	•			ļ		}	-			ferent fizes, 6 or 7' d. iR. F. red colour.

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Seventh class. Pretty much compressed clusters of large or small stars.

V11.	1784	Stars.		м.	S.		D.	м.	ΟЪ,	Description.
1	Jan. 18	90 (1 c) Tauii	f	11	0	ſ	I	30	2	A Cl. of L. fcat. st. 10 or 12' in
á	24	8 Monocer	f	8	17	n	0	23	3	extent, with a vacancy M.  A beautiful Cl. of fc. st. chiefly of 2 forts. the first L. the se- cond arranged in winding lines.
	Est 0	a Tamonia			20	ſ		20	Ţ	contains the 12th Monoc.
3	reb. o	3 Leporis 15 (2 y) Orio	P f	72 3	30	n		30		A S. Cl. of com. st. some pL. A Cl. of pL. and p. com. st. c.
1										rich. 20 or 25' d. iR.
5	23	13 Monocer	P	3	15	ſ	0	28	I	A Cl. of com. it. of various mag.
6	Mar. 16	50 Gemino	f	2	55	ſ	2	۵	I	p. rich in Sft. not R. A p. rich and com. Cl. of ft.
7		3 (p) Sagitt'	f	15	54	ſ	0	8	1	A c. rich, but p. co. sc. Cl. of st.
8	F1	(1) (2	c					_		l. more com. M.
٩	July 17	41 (i) Cygni	I	5	42	•	2	1	5	A v. rich Cl. of pS. sc. st. most of the same size. 20' d.
9	19	12 Velpecu	P	0	5	n	0	30	2	A L. Cl. of p. com. st. most of
7.0	NT	m /El Morrie	f	_	-6	_				one fize.
10	1785	7 (ξ) Navis	1	5	50	**	10	40	3	A vL. Cl. of fc. st. c. rich and com. more than 15' d.
11		19 Navis	P	0	40	n	0	5	1	A c. 1ich Cl. of co. sc. st. above
	T. I	6 27				_				20' d.
12	red. 4	6 Navis	P	31	59	11	I	25	4	A beautiful Cl. of p. com. st. near ½ deg. d. C. H.
13	6	2 (β) Canis	p	7	10	ſ	0	44	1	A Cl. of fc. Sft. not v. rich above
_	0	-0 ( ) (	e				l			15' d.
14		18 (µ) Canis 26 Canis	t	3	17	n	0	20	I	A Cl. of co. fc. ft. 20' d.
15	Mai. O	20 Cams	f	I	56	n	1	52 16	I	A S. Cl. of p. com. ft. not v. rich.
17			f		26			10		A Cl. of fc. st. c. rich. 20'd.
-1					~		-			A v. beautiful Cl. of pL. st. v. rich. contains the 30 Canis.
,										3- 3-

Eighth class. Coarsely scattered clusters of stars.

VIII.	1783	Stars.	M. s.	D.M.	Description.
	Dec.	14 Navis	4 0	0 40	A Cl. of co. fc. ft. The place is that of the most com. part
		58 (a) Orion 13 Monocer	8 28 1 30	1 16 1 2	which is not M. A S. Cl. of vS. fc. ft. An E. Cl. of L. fc. ft.

VIII.

Jan. 16	VIII	1784	Stars.		М	. S.		D	.M	Ob	Description.
than 30 cLft.  than 30 cLft.  A Cl. of co. fc. ft. not rich.  A Cl. of vv. co. fc. ft. not rich.  A Cl. of vv. co. fc. ft. not rich.  A Cl. of vv. co. fc. ft. not rich.  A Cl. of vv. co. fc. ft. not rich.  A Cl. of vv. co. fc. ft. not rich.  A Cl. of vv. co. fc. ft. not rich.  A Cl. of vv. co. fc. ft. not rich.  A Cl. of vv. co. fc. ft. not rich.  A Cl. of vv. co. fc. ft. not rich.  A Cl. of vv. co. fc. ft. not rich.  A Cl. of vv. co. fc. ft. not rich.  A Cl. of vv. co. fc. ft.  A Cl.						-	1	1		3	A Cl. of co. and i. fc. pl.ft.  Double and attended by
Feb. 10 4 Orioms										١.	than 30 cLit.
19   19   24 (γ) Gem   P   8   15   n   0   15   15   15   15   16   16   16   16						20	n	1		1	A Cl. of co. fc. fl. not rich.
19   19   24 (γ) Gem   P   8   15   n   0   15   15   15   15   16   16   16   16	8							1			A Cl. of L. and S. ic. ft. not rich.
19	1	-3	97 (2) = 11412	r	3	20	["	ľ	*3	-	a projecting point of the manage
11	9	19	24 (γ) Gemi	p	8	15	n	0	15	1	A Cl. of van. fc. ft. of various
11	70	Mar. 15	FO(2A) Canc	f	_	_	ſ		11	,	magnit, near & deg. not rich.
June 16   1 (m) Aquilæ   f   1 42 n   0 2 1   A Cl. of v. co. fc. ft.		16	50 Gemini	f							A Cl. of to ft
13	i	June 16	I (m) Aquilæ							ı	A Cl. of v. co. fc ft
14	13				12	48	ſ	0		1	A Cl. of co. fc. ft. not rich
15				P	44	48	n	τ	54	1	A Cl. of fc. pLft.
It may be called (if the expression be allowed) a forming Cl. or one that it ems to be gathering  A Cl. of many L. ic. ft.  A S. forming Cl. of if.  A Cl. of co. fc. ft. not rich.  A Cl. of co. fc. ft.  A Cl. of fc. ft.  A Cl. of co. fc. ft.  A Cl. of fc. ft. not rich, nor v. rich. 6 or 7' d.  A Cl. of a few co. fc. I. ft.  A Cl. of a few co. fc. II. ft.  A Cl. of a few co. fc. II. ft.  A Cl. of co. fc. ft.  A Cl. of co. fc. ft.  A Cl. of a few co. fc. II. ft.  A Cl. of a few co. fc. II. ft.  A Cl. of co. fc. ft.  A Cl. of co. fc. ft. not rich, nor v. rich.  A Cl. of co. fc. ft. not rich.  A Cl. of a few co. fc. II. ft.  A Cl. of co. fc. ft. not rich.  A Cl. of co. fc. ft.	2.1			P	103						A Cl. of co. fc. ft.
18 33 Vulpec   P   24 18 n   O   4   If may be called (if the expression be allowed) a forming Cl. or one that teems to be gathering A Cl. of many L. ic. ft.  18 20   Sept.   461(p)Aquilæ   P   2 54 n   O 18   I   A S. forming Cl. or one that teems to be gathering A Cl. of many L. ic. ft.  18 20   O   18 Vulpec   D   O   O   O   O   O   O   O   O   O	10	17	12 (φ) Cygni	1	13	6	1	0	44	1	A Cl. of not v. com. fl. closest M.
17	- 1		I	-		- 1					It may be called (if the expres-
18   Sept. 461(\$\rho\$) Aquilæ   P   24, 18   n   0   44   1   A   S. forming Cl. of st.	- 1		I	- 1		. 1					non he allowed) a forming Cl.
Sept. 4 6 1 (φ) Aquilæ P	17	18	33 Vulpec	p	24	- 1	n	0	4	r	A CL of many I to 6
19	18			P			- 1			- 1	A S. forming (1) of 0
20   9 10 v lipec   1   1   0   1   0   27   1   A Cl. of co. fc. ft. not rich.							- 1	0	- 1	1	A Cl. of co. fc. L. ft. not rich
10   Vulpec   P   2   27   n   0   29   2   A   Cl. of cL. co. fc. ft.	20			t			ſ	0	27	1	A Cl. of co. fc. ft. not rich.
23 Oct. 15 12 (γ) Delph p 5 18 n 0 3; I A Cl. of co. fc. ft.					2			0	29	- 1	A Cl. of cL. co. fc. ft.
24							3				A Cl. of co. fc. ft.
25		Oct. 15	(v) Orion	P						- 1	A Cl. of co. fc. ft.
26 Nov. 16 I (H) Gem P 2 16 n O 3 I by many Bft.  27 20 II (e) Navis P 36 41 n O 46 I A Cl. of ft. of various magnit.  28 Dec. 554(1\(\lambda\)) Orion P 11 53 f O 15 I A Cl. of fc. ft. not rich, nor v. com.  29 9 10I(4b) Aqu f 32 30 n O 11 I A Cl. of a few co. fc. L. ft.  30 -25 (8) Canis f 57 10 f I 15 I A vL. Cl. of many co. fc. L. ft.  31 Jan. 6 19 Monocer P 34 32 f O 41 I A Cl. of co. fc. ft. not v. rich.  32 34 32 f O 41 I A L. Cl. of fc. ft. not v. rich.  33 A Cl. of fc. ft. not v. rich.  34 Cl. of co. fc. ft. of many magn. p. rich. above 15' d.  36 A Cl. of fc. L. ft.  37 A Cl. of fc. ft. not v. rich.  38 A Cl. of fc. ft. not v. rich.  39 A Cl. of fc. ft. not v. rich.  30 A Cl. of fc. ft. not v. rich.  31 A Cl. of fc. ft. not v. rich.  32 A Cl. of fc. ft. not v. rich.  33 A Cl. of fc. ft. not v. rich.  34 A Cl. of fc. ft. not v. rich.  35 A Cl. of fc. ft. not v. rich.  36 A Cl. of fc. ft. not v. rich.  37 A Cl. of fc. ft. not v. rich.  38 A Cl. of fc. ft. not v. rich.  39 A Cl. of fc. ft. not v. rich.  30 A Cl. of fc. ft. not v. rich.  31 A Cl. of fc. ft. not v. rich.  32 A Cl. of fc. ft. not v. rich.  33 A Cl. of fc. ft. not v. rich.  34 A Cl. of fc. ft. not v. rich.  35 A Cl. of fc. ft. not v. rich.  36 A Cl. of fc. ft. not v. rich.  37 A Cl. of fc. ft. not v. rich.  38 A Cl. of fc. ft. not v. rich.  39 A Cl. of fc. ft. not v. rich.  30 A Cl. of fc. ft. not v. rich.  31 A Cl. of fc. ft. not v. rich.  32 A Cl. of fc. ft. not v. rich.  34 A Cl. of fc. ft. not v. rich.  36 A Cl. of fc. ft. not v. rich.  37 A Cl. of fc. ft. not v. rich.  38 A Cl. of fc. ft. not v. rich.  39 A Cl. of fc. ft. not v. rich.  30 A Cl. of fc. ft. not v. rich.										- 1	A SCI. of pl. white ft.
20 Nov. 10 I (H) Gem P 2 16 n O 3 I A Cl. of fl. of various magnit. 27 20 II (e) Navis P 36 4I n O 46 I A S. Cl. of fc. ft. not rich, nor v. 28 Dec. 5 54(Iλ) Orion P II 53 f O 15 I A Cl. of pL. fc. ft. not rich. 29 9 101(4b) Aqu f 32 30 n O II I A Cl. of a few co. fc. L. ft. 20 25 (δ) Canis f 57 10 f I 15 I A vL. Cl. of many co. fc. L. ft. 31 Jan. 6 19 Monocer P 34 32 f O 4I A Cl. of co. fc. ft. not v. rich. 32 34 2	-3				Ü	٦	۱ ا	•	4	١.	by many RG
27 20 11 (e) Navis p 36 41 n 0 46 1 not v. rich. 6 or 7' d.  28 Dec. 5 54(1\lambda) Orion p 11 53 f 0 15 1 A Cl. of fc. st. not rich. 29 9101(4b) Aqu f 32 30 n 0 11 1 A Cl. of a few co. sc. l. st. 20 1785	26	Nov. 16	(H) Gem		2 1	(6)	اء	2	3	1	A Cl. of fl. of verious manufacture
28 Dec. 5 54 (1λ) Orion p 11 53 f 0 15 1 A Cl. of fc. st. not rich, nor v. com.  29 9 101 (4b) Aqu f 32 30 n 0 11 1 A Cl. of a few co. sc. l. st.  30 25 (δ) Canis f 57 10 f 1 15 1 A Cl. of a few co. sc. l. st.  31 Jan. 6 19 Monocer p 15 36 n 1 3 1 A L. Cl. of sc. st. not v. rich.  32 Jan. 6 19 Monocer p 34 32 f 0 41 1 A Cl. of sc. st. not v. rich.  31 Jan. 6 19 Monocer p 34 32 f 0 41 1 A Cl. of sc. st. of many magn. p. rich. above 15' d.  32 Jan. 6 19 Monocer p 32 50 f 1 15 1 A Cl. of sc. st. of many magn. p. rich. above 15' d.  33 Jan. 6 19 Monocer p 32 50 f 1 15 1 A Cl. of sc. st. of many magn. p. rich. above 15' d.  34 Jan. 6 19 Monocer p 32 50 f 1 15 1 A Cl. of sc. st. of many magn. p. rich. above 15' d.  35 Jan. 6 19 Monocer p 32 50 f 1 15 1 A Cl. of sc. st. of many magn. p. rich. above 15' d.  36 Jan. 6 19 Monocer p 32 50 f 1 15 1 A Cl. of sc. st. of many magn. p. rich. above 15' d.  37 Jan. 6 19 Monocer p 32 50 f 1 15 1 A Cl. of sc. st. of many magn. p. rich. above 15' d.  38 Jan. 6 19 Monocer p 32 50 f 1 15 1 A Cl. of sc. st. of many magn. p. rich. above 15' d.  39 Jan. 6 19 Monocer p 32 50 f 1 15 1 A Cl. of sc. st. of many magn. p. rich. above 15' d.  30 Jan. 6 19 Monocer p 32 50 f 1 15 1 A Cl. of sc. st. of sc. st. of many magn. p. rich. above 15' d.  31 Jan. 6 19 Monocer p 32 50 f 1 15 1 A Cl. of sc. st. of sc. st. of many magn. p. rich. above 15' d.		-							1		not v. rich. 6 or 7' d
28 Dec. 5 54(1\(\lambda\)) Orion p 11 53 f 0 15 1 A Cl. of pL. fc. st. not rich. 29 9 101(4\(\lambda\)) Aqu f 32 30 n 0 11 1 A Cl. of a few co. sc. L. st. 30 -25(\(\lambda\)) Canis f 57 10 f 1 15 1 A VL. Cl. of many co. sc. L. st. 31 Jan. 6 19 Monocer p 15 36 n 1 3 1 A L. Cl. of sc. st. not v. rich. 32 - 0 26 Monocer p 32 50 f 1 15 1 A Cl. of co. sc. st. of many magn. p. rich. above 15' d. 34 - 0 26 36 f 0 52 1 A Cl. of sc. L. st. 31 A Cl. of sc. L. st. 32 A Cl. of sc. st. of sc. st. of many magn. p. rich. above 15' d. 33 A Cl. of pL, fc. st. p. rich. about	27	20 1	1 (e) Navis   1	2	36 <sub>4</sub>	,1 1	a	<b>)</b>	46	1	A S. Cl. of fc. ft. not rich, nor v.
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3- 10 26 Monocer P 34 32 f 0 41 I A Cl. of co. fc. ft. of many  33 ——————————————————————————————————		1785			3/ 4	٦,	Ι.	. ,	,2	•	A VL. Cl. of many co. ic. L. ft.
33	31		2 34		15 3	6 r	ווי		3	1	A L. Cl. of fc. ft. not v. rich.
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34	22			1.	aa =	7	١.		. ا ـ	-	magn, p. rich, above 15' d.
35 31 2 Navis P 21 23 n 1 21 3 A Cl. of pL, fc, ft. p. rich, about	34				ერ ე 26 ი	9 4					An extending Classics
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		- 1	1		•	7	1		1.	1	20' l. crooked fig.

vIII.	1785	Stars.		М.	s.		D	Μ.	ОЪ.	Description.
36	Jan. 31	19 Navis	P	43	20	n	I	0	1	A forming Cl. of co. fc. ft. 20 or 30' dia.
37	Feb. 4	6 Navis	P	16	47	n	I	43	2	AS. Cl of p. com. st. of various fizes not v. rich.
38		2 Navis	P	8	55	n	0	10	2	A Cl. of 'p. com L. and S. ft. R. abeve 15' d.
39	Mar. 4	II Monocer	f	23		1	1		3	An extensive Cl. of ic. st. of
40	II	47 Geminor	р	4	2	n	0	18	I	Clustering L. sc. st. many of equal nzc.

### Notes to some Nebulæ and Clusters of Stars.

- I. 7. This remarkable appearance being no longer in the place it has been observed, we must look upon it as a very considerable telescopic comet. It was visible in the finder and resembled one of the bright nebulæ of the Connonsance des Temps so much, that I took it for one of them till I came to settle its place; but this not being done till a month or two after the observation, the opportunity of pursuing and investigating its track was lost.
- I. 13.. The figures referred to, in the description of this and some other nebulæ, may be found in the Philosophical Transactions, vol. LXXIV. tab. XVII. P. 450.
- I. 28. The numbers annexed to some of the nebulæ refer to the class and number of the preceding Catalogue: thus, II. 41. denotes that the 41st in the second class is the third nebula, sollowing the two here described.
  - I. 28. Near the 84. and 86. neb. of the Connoissance des Temps.
- II. 6. This has probably been a telescopic comet, as I have not been able to find it again, notwithstanding the assistance of a drawing which represents the telescopic stars in its neighbourhood.
  - II. 55. The preceding is the 85 of the Connoissance des Temps.
  - II. 84. 6 or 8' following the 100 of the Connoissance des Temps.
  - II. 118. Just following the 88. of the Connoissance des Temps.
  - II. 123. 124. The third is the 87th of the Connoissance des Temps.
  - III. 44. The following is the 60th of the Connoissance des Temps.
- IV. 13. Before the value of the degree was more strictly ascertained, the two abservations were thus:

which, if there be no error in the place of the stars in FLAMITTID's Catalogue, desser about 14' in polar distance, for which reason in the second Paper on the Construction of the Heavens this nebula was put down twice, whereas it now appears, that both observations belong to the same.

V. I. This nebula was discovered Sept. 23, 1783, by my fister CAROLINI HERSCHEL, with an excellent small Newtonian Sweeper of 27 inches focal length, and a power of 30. I have therefore marked it with the initial letters, C. II. of her name. See also V. 19. discovered Aug. 27, 1783, and VII. 13. discovered Feb. 26, 1783.

V. The Front-view is a method of using the reflecting telescope different from the Newtonian, Gregorian, and Cassagrain forms. It consists in looking with the eye glass, placed a little out of the axis, directly in at the front, without the interpofition of a small speculum; and has the capital advantage of giving us almost double the light of the former constructions. In the year 1776 I tried it for the first time with a 10 feet reflector, and in 1784 again with a 20 feet one; but the success not immediately answering my expectations, it was too hastily laid aside. By a more careful repetition of the same experiment I find now, that several other considerable advantages, added to the brilliant light before mentioned, make it so valuable a construction that a judicious observer may avail himself of it at least in all cases where light is more particularly wanted; and from the experience of 30 sweeps, which I have already made with it, I may venture to announce it to be a very convenient and pleasant, as well as useful, way of observing. With regard to the position of objects, it differs from other constructions, by inverting the north and fouth, but not the preceding and following.

#### . Errata of the Catalogue.

The following nebulæ should stand thus.

I. 54.	35 (1) Andr. 18 36 1 26	pB. S. R. vgbM.
	In the description read	F. cL. mE. bM. er.
II. 239.	In the description read	The 2d of two.



XXVIII. Investigation of the Cause of that Indistinctness of Vision which has been ascribed to the smallness of the Optic Pencil. By William Herschel, LL.D. F.R.S.

#### Read June 22, 1786.

S OON after my first essays of using high powers with the Newtonian telescope, I began to doubt whether an opinion which has been entertained by feveral eminent authors, "that " vision will grow indistinct, when the optic pencils are less " than the 40th or 50th part of an inch," would hold good in all cases. To judge according to so rigid a criterion, I perceived that I was not intitled to fee distinctly with a power much more than about 320, in a 7-feet telescope which bore an aperture of 6,4 inches; whereas in many experiments on double stars I found myself very well pleased with magnifiers that far exceeded such narrow limits. This induced me, as it were, by way of apology to myfelf, for feeing well where I ought to have feen less distinctly, to make a few experiments on the subject of the diameter of optic pencils. It occurred to me, that an opinion which limits them to any given fize cannot be supported by theory, which does not determine on subjects of this manny other be decided, like many other physical questions relating to matters of fact, by careful experiments made upon the fubject. The way, therefore, to come at truth, in a case which seemed to me of considerable impostance, lay still open to me; as it had done to former obfervers: fervers; and I thought myself authorised, according to a Cartesian maxim (Dubia etiam pro falsis habenda), to suppose, for a while, the size of optic pencils, requisite for distinct vision, intirely undecided.

The first opportunity I had of making the proposed experiments was in the year 1778, and the result of them proved so decisive that I have never since resumed the subject; and had it not been for a late conversation with some of my highly esteemed and learned friends, I might probably have left the papers, on which these experiments were recorded, among the rest of those that are laid aside when they have afforded me the information I want. But a doubt seeming still to be entertained on the subject of the smallness of the optic pencils, it may now be proper for me to communicate these experiments, that it may appear how far the conclusions I have drawn from them are warranted by the facts on which I suppose them to rest.

#### Experiments with the naked eye.

Exp. 1. Through a very thin plate of brass I made a minute hole with the fine point of a needle; its magnified diameter, very accurately measured under a double microscope, I sound to be ,465 of an inch, while under the same apparatus a line of ,05 in length gave a magnified image of 3,545 inches. Hence I concluded, that the real diameter of the perforation was about the 152d part of an inch. Through this small opening, held close to the eye, I could very distinctly read any printed letters on which I made the trial. Proper allowance that he made for the very inconvenient situation of the eye, which by the unusual closeness to the paper cannot be expected

to see with its common facility. Besides, the continual motion of the letters, which is required on account of the smallness of the sield of view, must needs take up a considerable time.

Exp. 2. In some other pieces of brass I made smaller holes; and among many, that were measured with the same accuracy as in the former experiment, I sound one whose magnified diameter was, 29: hence the real diameter could not exceed the 244th part of an inch. Through this opening I could also read the same letters; but the difficulty of managing so as not to intercept all the incident light, as well as the very uneasy situation of the eye, were sufficient reasons for not carrying the intended experiments any further under this form. Besides, I should hardly have allowed them to be fair, if, on a further contraction of the hole in the brass plate, an indistinctness had come on; as we might well have suspected at least two other causes, besides the smallness of the pencils, to contribute to such an impersection; viz. want of light, and a deslection of it on the contracted edges of the hole.

#### Microscopic Experiments.

Exp. 3. I had now recourse to a double microscope, consisting, for simplicity's sake, of only two lenses. The focal length of the eye-glass, carefully ascertained by an object half a mile off, being ,9; the distance of the object-glass from the eye-glass 9,36; and the aperture of the object-glass ,0405. Hence we compute that the diameter of the optic pencil, when it entered the eye, could not exceed the 232d part of an inch; yet with this construction I saw very distinctly every object I ced under the microscope.

- Exp. 4. I reduced the aperture of the object-glass to ,013; hence the pencil was found to be the 724th part of an inch; and yet I saw with this construction very distinctly every object that was placed under the magnifier.
- Exp. 5. I made a fecond reduction of the aperture of the object-glass, so that now it was no more than ,0052; and therefore the optic pencil less than the 1800th part of an inch; and yet I could very well count the bristles on the edge of the wing of a fly, and distinguish their length and thickness.
- Exp. 6. Changing the construction of the microscope, I now reduced the pencils by an increase of power. Solar focus of the eye-glass, 52; distance between the object-glass and eye-glass 7,6; aperture the same as in the third experiment. This gave me a pencil of the 336th part of an inch, with which I saw very distinctly.
- Exp 7. Applying now the reduced aperture of the fourth experiment, I had a pencil of the 1139th part of an inch, with which I saw very well.
- Exp. 8 I changed the eye lens for another of ,171 focal length; the object glass and distance between the two lenses remaining as in the two last experiments; aperture,02. This gave a pencil of the 2173d part of an inch, with which I could count, or rather successively see, the bristles before mentioned very well; the field, on account of the great power, not taking in more than two large and a small one at a time.
- Exp. 9. I was now convinced, that we may fee distinctly with pencils incomparably less than the 40th or 50th part of an inch; and indeed so far from expecting any obstruction to distinct vision from the smallness of the pencils, it appeared to me now as if their size might in suture be intirely lest out of the account. With a view, however, of seeing what other:

cause might bring on that indistinctness which had been ascribed to the smallness of the optic pencils, I continued these experiments with a variation in the apparatus, and used now an object lens of a different socal length; the aperture and other particulars being as in the 4th experiment. By this construction, which gave me a pencil of the 724th part of an inch, I could see objects very well; but though they appeared distinctly, they were not so sharp on the edges as one would wish to see them. This being compared with the 4th experiment, it appeared that, with equal pencils, unequal degrees of distinctness may take place; and a pretty striking circumstance, which served to lead me in the following experiments, was, that the smallest power gave me the least distinct image; notwithstanding, from former trials, the goodness of the lenses I employed could not be doubted.

Exp. 10 On an examination of circumstances it occurred to me, as indeed I had already before surmised, that a certain proportion of aperture might be necessary to a given socal length of an object-lens or speculum; and that a failure in this point might probably bring on that indistinctness which had been ascribed to the smallness of the pencils. In order, therefore, to put this to a trial, I used now an object-lens of 1,25 socal length, with an aperture consined to ,01; the rest of the apparatus being as in the 3d, 4th, and 5th experiments. The pencil in this case was about the 1000dth part of an inch; and though by a different construction I had already seen very well with a pencil of not half that diameter, I sound this to give me, as now I had reason to expect, a very indistinct that the stiect.

Exp. 11. Increasing the aperture of the object-lens to ,0124, I had a pencil of the 758th part of an inch, but could see no better with it.

Exp. 12. Proceeding in the track now pointed out to me, I admitted an aperture of ,017, which gave a pencil of the 550th part of an inch, but could fee not much better with it than before.

Exp. 13. On a farther increase of the aperture to ,0231, and a pencil of the 406th part of an inch, I saw a little better; but still had not distinctness enough even to see the bristles before-mentioned at all. Hence we may conclude, that, in such constructions as the present one, the aperture of the object-glass must bear a considerable proportion to its focal length; since the 54th part (for ,0231: 1,25:: 1:54) is here not nearly sufficient.

Exp. 14. To the same apparatus I applied a higher power, by an exchange of the eye-glass; but the indistinctness tempined as before.

Exp. 15. Returning again to the former construction, I admitted an aperture of about ,037; and having now a pencil of nearly the 250th part of an inch, I could but just perceive some of the large bristles, which shows that even the 34th part (for ,037: 1,25:: 1: 34) of the socal length is not a sufficient aperture for object-lenses that act under such circumstances as the present.

So far I have only related experiments that were made in the year 1778; and my opinion that the smallness of the optic. pencils could be no objection to seeing well being thus supported by evident sales. I hestated not, in a Paper on the Parellax of the Fixed Stars (Phil. Trans. vol. LXXII. p. 96.) to efficient that we might see distinctly with pencils much smaller.

smaller than the 40th or 50th part of an inch. It did not appear to be necessary, nor would the subject of that Paper permit me to enter into a detail of experiments; but having, in the course of my reading about that time, met with an account of some very small globules made for microscopic uses, I contented myself with an instance of small pencils taken from them. I shall, however, now proceed just to hint at a few inferences that may be drawn from these related experiments; as, upon a mature confideration, we may find reason to believe they point out a cause of indistinctness of vision hitherto never noticed by optical writers; and which, when properly investigated, cannot but influence, and in some respects contribute to the improvement of, our theories in optics. For, admitting that every object-glass or speculum, whose aperture bears less than a certain ratio to its focal length, will begin to give an indistinct picture, it will follow, that while former opticians have been endeavouring to diminish the aberrations arifing from the spherical figure, and the different refrangibility of rays, by increasing the focal length, they have been unaware of exposing themselves to the consequences of the cause of indistinctness here pointed out. And till its influence shall be well ascertained and brought to a proper theory, we must sufpect that fuch tables as those which are given in our best authors of optics, pointing out an aperture of less than 6 inches for a glass of 120 feet focal length (or a ratio of 1 to 240) must be far from having that degree of perfection which may yet be obtained. No wonder that telescopes, made according to theories or tables, where one of the causes of indiffinctness is unfuspected, and therefore left out of the account, can bear no smaller pencil than the 40th or 50th part of an certainly

certainly run into great imperfections, we ought nevertheless also to consider what dangers, on the other, we may incur by lessening them too much.

As foon as convenient, I intend experimentally to pursue this subject, in order to obtain proper data for submitting this cause of optical impersection to theory; at present my engagement with the work of a 40-seet resector will hardly permit so much leisure; and till I shall have repeated, extended, and varied these experimental investigations, I would wish them to be looked upon as mere hints that may afford matter for suture disquisitions to the theoretical optician.



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Medical Transactions published by the College of Physicians in London. Vol. III. London, 1785.

Transactions of the Society, instituted at London for Encouragement of Arts, Manufactures, and Commerce. Vol. III. London, 1785.

The abridged Minutes of the Society of Arts in Barbados, continued [from page 45 to 98].

Kongl. Vetenskaps Academiens nya Handlingar. Tom. IV. for 1783, and the first quarter of tem. V. for 1784. Stockholm. Donors.

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